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9.71 Functional MRI of High-Level Vision
Fall 2007

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Lecture 8B

Number: A Candidate “Special” Domain of Cognition

I. Understanding approximate number

Adults

Infants

Animals

II. Brain basis of number:

neuropsychological patients

fMRI understanding approximate number

Understanding Number

- “animals, young infants, and adult humans possess a biologically determined, domain-specific representation of number”
- “a specific neural substrate, located in the left and right intraparietal area, is associated with knowledge of numbers and their relations (‘number sense’). The number domain is a prime example where strong evidence points to an evolutionary endowment of abstract domain-specific knowledge in the brain because there are parallels between number processing in animals and humans.”

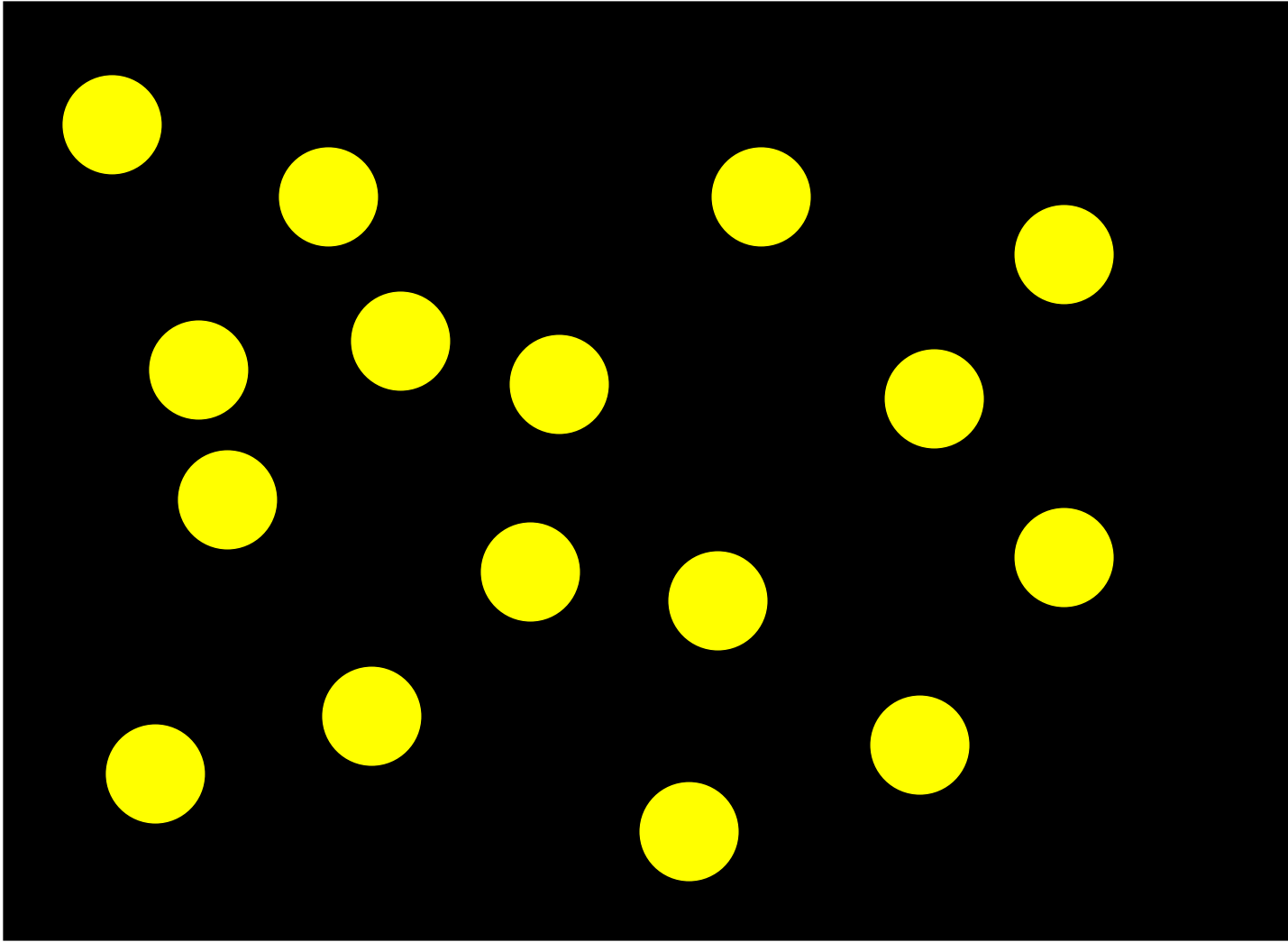
–Dehaene, Dehaene-Lambertz & Cohen, TINS, 1998

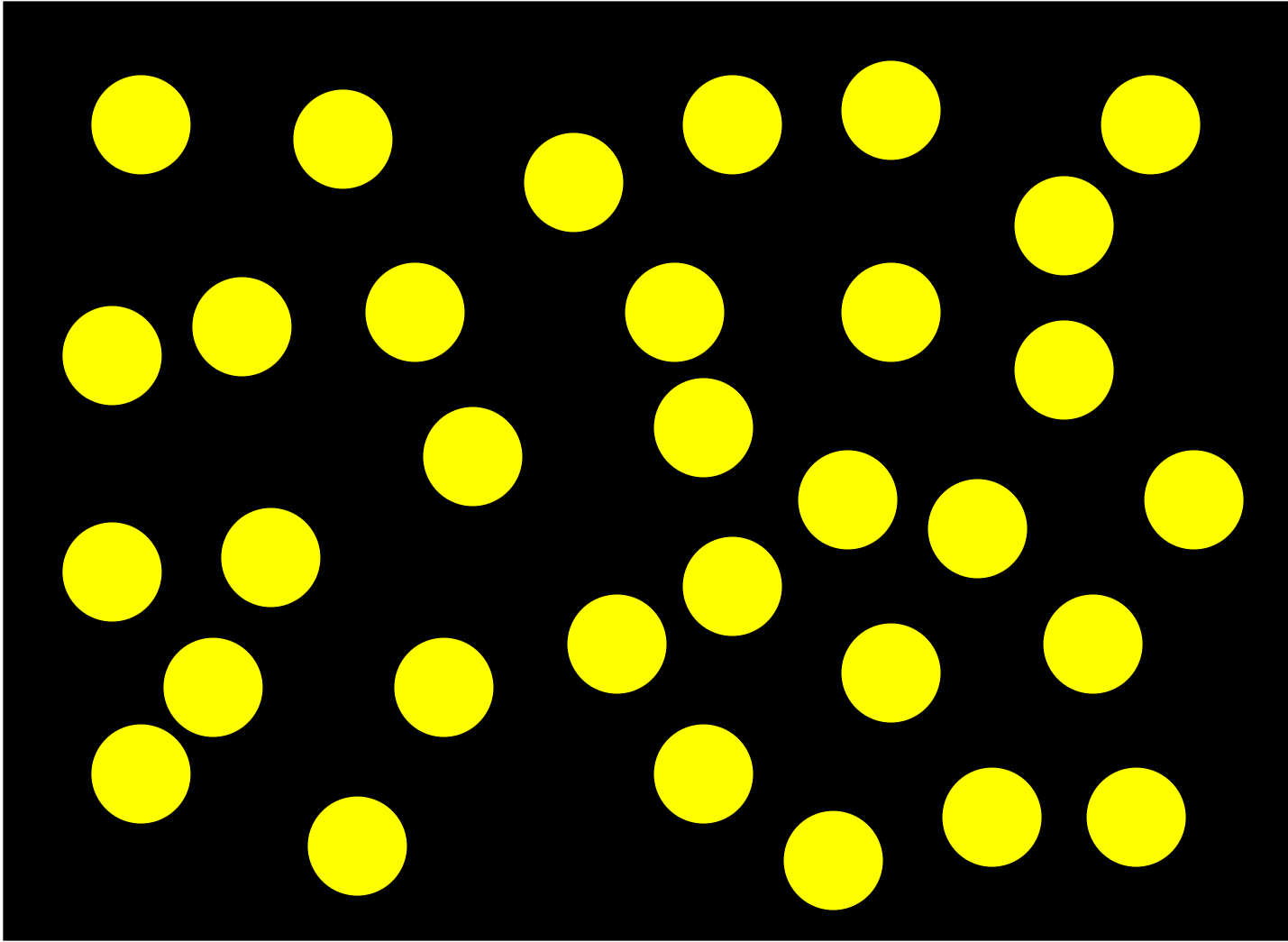
What does “number sense” mean?

- Adults can represent large numerical magnitudes without verbal counting.
- The representations are approximate; discriminability of two numerosities depends on their ratio.
- The representations are abstract.
- The representations enter into arithmetic computations (addition).

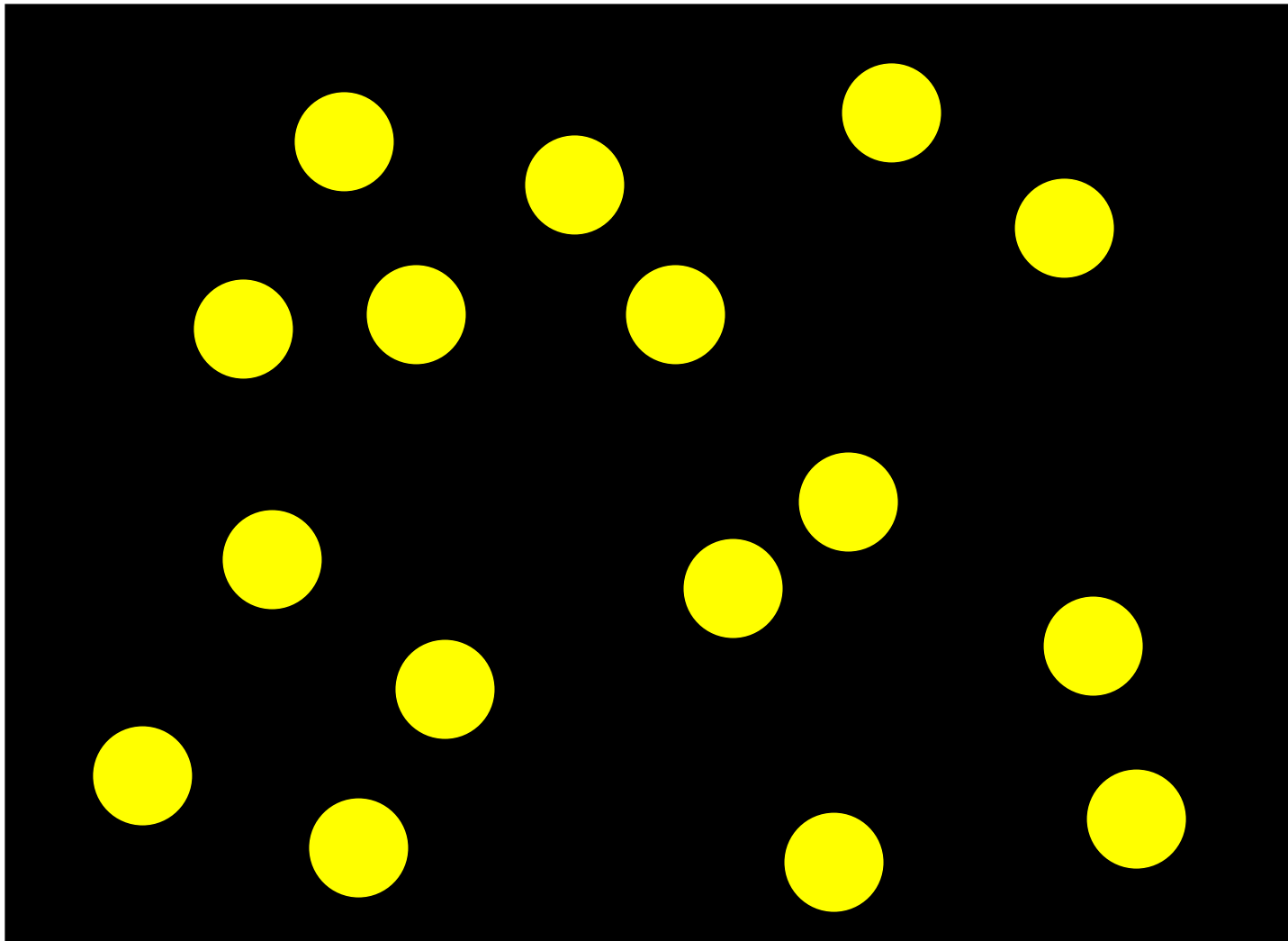
For example.....

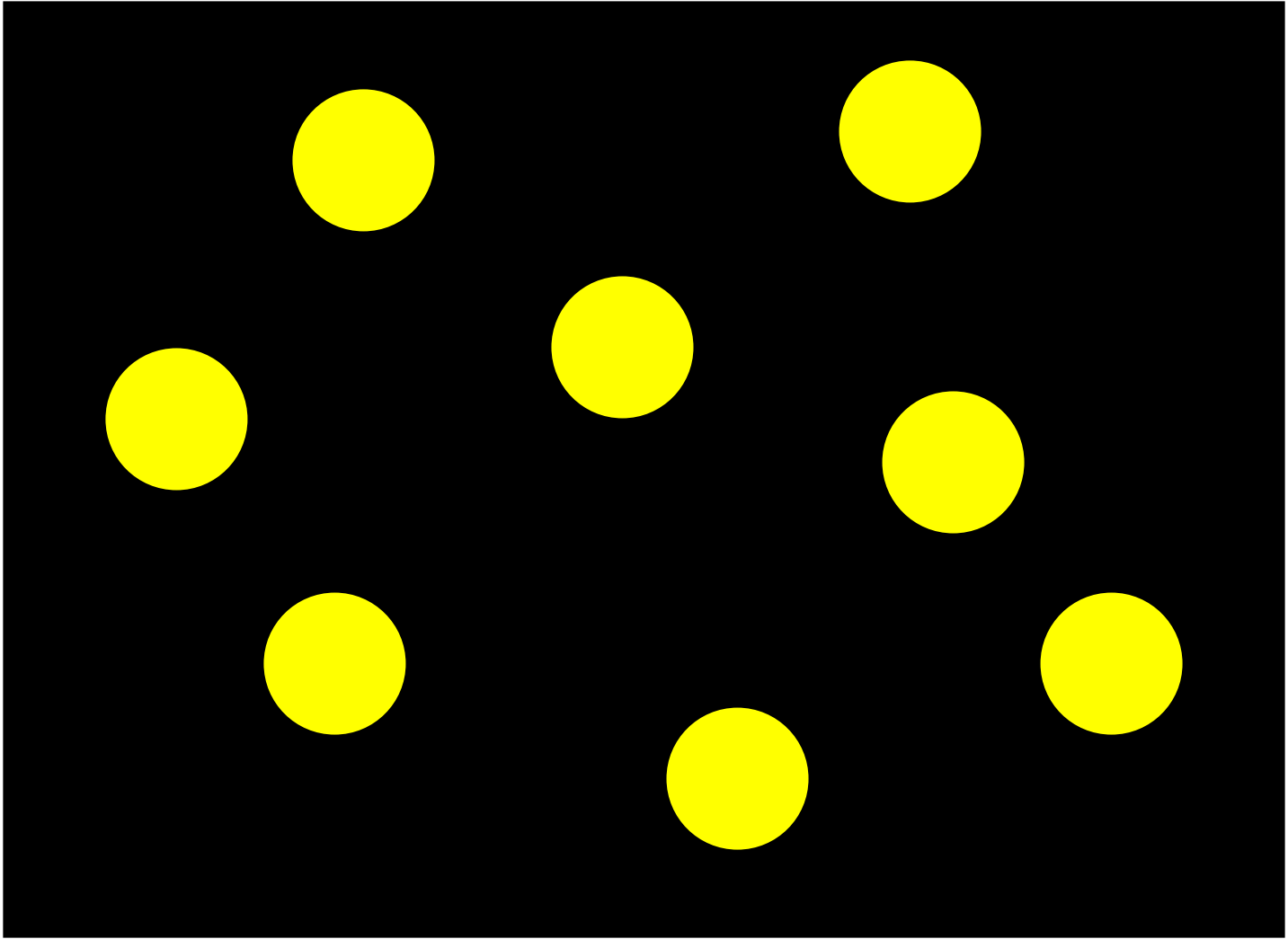
Which has more dots?



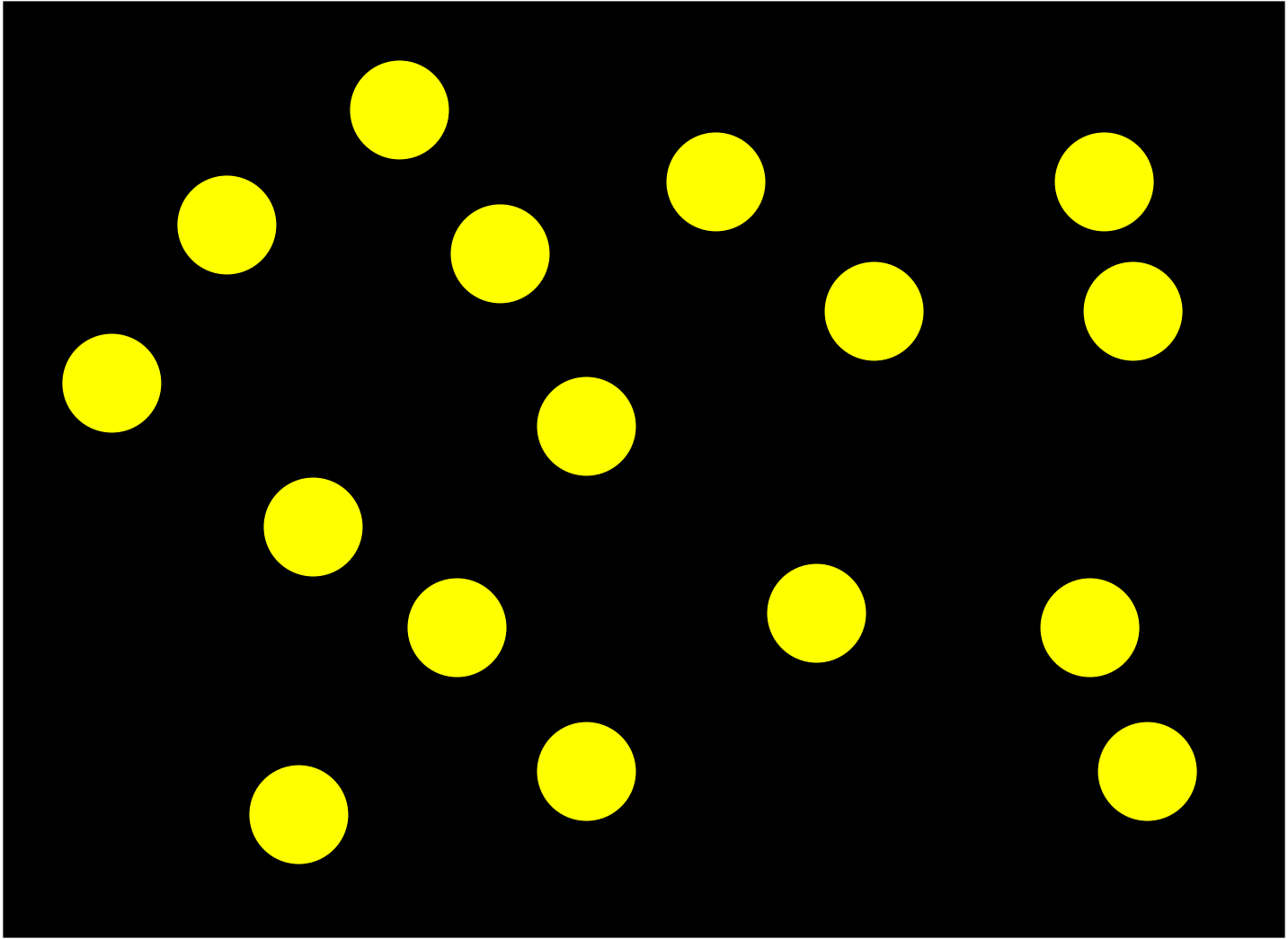


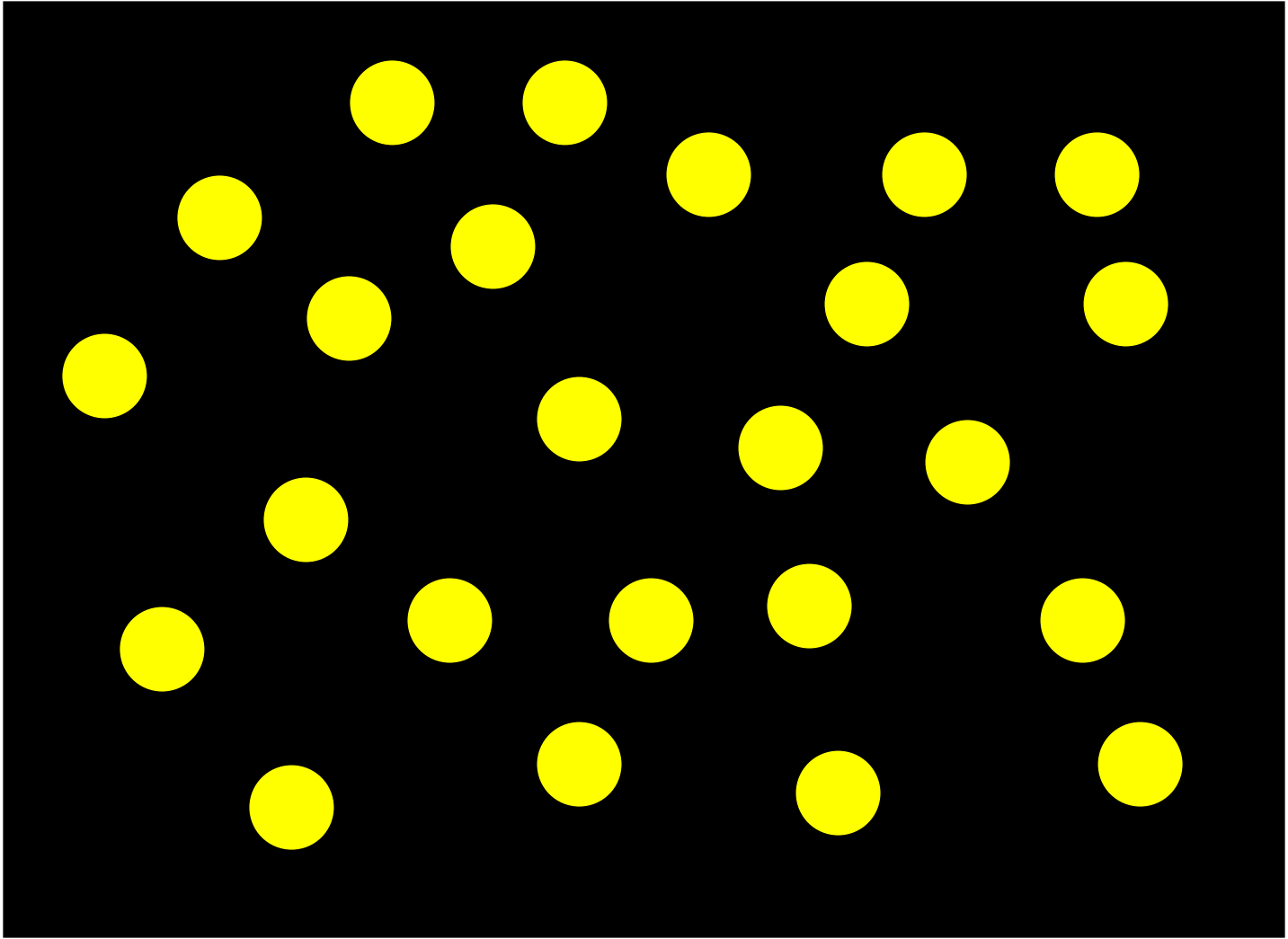
Which has more dots?



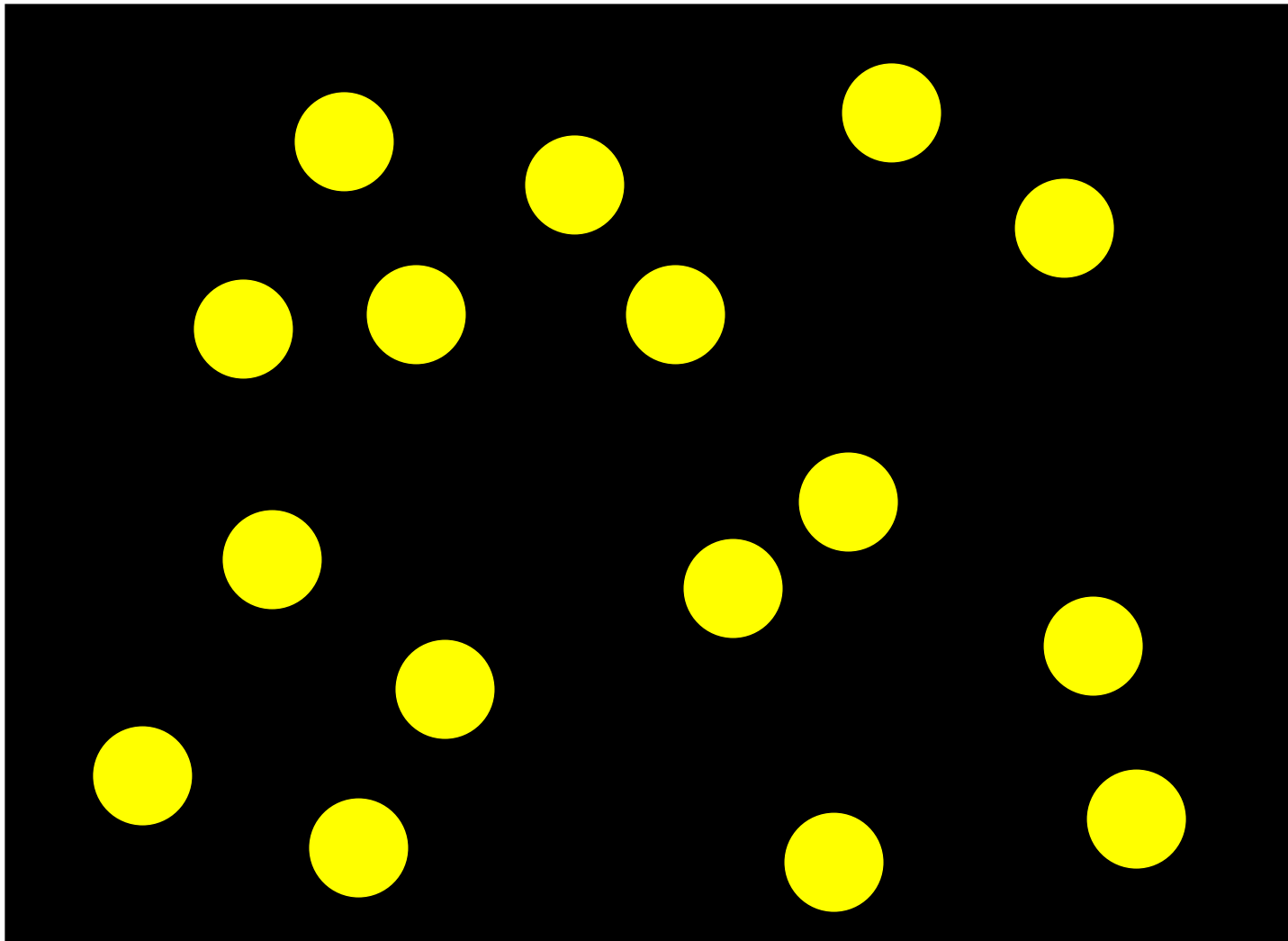


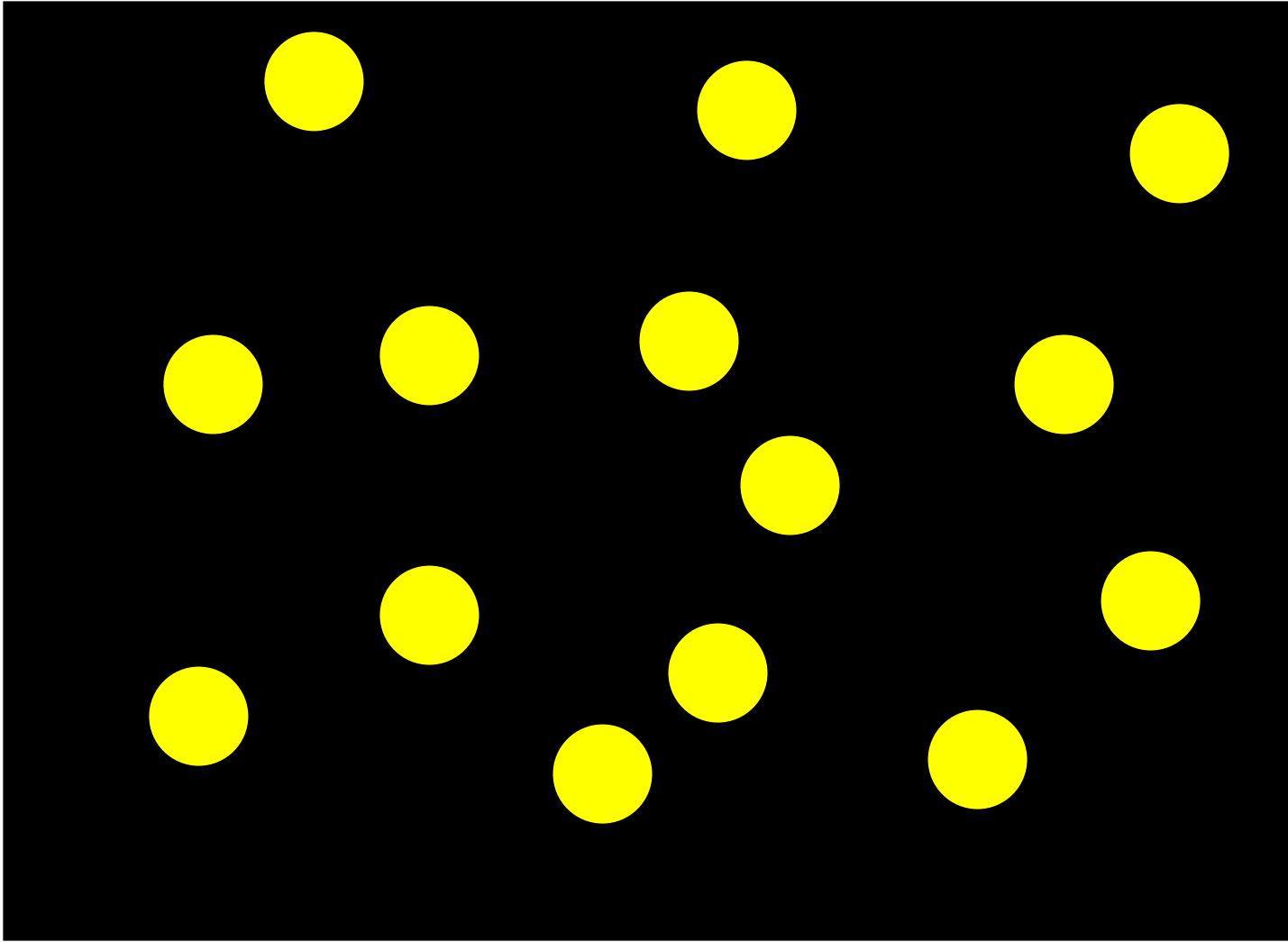
Which has more dots?



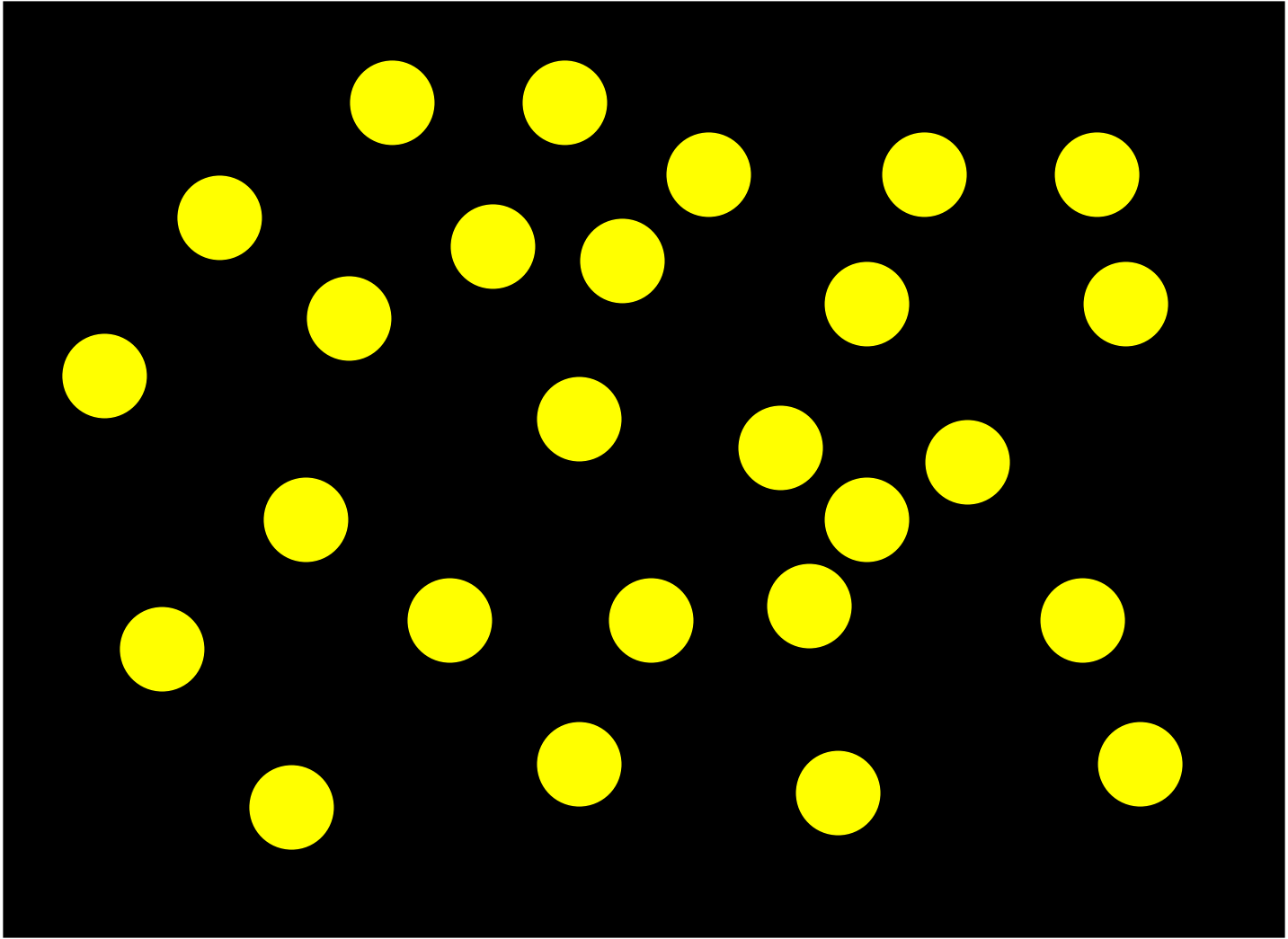


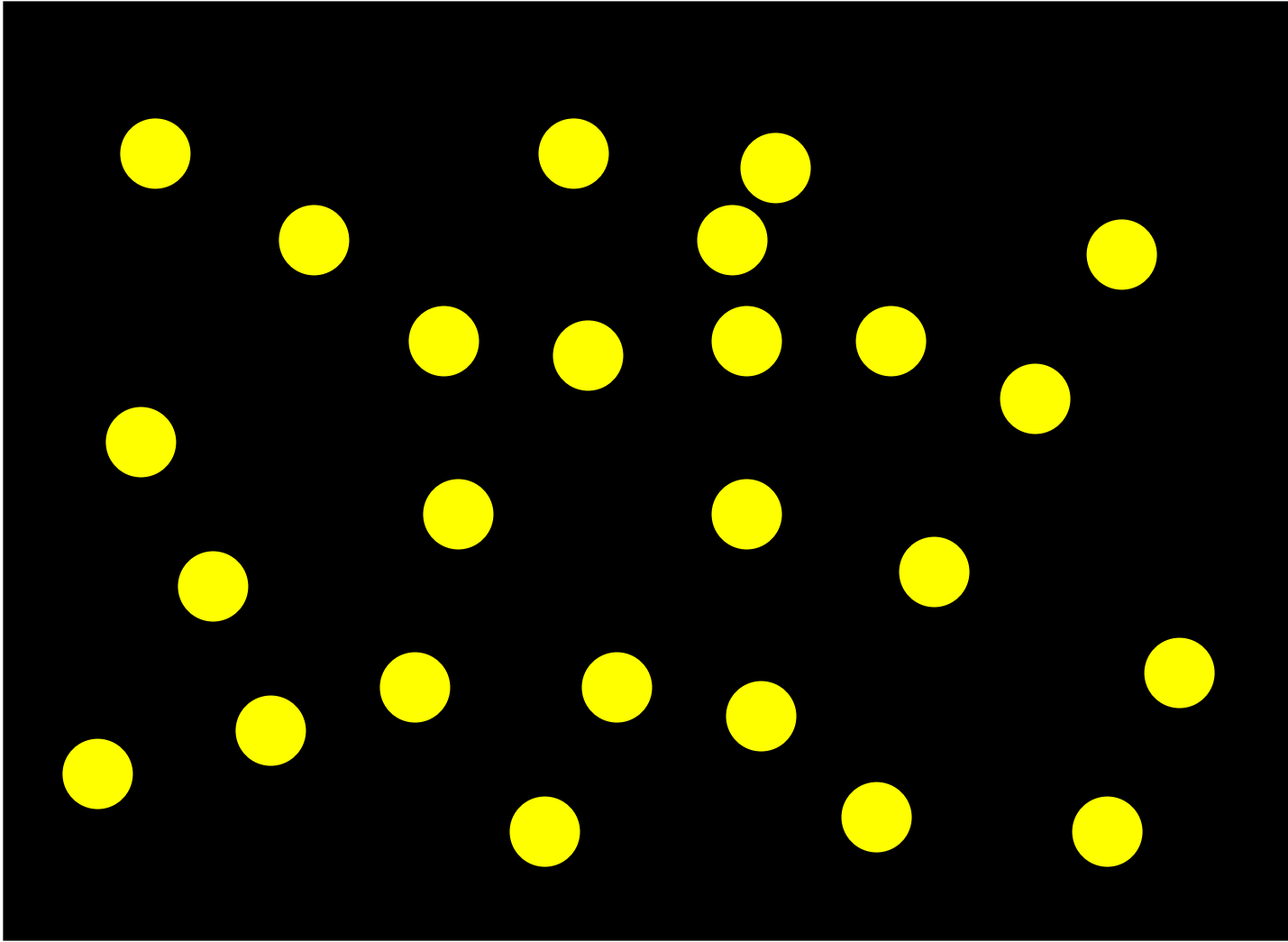
Which has more dots?





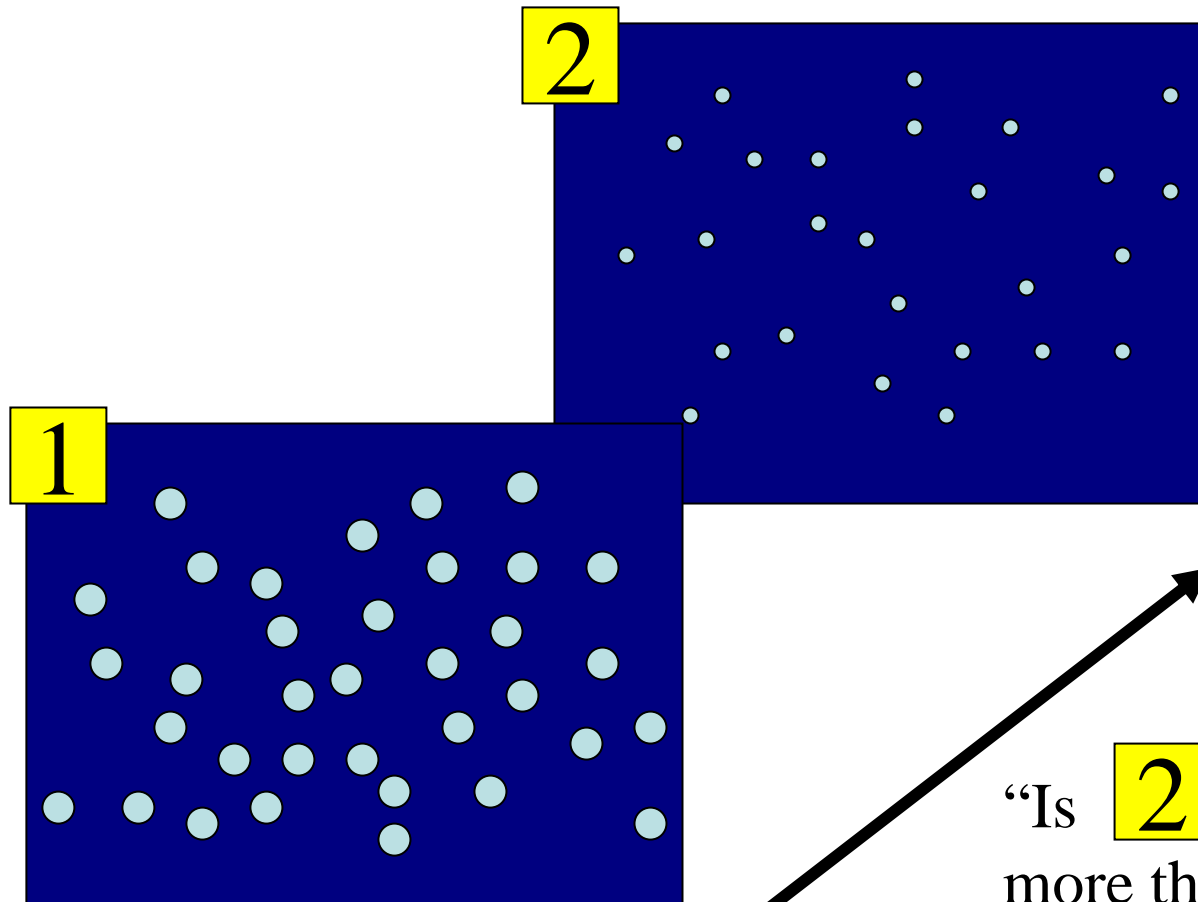
Which has more dots?





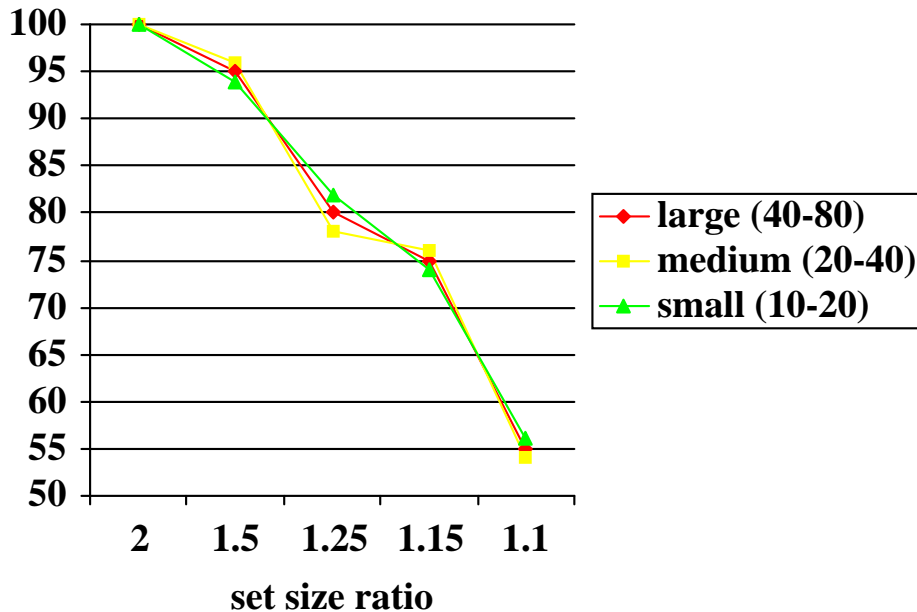
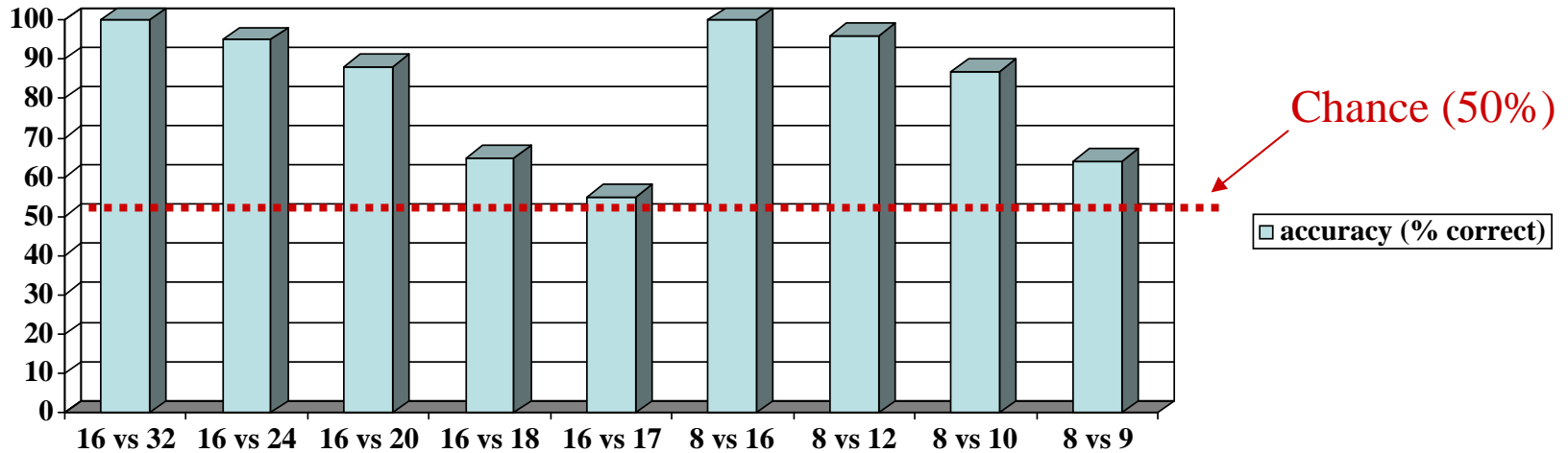
How did you do this?
Did you count verbally?
Which ones were harder?

How accurate are adults' large number representations? (Barth, Kanwisher & Spelke, 2003)



“Is **2** fewer or
more than **1**?”

Numerosity discrimination by adults (Barth)

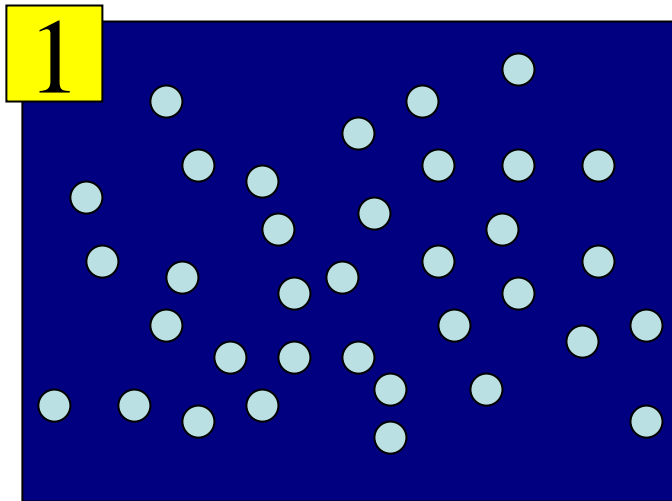
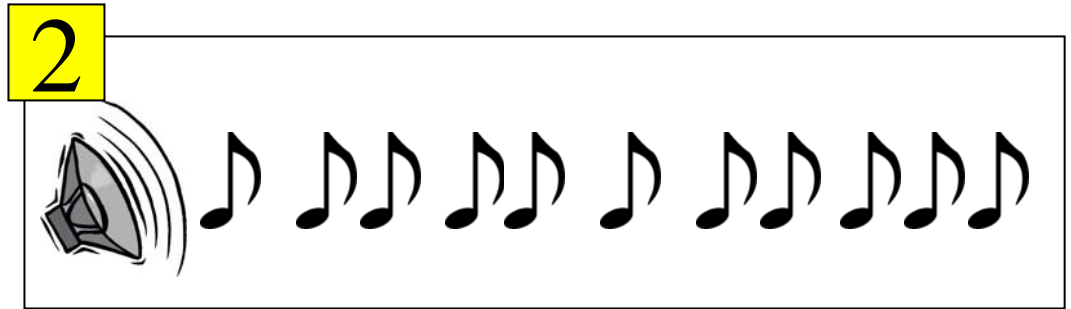


Weber's Law:
The discriminability of two numerosities depends on their *ratio* (not absolute diff).

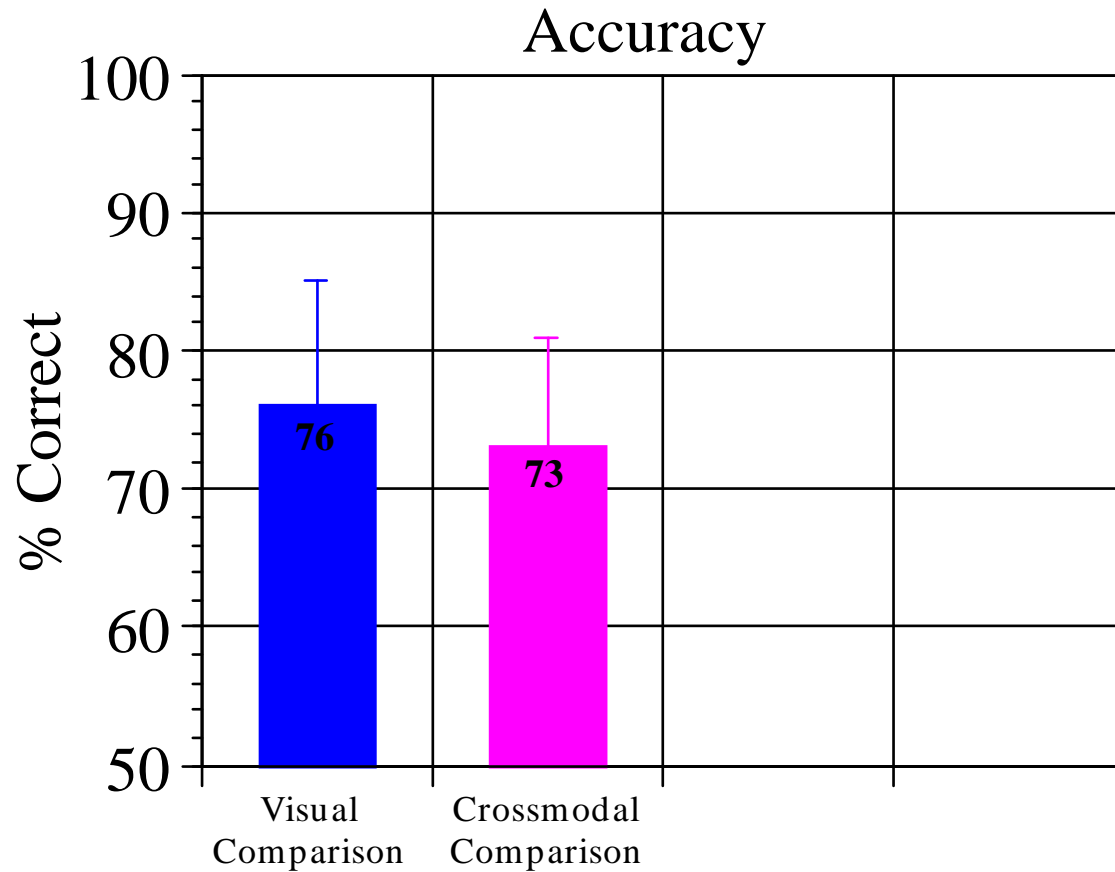
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- ✓ • The representations are not based on continuous quantities like *area*, but rather on discrete *number*.
- ? • The representations are abstract.
- ? • The representations enter into arithmetic computations (addition).

How abstract are adults' large number representations?



“Is **2** fewer or more than **1**?”



Cross-modal comparisons are almost as accurate as comparisons within the visual modality alone.

What does “number sense” mean?

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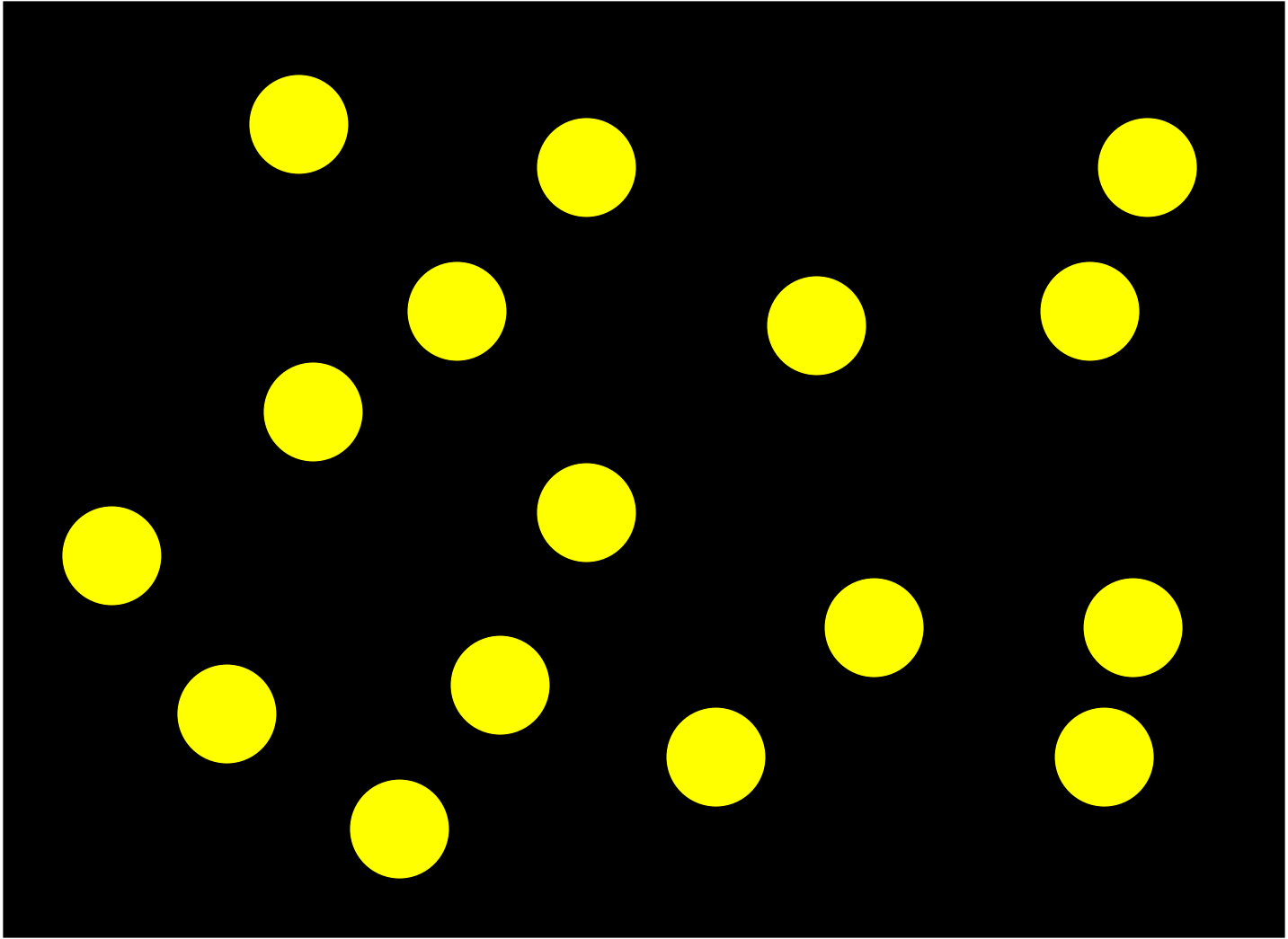
What can adults do with these large number representations?

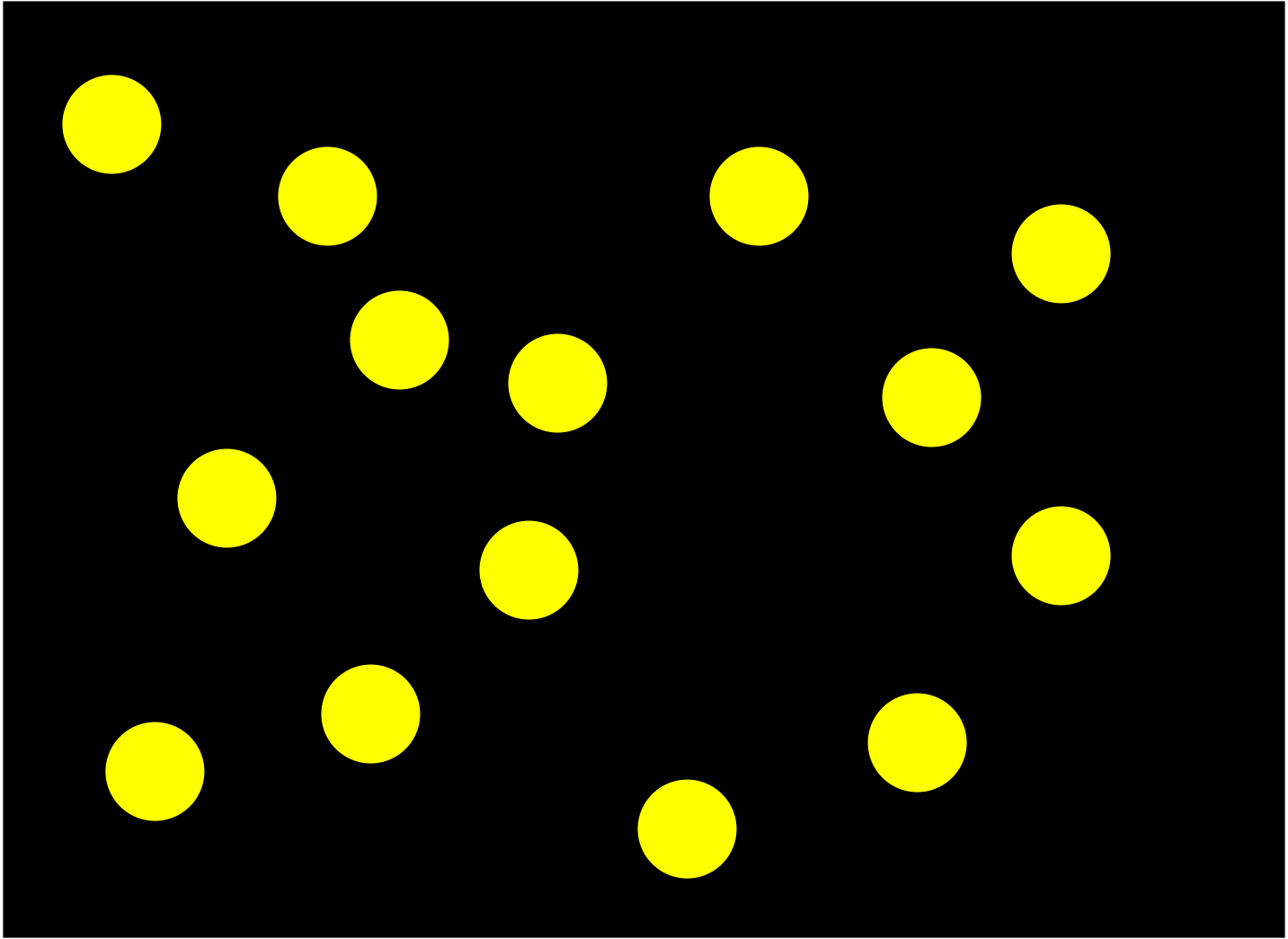
Addition of visual arrays

“add”

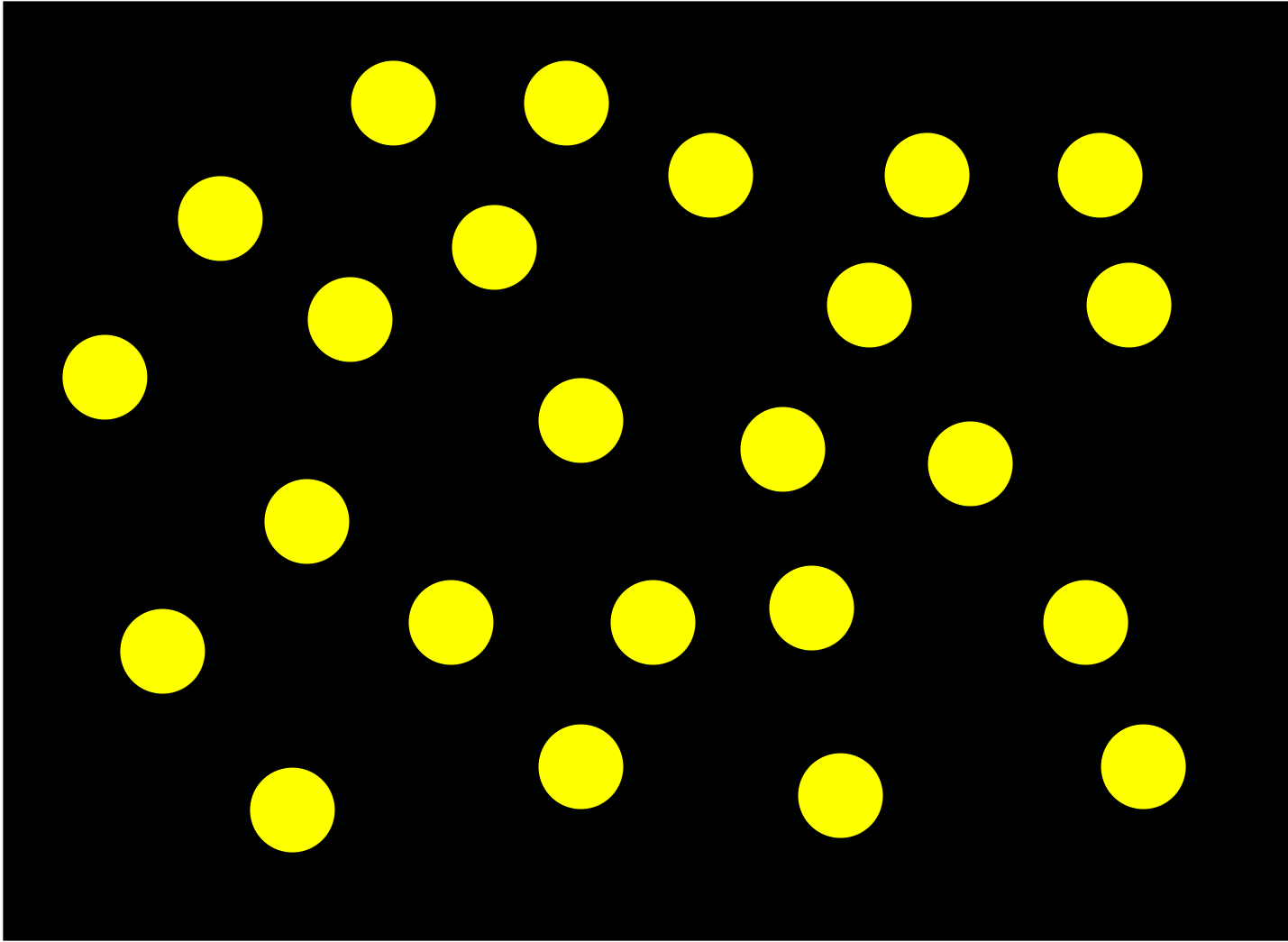
For example...

“Is the sum of **1** and **2** fewer or more than **3**?”



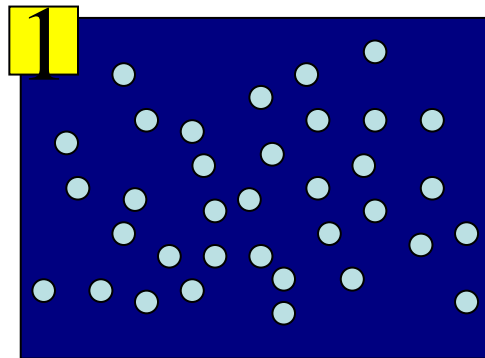


add

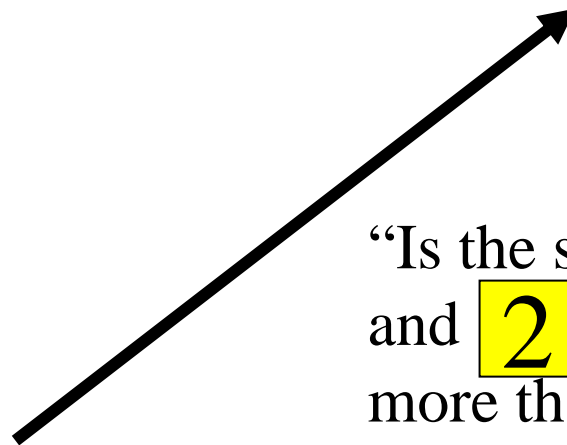
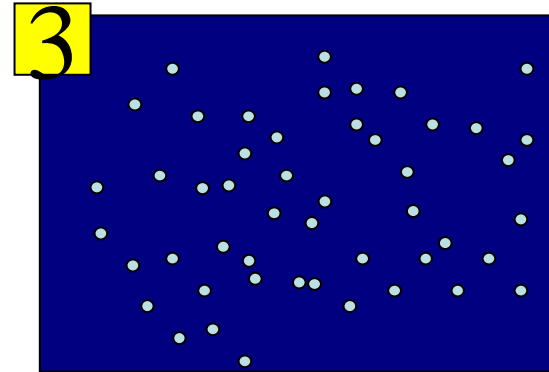


What can adults do with these large number representations?

Cross-modal addition

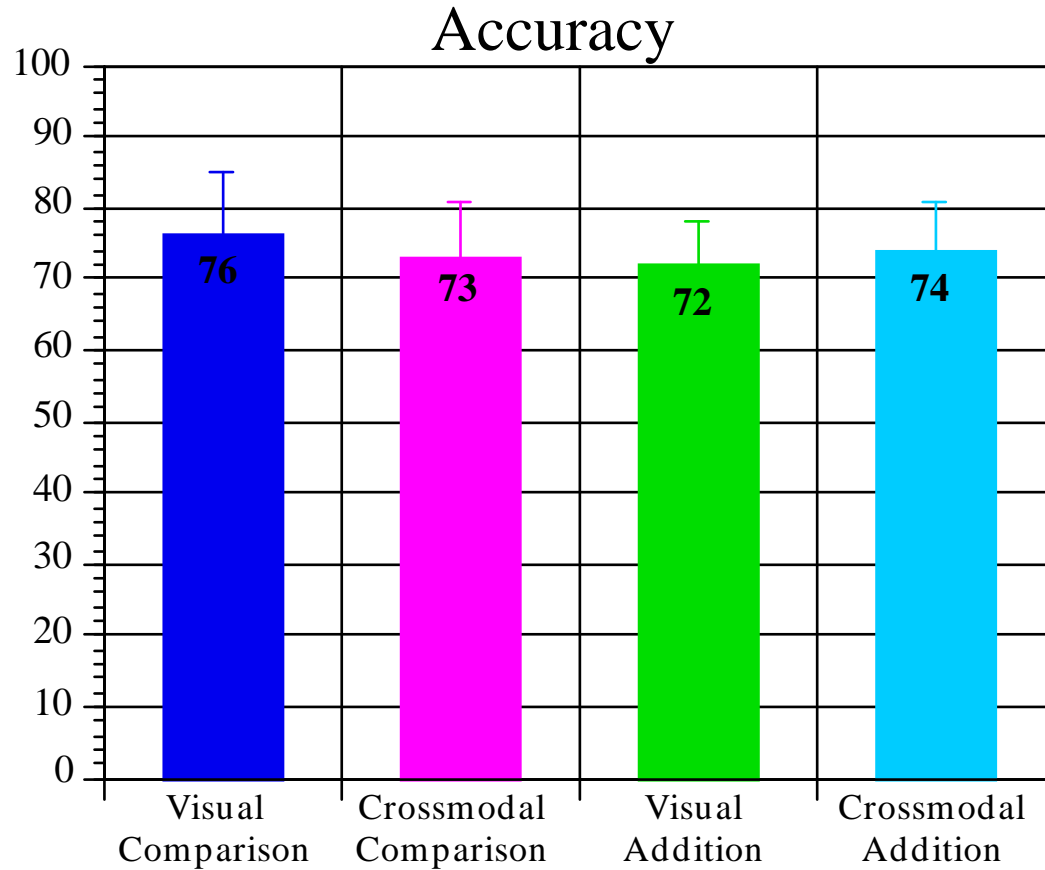


“add”



“Is the sum of **1**
and **2** fewer or
more than **3**?”

Nonsymbolic Comparison and Addition



Barth (2001)

What does “number sense” mean?

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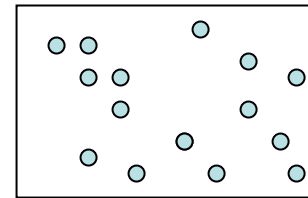
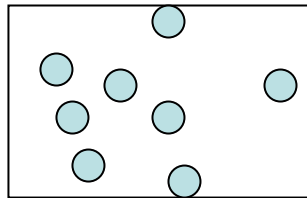
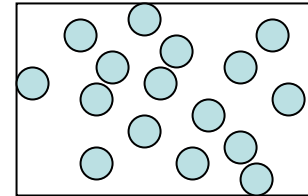
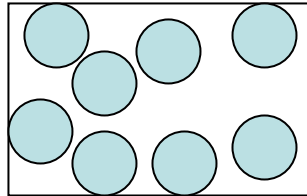
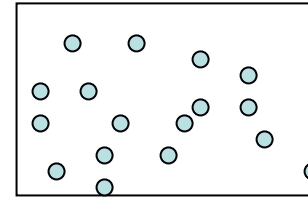
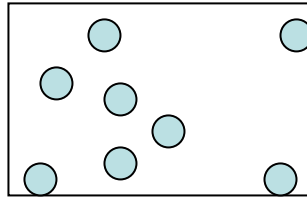
But: the people in these studies have spent years learning and using formal arithmetic. Do these abilities exist in infants? Animals?

Large number representations in infants

8

16

Habituation

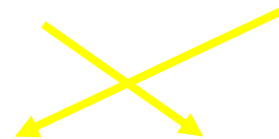


Old number

New number

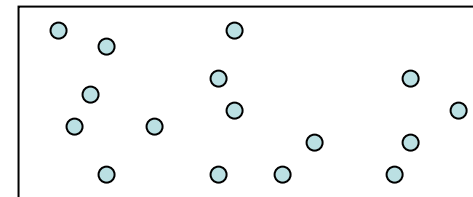
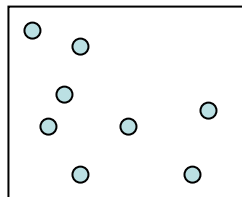


(...)



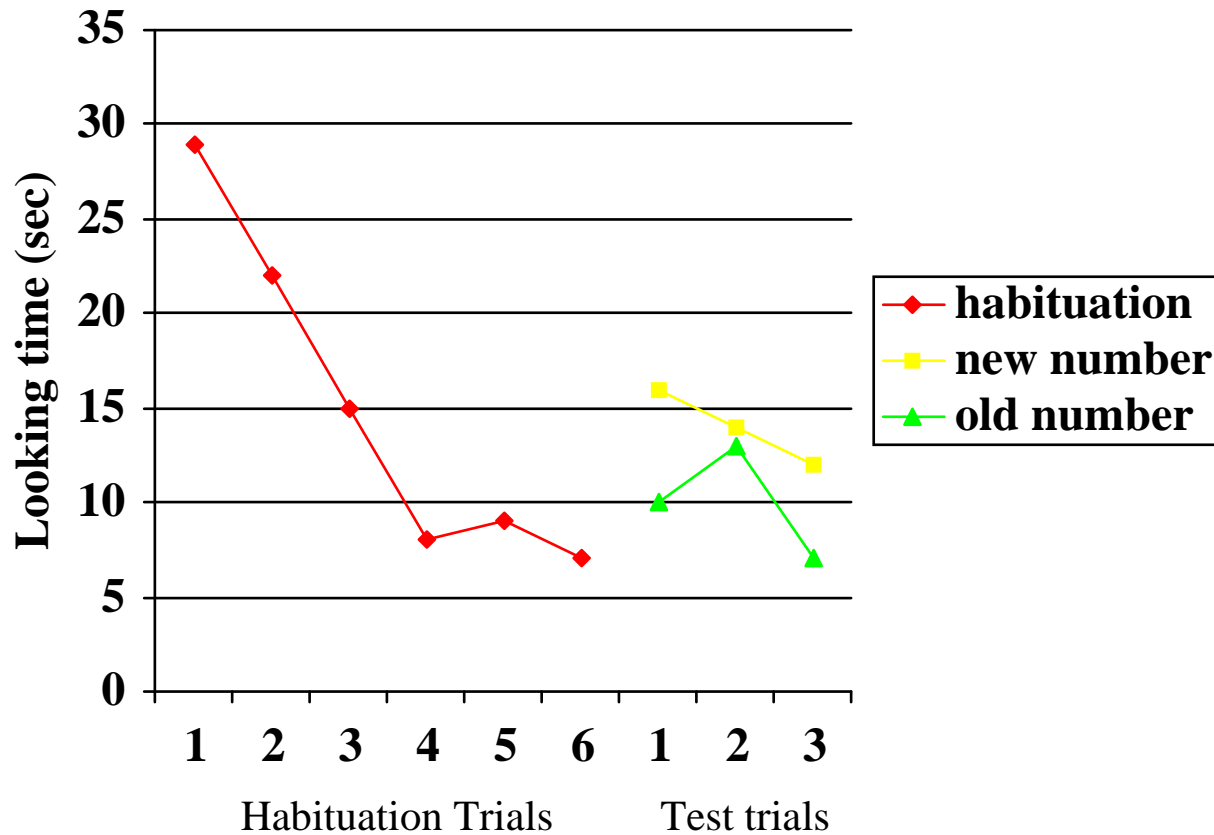
(...)

Test



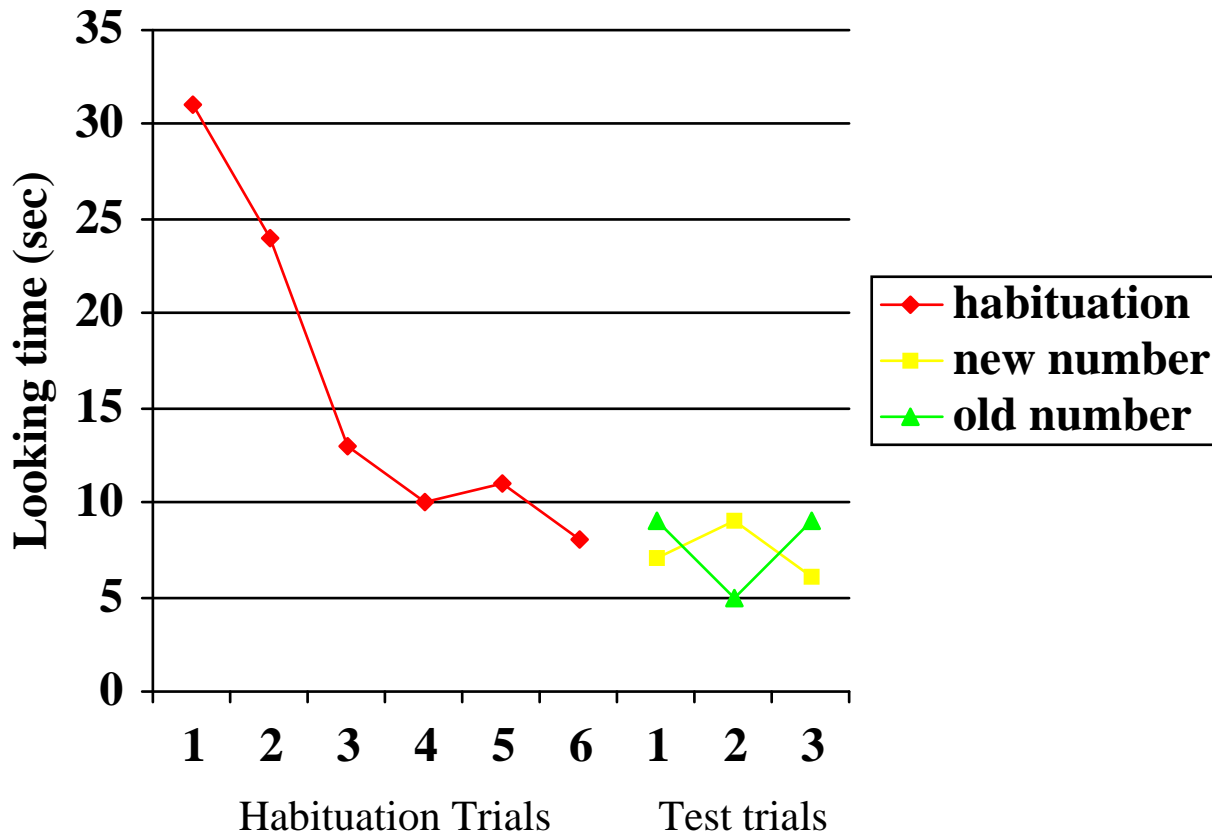
Xu & Spelke (2000)

Discriminating 8 vs. 16 dots at 6 months



Infants discriminate between large numerosities in dot arrays.

Discriminating 8 vs. 12 dots at 6 months



Infants' number representations are imprecise.

Large number representations in non-human animals

The case of Clever Hans

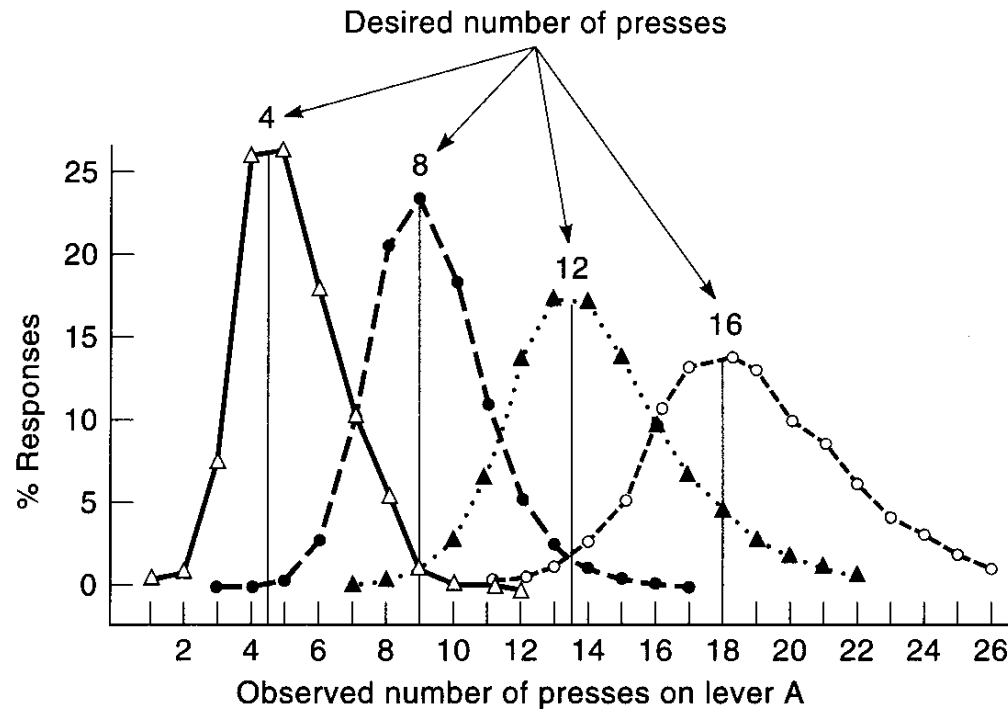


Source: Wikipedia (public domain photo).

Arguments against number representations in animals: what good is number?

- foraging? (continuous amount, not number)
- keeping track of offspring? (individual recognition, not number)

Large number representations in non-human animals: Evidence from rats (Mechner expts.)



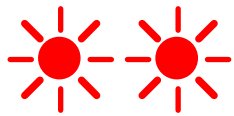
Courtesy of The Society for the Experimental Analysis of Behavior.
Used with permission. (c) 1958 The Society for the Experimental
Analysis of Behavior.

Rats represent the approximate number of presses.
Their representation of number accords with Weber's Law.

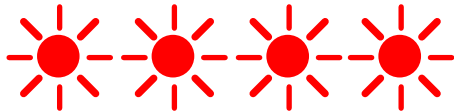
Church & Meck: abstract number in rats

Training phase:

If 2 lights or 2 sounds press "2" lever



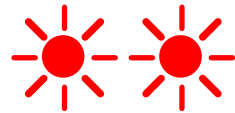
If 4 lights or 4 sounds press "4" lever



Church & Meck: abstract number in rats

Testing phase:

Present 2 lights AND 2 sounds



*Rats press the “4” lever: spontaneous
abstraction across modalities!*

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- ✓ • The representations enter into arithmetic computations (addition).

But: the people in these studies have spent years learning and using formal arithmetic. Do these abilities exist in infants? Animals? YES!

They are part of our basic cognitive machinery.

I. Understanding approximate number

Adults

Infants

Animals

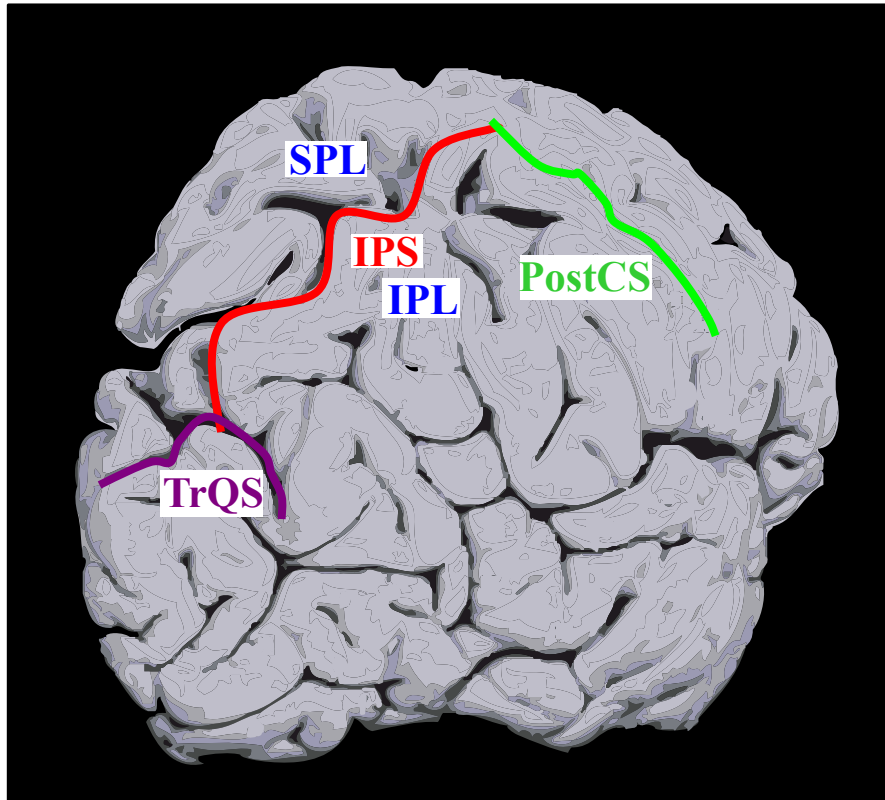
II. Brain basis of number:

neuropsychological patients

fMRI: understanding approximate number

HUMAN PARIETAL CORTEX

Neuroanatomy



Intraparietal sulcus
(IPS)

divides superior (SPL)
and inferior (IPL)
parietal lobules

Figure by MIT OpenCourseWare.

Neuropsychological Studies

- Lemer, Dehaene, Spelke, Cohen (2003):
 - One “acalculic” patient :
 - Left parietal lobe damage
 - Bad at approximation
 - More impaired on subtraction than multiplication
 - Another “acalculic” patient :
 - left temporal
 - Intact approximation
 - More impaired at multiplication than subtraction

•Taken together, these two patients are a.....???

fMRI: Comparing “Approximate Vs. Exact” calculation (Dehaene et al, 1999)

- Addition of Arabic Numerals

- Two versions:

$8 + 9$	$12 \square 16$	Approximate
---------	-----------------	-------------

$9 + 5$	$14 \square 16$	Exact
---------	-----------------	-------

- One control task:

$A + H$	$A \square D$	Letters
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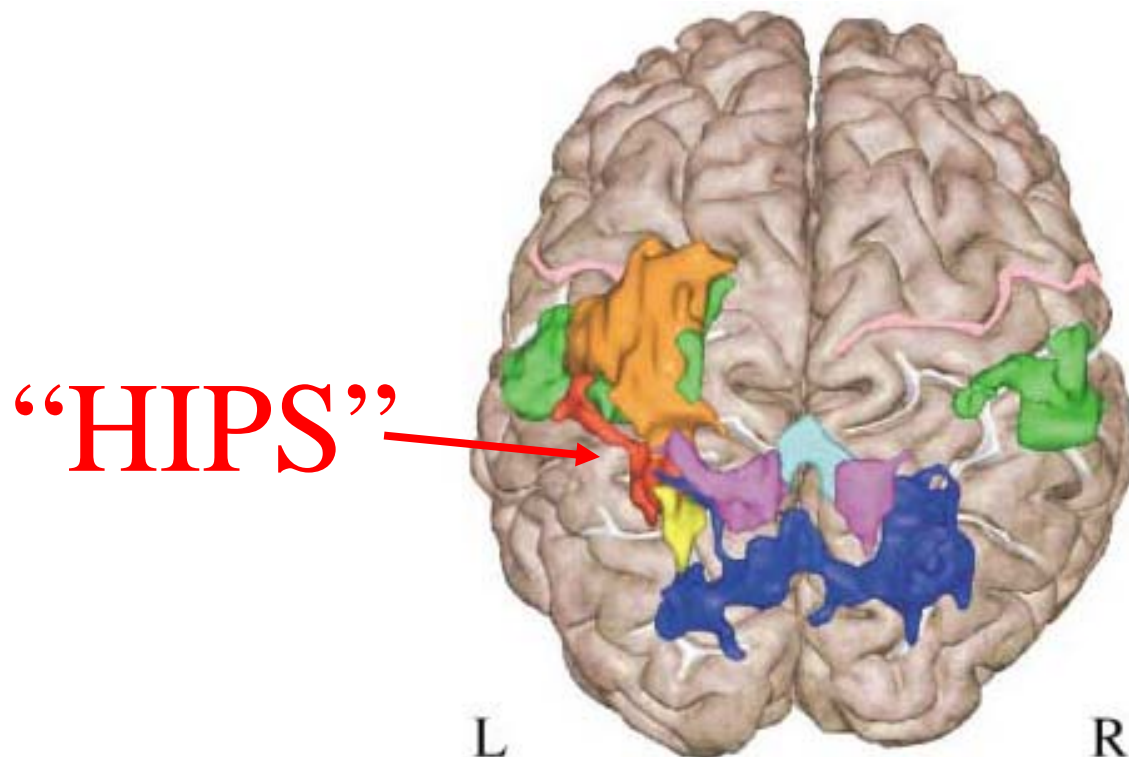
Image removed due to copyright restrictions.

Two MRI images from Fig. 3 in Dehaene, S., et al. "Sources of Mathematical Thinking: Behavioral and Brain-Imaging Evidence." *Science* 284, no. 5416 (1999): 970-974.

Dehaene-Spelke Results

- Approximate > exact activations (in yellow) in the intraparietal sulci, extending anteriorly to the depth of the postcentral sulcus and laterally into the inferior parietal lobule

Simon, Mangin, Cohen, Le Bihan & Dehaene, *Neuron*, 2002



“HIPS”

Claim: this parietal region is the approximate number system that has been characterized behaviorally.

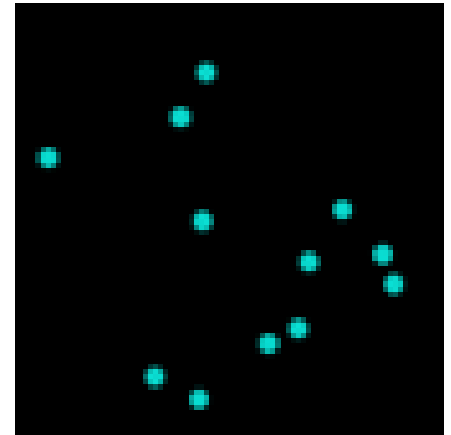
But only tested with symbolic number.

- | | | | |
|---------------|---------------------|------------------------------------|----------------|
| Grasping only | Saccades only | Calculation only | Attention only |
| Manual tasks | Visuo-spatial tasks | Calculation, Saccades and Language | |

Shuman & Kanwisher (2004)

- Are these parietal regions engaged in processing abstract numerical magnitude?

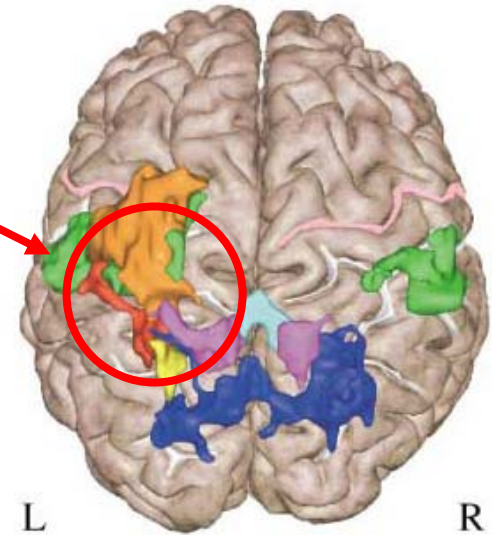
– Test using *non-symbolic* number:



- Are these parietal regions *selectively* engaged in processing numerical magnitude?

Design

- fMRI using 2 methods:
 - Task Manipulation
 - Adaptation
- ROI method: Look in “HIPS”



–Mean Coordinates from Meta-Analysis

–Individual, Functionally Defined ROIs

using Dehaene’s letter approximation task as a localizer

Localizer task: Dehaene et al, 1999, *Science*

$$8 + 9$$

$$12 \square 16$$

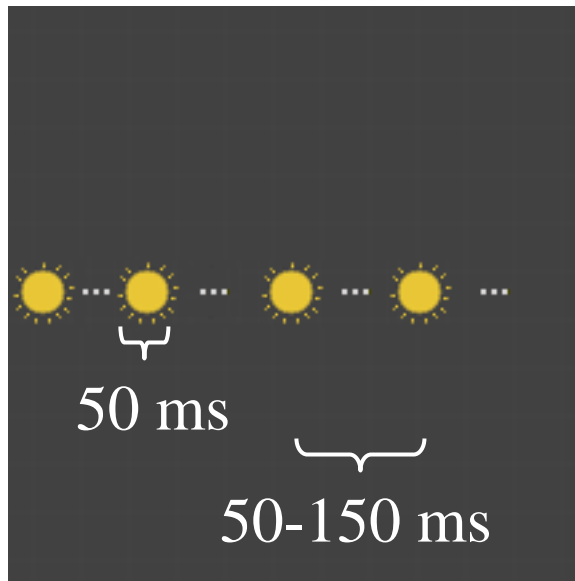
Approximate Addition

$$A + H$$

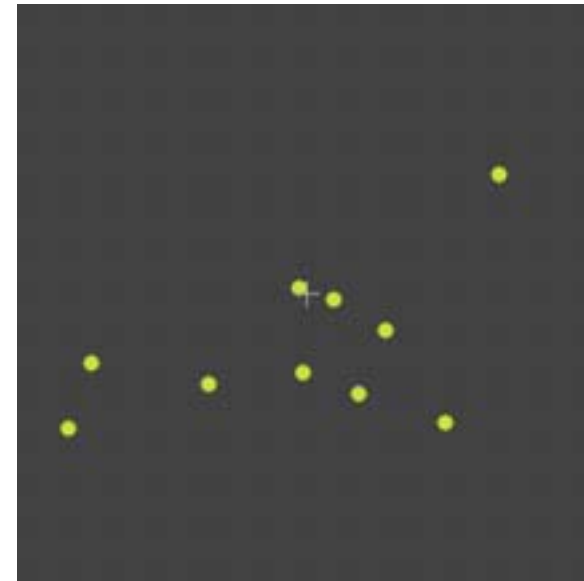
$$A \square D$$

Letter Comparison

Experiment 1: Task Manipulation



4000 ms Sequence + Fixation



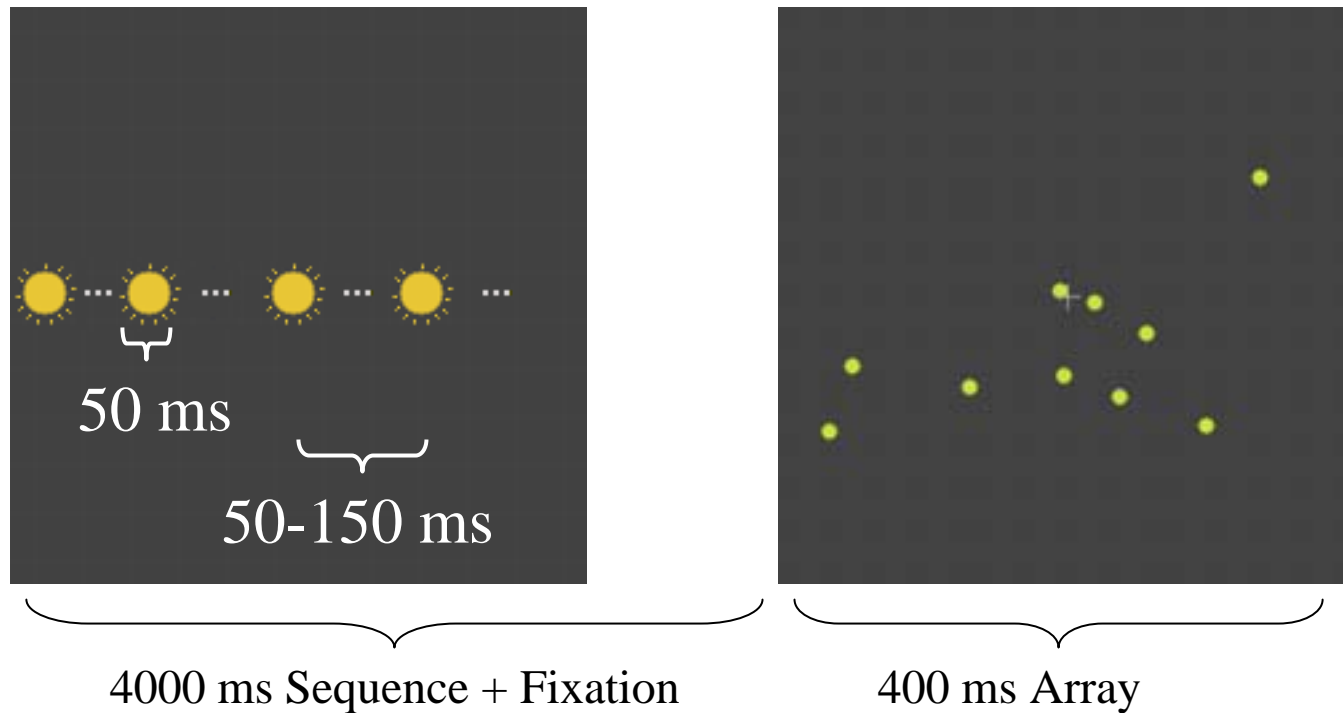
400 ms Array

Number:
More Flashes or Dots?

OR

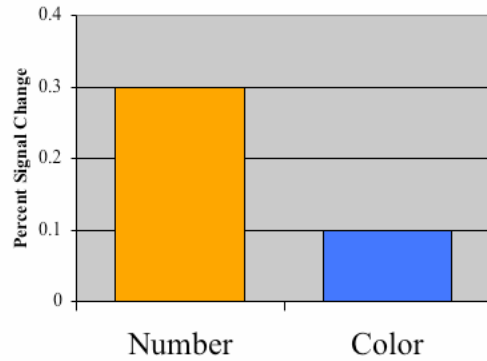
Color:
Same or different?

Experiment 1: Task Manipulation

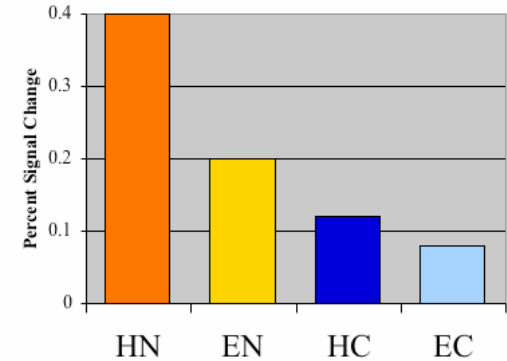


2 x 2 Design:
Difficulty (Hard / Easy) x Task (Number / Color)

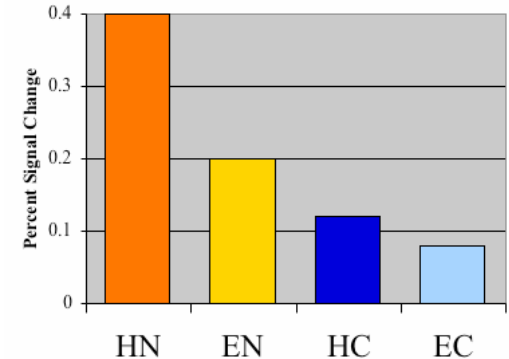
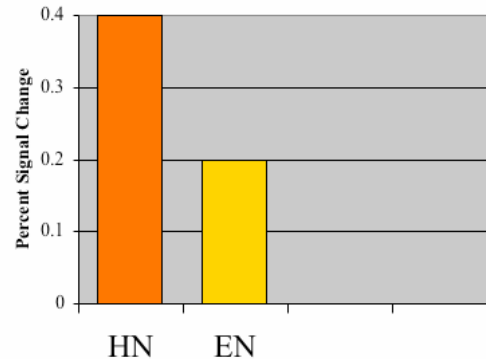
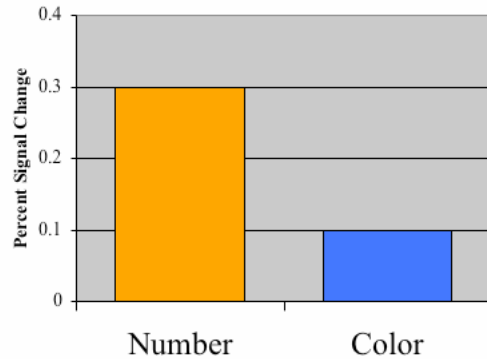
Predictions for a “number” region:



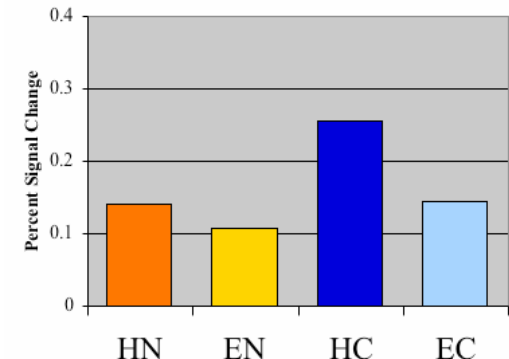
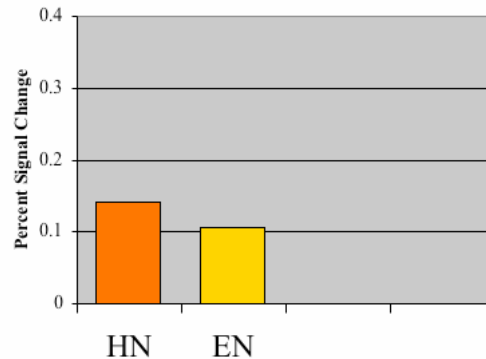
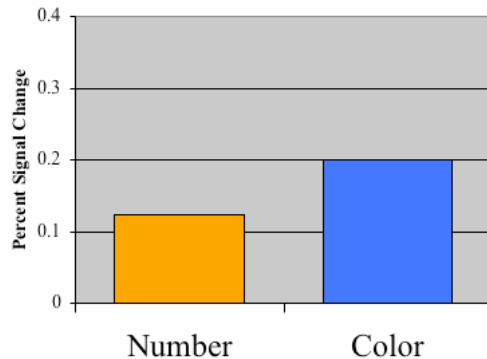
and



Predictions for a “number” region: :



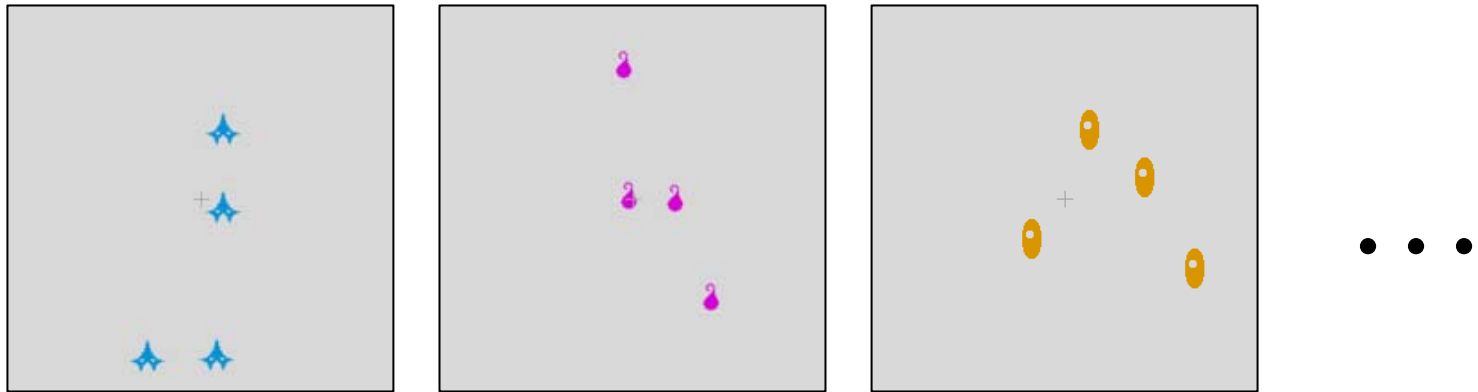
Results in HIPS:



Doesn't look like a number region.

Experiment 2: fMRI Adaptation

Experiment 2: fMRI Adaptation

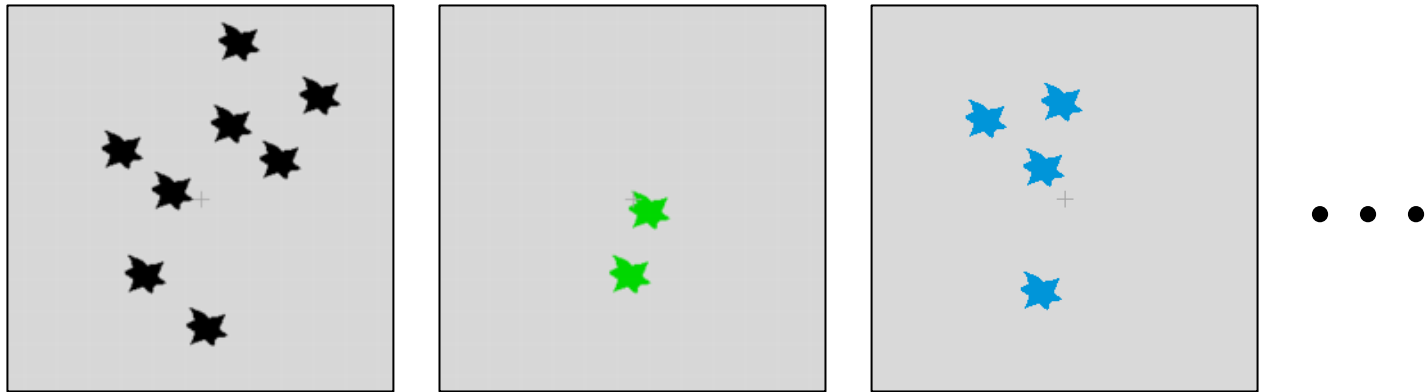


Sequence of 16 different shape arrays

Blocked; task = Passive viewing or color '1-back'

	Shape Const	Shape Varies
Number Const		
Numb. Varies		

Experiment 2: fMRI Adaptation

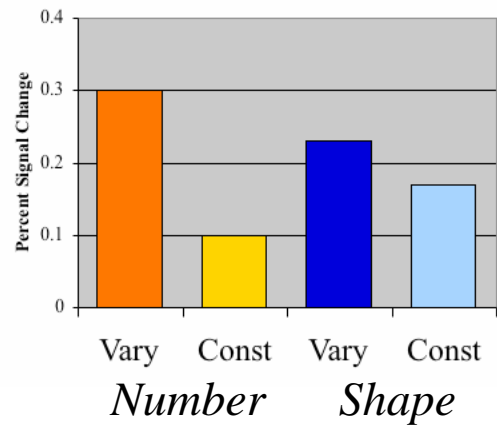
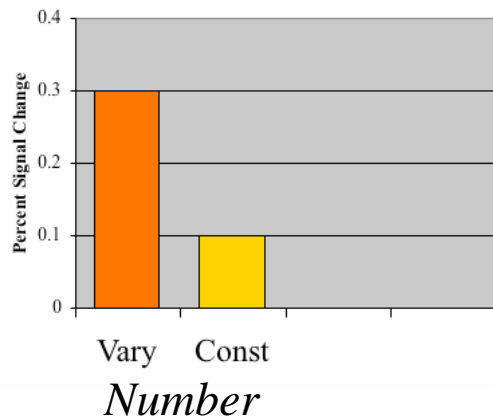


Sequence of 16 different shape arrays

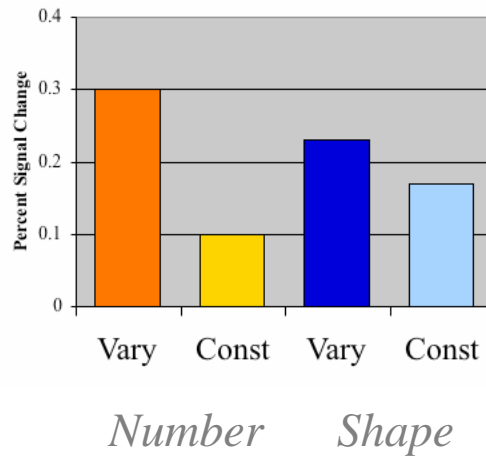
	Shape Const	Shape Varies
Number Const		
Numb. Varies		

Passive viewing or color '1-back'

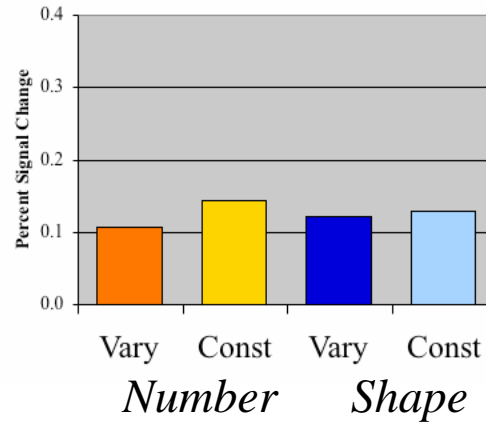
Predictions:



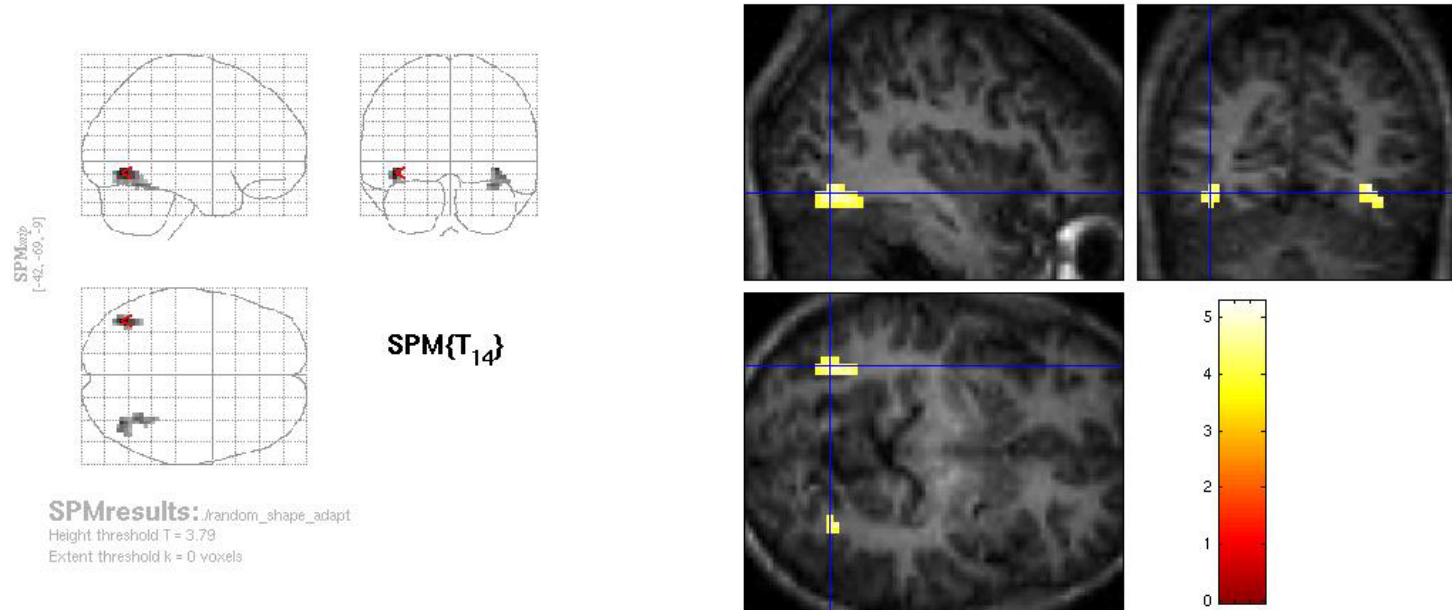
Predictions:



Results in HIPS:



Shape Adaptation in LO

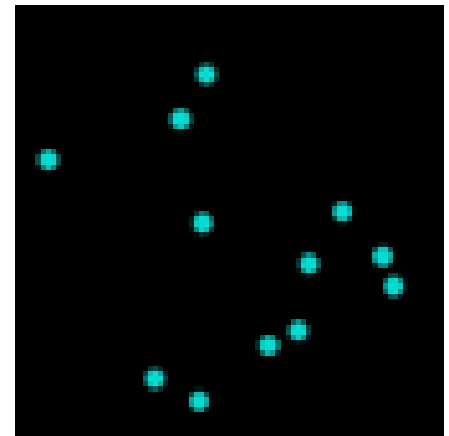


Courtesy of Susan Whitfield-Gabrieli. Used with permission.

Shuman & Kanwisher (2004)

- Are these parietal regions engaged in processing abstract numerical magnitude?

– Test using *non-symbolic* number:



- Are these parietal regions *selectively* engaged in processing numerical magnitude?

No evidence in our data for parietal regions selectively engaged in processing number. But this debate goes on.....

Understanding Number: What is the evidence for these Claims?

- “animals, young infants, and adult humans possess a biologically determined, domain-specific representation of number”
- “a specific neural substrate, located in the left and right intraparietal area, is associated with knowledge of numbers and their relations (‘number sense’). The number domain is a prime example where strong evidence points to an evolutionary endowment of abstract domain-specific knowledge in the brain because there are parallels between number processing in animals and humans.”

–Dehaene, Dehaene-Lambertz & Cohen, TINS, 1998