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### 12.002 Physics and Chemistry of the Earth and Terrestrial Planets

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## Planets

## Overview

Terrestrial planets: Earth, Mars, Moon, Mercury, Venus
Bulk gross products have regular features, but the Moon does not fit the other trends origin different?

Each of these objects except for Venus have timescales
Earth: originally based fossils, now radiometric dating
Moon: radiometric dating of returned samples and crater counting
Venus - not enough craters to do crater counting: young (half a billion years old surface)..so no time scale.

Uncompressed density - density of a planet if all material was at zero pressure
I/MR ${ }^{2}$--> normalized moment of inertia - very important to measure. Relates to the mass distribution inside the planet
$I=\int_{v} \rho r_{0}^{2} d v$
$r$ is cylindrical distance, defined with respect to an axis (not a point). Usually use rotation axis.

Moment of Inertia of a disk of radius y , and thickness dz

$$
\begin{aligned}
\mathrm{I}_{d i s k} & =\int \rho y^{\prime 2} d v \quad d v=2 \pi y^{\prime} d z d y^{\prime} \\
& =\int 2 \pi \rho y^{\prime 2} y^{\prime} d z d y^{\prime} \\
& =2 \pi \rho d z \int_{0}^{y} y^{\prime 3} d y^{\prime} \quad \rho=\frac{m}{v} \\
& =\frac{1}{2} \pi \rho y^{4} d z \\
& \begin{aligned}
I_{\text {sphere }} & =\int_{-R}^{R} I_{d i s k} d z \\
& =\int_{-R}^{R} \frac{1}{2} \pi \rho y^{4} d z \\
& =\frac{1}{2} \pi \rho \int_{-R}^{R}\left(R^{2}-z^{2}\right)^{2} d z \\
& =\frac{8}{15} \pi \rho R^{5} \\
\text { Using } \rho & =\frac{m}{v}=\frac{m}{\frac{4}{3} \pi R^{3}} \quad \text { this becomes } \\
I_{\text {sphere }} & =\frac{2}{5} m R^{2} \quad \text { for a sphere of uniform density. }
\end{aligned}
\end{aligned}
$$



Figure by MIT OpenCourseWare.

For a centrally condensed body, $\mathrm{I}<2 / 5 \mathrm{MR}^{2}$


Figure by MIT OpenCourseWare.

For a hollow body $\mathrm{I}>2 / 5 \mathrm{MR}^{2}$
To get I, measure procession rate of spin pole

## Density and Composition of Planets

The planets have different densities, and different mass distributions...
-can we understand these from first principles?
-why are there differences? (if everything is made of Cl chondrites)
Two possibilities:

1. Different initial compositions (all planets are not made of Cl chondrites) (Urey, Lewis)
2. All have the same initial composition (Cl chondrites) but divergent evolution (Ringwood)

Lewis - showed how gross compositions (densities) of the terrestrial planets (giant planets as well) can be explained at least partly by where they formed in the solar nebula (which determined the temperatures of the condensing materials which they ultimately accreted, which determines abundance of elements)

Lewis predictions:

1. Mercury should be Fe-metal rich, FeO poor, and H 20 poor (low FeO/Fe)
2. Mars should have high $\mathrm{FeO} / \mathrm{Fe}$. Mars should be relativel enriched in volatiles (like oxygen and water...minerals enriched in OH )
3. Earth and Venus should be in the middle - the Earth should be a little more dense that Venus due to iron sulfide condensation -- Moon as well

|  | Fe Wt\% | Uncompressed Density <br> $\left(\mathbf{g} / \mathbf{c m}^{\mathbf{3}} \mathbf{)}\right.$ | $\mathbf{I} / \mathbf{M R}^{\mathbf{2}}$ | $\mathbf{H}_{\mathbf{2}} \mathbf{O}$ Rich? |
| :--- | :--- | :--- | :--- | :--- |
|  |  |  |  |  |
| Mercury | 3 | 5.3 | 0.33 | low |
| Venus | 8 | 4.0 | 0.33 | low |
| Earth | 8 | 4.05 | 0.33 | high |
| Mars | 18 | 3.74 | 0.37 | $? ? ?$ |
| Moon | 5 to 10 | 3.33 | 0.39 | low |

Only Moon does not fit Lewis' predictions well.
Wetherill - condensation of planet modeling
Accreted material from a large range of heliocentric distance

