

## MASSACHUSETTS INSTITUTE OF TECHNOLOGY

### 6.824 Spring 2005 <br> Second Exam

Answers


The average is 62 . The standard deviation is 16 .

## I Part One

1. [10 points]: Why does Frangipani distinguish between read locks and write locks? Why is that a better approach than having a single kind of lock?

The read locks allow multiple Frangipani servers to cache and use files and directories at the same time. This concurrency will increase total performance for read-intensive workloads.
2. [15 points]: Look at the pseudo-code in Section 3.1 of the Ivy paper (Li and Hudak's Memory Coherence in Shared Virtual Memory Systems). Observe this code at the end of the Write Server:

```
IF I am manager THEN BEGIN
    lock(info[p].lock);
    invalidate(p, info[p].copy_set);
```

Suppose that the programmer implementing this code accidentally swaps the lock and invalidate, so that the implementation looked like this:

```
IF I am manager THEN BEGIN
    invalidate(p, info[p].copy_set);
    lock(info[p].lock);
```

Explain a specific situation in which this erroneous code would cause Ivy to produce incorrect memory contents.
Host H 1 takes a write fault on a page, asks the manager for write access, and the manager executes the invalidate but has not yet locked. Host H 2 takes a read fault on the same page, and completes the entire read process, which involves the manager adding $\mathbf{H} 2$ to copy set. Now the manager gets the lock on behalf of H1's write, clears copy set, and gives ownership of the page to H 1 . Now H1 can write the page, which will result in H 2 having a stale copy of the page.

## II Paxos

The Reliable Computing Corporation ( RCC ) has designed a fault-tolerant airline seat reservation service. Travel agents send reservation requests to the service over the Internet, and the service responds with either a seat reservation or an error indication. Obviously it is vital that the service not assign the same seat to two different passengers.

RCC's system achieves fault-tolerance by replicating the reservation state on three servers. The state consists of a list of the reservation requests that have been granted, in the order that they were granted. Each entry in the list contains the seat number, the passenger name, and a request ID included by the travel agent in each request message. The request ID allows the service to recognize retransmitted requests, and reply with the information from the record that's already in the list, rather than incorrectly allocating a new seat. A server can tell which seats have already been reserved by scanning the reservation list.

RCC uses a replicated state machine to ensure that the servers have identical reservation lists. The three servers use Paxos (see the notes for Lecture 15) to agree on each new reservation to be added to the list. They execute Paxos for each reservation (rather than just using Paxos to agree on a new view and primary after each server failure). Each value that the servers agree on looks like "reservation list entry number 37 assigns seat 32 to passenger Robert Morris with request ID 997." When a server receives a request from a travel agent, it scans its reservation list to find the next available seat and the next list entry number, and uses Paxos to propose the value for that list entry number. The system runs a separate instance of Paxos to agree on the value for each numbered list entry.

The three servers are S1, S2, and S3. S1 receives a request from a travel agent asking for a seat for Aaron Burr. S1 picks Paxos proposal number 101 (this is the n in Lecture 15). At about the same time S 2 receives a request asking for a seat for Alexander Hamilton. S2 picks Paxos proposal number 102. Both servers look at their reservation lists and see that the next entry number is 38 , and that the next seat available is seat 33 . Both servers start executing Paxos as a leader for reservation list entry number 38.

Each of the three sequences below indicates the initial sequence of messages of a possible execution of Paxos when both S 1 and S 2 are acting as leader. Each message shown is received successfully. The messages are sent and received one by one in the indicated order. No other messages are sent until after the last message shown is received. Your job is to answer these questions about the final outcomes that could result from each of the initial sequences: Is it possible for the servers to agree on Aaron Burr in seat 33 as entry 38? Is it possible for them to agree on Alexander Hamilton in seat 33 as entry 38? For each of these two outcomes, how it could occur or how does Paxos prevent it from occurring?

```
S1 -> S1 PREPARE (101)
    S1 -> S1 RESPONSE(nil, nil)
S1 -> S2 PREPARE (101)
    S2 -> S1 RESPONSE(nil, nil)
S1 -> S3 PREPARE (101)
    S3 -> S1 RESPONSE (nil, nil)
S2 -> S1 PREPARE (102)
S2 -> S2 PREPARE (102)
S2 -> S3 PREPARE (102)
... the rest of the Paxos messages.
```

3. [5 points]: Answers: Only Alexander Hamilton, because S2's PREPARE will cause all servers to ignore S1's subsequent ACCEPT.
```
S1 -> S1 PREPARE (101)
    S1 -> S1 RESPONSE(nil, nil)
S1 -> S2 PREPARE (101)
    S2 -> S1 RESPONSE(nil, nil)
S1 -> S3 PREPARE (101)
    S3 -> S1 RESPONSE(nil, nil)
S1 -> S3 ACCEPT(101, '`Aaaron Burr...'')
S2 -> S1 PREPARE (102)
S2 -> S2 PREPARE (102)
S2 -> S3 PREPARE (102)
... the rest of the Paxos messages.
```

4. [ 5 points]: Answers: Either Aaron Burr or Alexander Hamilton. If S2 hears a RESPONSE from S3, S2 will propose Aaron Burr. If S2 does not hear a RESPONSE from S3, S2 will propose Alexander Hamilton.
```
S1 -> S1 PREPARE (101)
    S1 -> S1 RESPONSE(nil, nil)
S1 -> S2 PREPARE (101)
    S2 -> S1 RESPONSE(nil, nil)
S1 -> S3 PREPARE (101)
    S3 -> S1 RESPONSE(nil, nil)
S1 -> S3 ACCEPT(101, '`Aaaron Burr...'')
S1 -> S1 ACCEPT(101, '`Aaaron Burr...'')
S2 -> S1 PREPARE (102)
S2 -> S2 PREPARE (102)
S2 -> S3 PREPARE (102)
... the rest of the Paxos messages.
```

5. [5 points]: Answers: Only Aaron Burr. Any majority of RESPONSEs that $\mathbf{S} 2$ hears in Phase 2 will include the value Aaron Burr, so S2 will propose Aaron Burr.
6. [10 points]: Suppose one of the RCC servers has received an ACCEPT for a particular instance of Paxos (i.e. for a particular reservation list entry), but never received any indication about what the final outcome of the Paxos protocol was. Outline what steps the server should take to figure out whether agreement was reached and to find out the agreed-on value. Explain why your procedure is correct even if there are still active leaders executing this instance of Paxos.
The server should send messages to all the servers asking them whether they accepted an ACCEPT message. If a majority of them respond with the same value, then agreement has been reached. This procedure is safe even if there are still active leaders because any such leader must hear from someone from that majority in Phase 2. (It's actually more complex than this; a real argument would include an inductive proof that there cannot be a minority value with higher $n$ number.)

## III FAB

7. [15 points]: Suppose that a FAB system has three bricks, $b_{1}, b_{2}$, and $b_{3}$. There is just one seggroup, and it contains all three bricks. FAB is using replication, as detailed in Figure 4 of the FAB paper. Block $x$ starts out containing value 100 (all replicas have value 100, and all replicas have ordTs equal to valTs). Coordinator $c_{1}$ starts to execute write(200) for block $x$, but crashes after it sends the Write message to $b_{1}$ and before it sends Writes to the other two bricks. $b_{1}$ receives and processes the Write. This is the only execution of the write() function by any coordinator. Then coordinator $c_{2}$ performs two read()s for block $x$, the second starting after the first completes, and prints the resulting pair of values. For each pair below, indicate whether that pair is possible, and explain how it could arise or how FAB prevents that pair of read values from occurring.

100 100: Yes. The first read apparently didn't hear from $b_{1}$, but it would have seen that ordTs and valTs were not equal, repaired $b_{2}$ and $b_{3}$, and the repaired valTs would be greater than the valTs on $b_{1}$. Thus the second read would prefer the repaired $\mathbf{1 0 0}$ even if the second read heard from $b_{1}$.

100 200: No. In order for the first read to return 100, it must have performed a repair. The repair would have guaranteed that the second read returned 200.

200 100: No, for reasons similar to the previous question.
200 200: Yes. The first read must have heard an Order reply from $b_{1}$ and repaired to 200.
8. [10 points]: You're the system administrator of a FAB with three replicated bricks. Your users use the FAB at all times to read and write data. You accidentally step on the Ethernet cable of one of the bricks, which permanently damages the cable and causes the brick to lose its network connection. It will take you about fifteen minutes to run out to CompUSA and buy a replacement Ethernet cable. Before you leave for CompUSA, you can either start a reconfiguration (as in Section 5) or not start a reconfiguration. Which is the best plan? Explain your reasoning. If you would need more information to answer, explain what that information is and how you would use it to decide.
If you don't reconfigure, the system will keep serving reads and writes even with the missing server, since only a quorum is required. The two live servers will keep timestamps for each written block in NVRAM, so that after the Ethernet cable is repaired it will be clear that the repaired server's data is out of date.
If you reconfigure, then when you repair the Ethernet cable you'll have to reconfigure again (to get back up to three replicas), and the second reconfigure will require a copy of the entire disk to the repaired server. This could take a long time. So the only reason to reconfigure is if the two live servers run out of NVRAM in which to store timestamps. Thus the information you need to answer the question is how long it will take for the NVRAM to fill up.

## IV Ruthenian Consistency

You are a member of the Ruthenian People's Popular Front (RPPF), whose aim is to plot the overthrow of the oppressive government of Ruthenia. The RPPF is organized as a large number of "cells," each cell consisting of three members. Each cell knows the members of a few other cells, but no-one knows all the members. However, everyone knows how many cells there are, and each cell knows its own unique ID (a number between 1 and the total number of cells). The total number of cells is constant. The cell structure is intended to make it hard for the government to arrest the whole RPPF, even if they have arrested a few of its members.

From time to time various RPPF cells generate instructions that they want to communicate to every other cell. Cells that know each other can exchange messages written on slips of paper. Thus a message will need to be forwarded between many cells before every cell has a copy.

The RPPF is worried about cells being confused by deceptive orders of arrival of messages. They are particularly anxious to ensure that cells can recognize situations in which two messages are originated simultaneously, by cells that were not aware of the other message. The reason is as follows. Suppose cell c 0 receives two messages m 1 and m 2 that are originated by different cells, and that m 1 and m 2 contain conflicting instructions. If the originator of m 2 knew about m 1 before it generated m 2 , then c 0 should ignore m 1 and pay attention to m 2 . But if m 1 and m 2 were generated without knowledge of each other, then c 0 will know that it should exercise extraordinary care when interpreting the two sets of instructions.

More formally, the RPPF wants every cell be able to decide the relative order in which any pair of messages was originated. Suppose cell c 0 has a copy of message m 1 originated by cell c 1 , and m 2 originated by c 2 . Cell c0 should be able to decide whether c 2 had a copy of m 1 when it originated m 2 , or c 1 had a copy of m 2 when it originated m 1 , or neither had a copy of the other message. Call these situations " m 2 is after m 1 ," " m 1 is after m 2 ," and " m 1 and m 2 are concurrent."

Your job is to design an ordering system for the RPPF.
Each cell is allowed to keep a copy of each message it sees, and can also maintain any state it can derive from those messages. The only form of communication allowed to a cell is passing written notes to the cells it knows about. Your solution should continue to operate even if the Ruthenian government eliminates a few cells, so it should not depend on any special cells. You can assume that the government is not aware of your communication system.

You should try to minimize the amount of communication required by your system; it would not be good if each message had to include a huge amount of book-keeping information.
9. [25 points]: Please explain how your ordering system works. You should describe the contents of each message, the state that each cell must keep, any communication protocol the cells must adhere to, and the algorithm a cell should use to decide whether one messages is after another or whether two messages are concurrent.
The hard part is deciding whether two messages are concurrent. A simple scheme is for the originating cell to include a complete list of all messages it has received in each message it originates. Then any cell can decide if two messages are concurrent by noticing that neither message's list mentions the other message. This solution requires a lot of communication to carry the lists, and the lists will grow in size as time passes.

If the messages originated by each cell arrive in order at every other cell, a cell can summarize what it has seen by just reporting the highest message number it has seen originated from each other cell. That is, a cell should include a version vector in each message it originates. This scheme requires less communication, but must include a protocol that ensures that each cell sees each other cell's messages in order.

## End of Exam

