# Lexical Semantics 

Regina Barzilay<br>MIT

October, 5766

## Last Time: Vector-Based Similarity <br> Measures



- Euclidian: $|\vec{x}, \vec{y}|=|\vec{x}-\vec{y}|=\sqrt{\sum_{i=1}^{n}\left(x_{i}-y_{i}\right)^{2}}$
- Cosine: $\cos (\vec{x}, \vec{y})=\frac{\vec{x} * \vec{y}}{|\vec{x}||\vec{y}|}=\frac{\sum_{i=1}^{n} x_{i} y_{i}}{\sqrt{\sum_{i=1}^{n} x_{i}^{2}} \sqrt{\sum_{i=1}^{n} y_{i}^{2}}}$


## Last Time: Probabilistic Similarity Measures

(Pointwise) Mutual Information: $I(x ; y)=\log \frac{P(x, y)}{P(x) P(y)}$

- Mutual Information: $I(X ; Y)=E_{p(x, y)} \log \frac{p(X, Y)}{p(X) p(Y)}$



## Example: Computing MI

| $I\left(w_{1}, w_{2}\right)$ | $C\left(w_{1}\right)$ | $C\left(w_{2}\right)$ | $C\left(w_{1}, w_{2}\right)$ | $w_{1}$ | $w_{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 16.31 | 30 | 117 | 20 | Agatha | Christie |
| 15.94 | 77 | 59 | 20 | videocassette | recorder |
| 15.19 | 24 | 320 | 20 | unsalted | butter |
| 1.09 | 14907 | 9017 | 20 | first | made |
| 0.29 | 15019 | 15629 | 20 | time | last |

## Example: Computing MI

| $I\left(w_{1}, w_{2}\right)$ | $C\left(w_{1}\right)$ | $C\left(w_{2}\right)$ | $C\left(w_{1}, w_{2}\right)$ | $w_{1}$ | $w_{2}$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 15.02 | 1 | 19 | 1 | fewest | visits |
| 12.00 | 5 | 31 | 1 | Indonesian | pieces |
| 9.21 | 13 | 82 | 20 | marijuana | growing |

## Last Time: Probabilistic Similarity Measures

Kullback Leibler Distance: $D(p \| q)=\sum p(x) \log \frac{p(x)}{q(x)}$

- Closely related to mutual information

$$
I(X ; Y)=D(p(x, y) \| p(x) p(y))
$$

- Related measure : Jensen-Shannon divergence:

$$
D_{J S(p, q)}=\frac{1}{2} D\left(p \| \frac{p+q}{2}\right)+\frac{1}{2} D\left(q \| \frac{p+q}{2}\right)
$$

## Beyond Pairwise Similarity

- Clustering is "The art of finding groups in data"(Kaufmann and Rousseeu)
- Clustering algorithms divide a data set into homogeneous groups (clusters), based on their similarity under the given representation.



## Hierarchical Clustering

Greedy, bottom-up version:

- Initialization: Create a separate cluster for each object
- Each iteration: Find two most similar clusters and merge them
- Termination: All the objects are in the same cluster


## Agglomerative Clustering

$$
\begin{array}{lllll} 
& \text { E } & \text { D } & \text { C } & \text { B } \\
\text { A } & 0.1 & 0.2 & 0.2 & 0.8 \\
& & & & \\
\text { B } & 0.1 & 0.1 & 0.2 & \\
& & & & \\
\text { C } & 0.0 & 0.7 & & \\
\text { D } & 0.6 & & &
\end{array}
$$

## Agglomerative Clustering

|  | E | D | C | B |
| :--- | :--- | :--- | :--- | :--- |
| A | 0.1 | 0.2 | 0.2 | 0.8 |
| B | 0.1 | 0.1 | 0.2 |  |
| C | 0.0 | 0.7 |  |  |
| D | 0.6 |  |  |  |



## Agglomerative Clustering

|  | E | D | C | B |
| :--- | :--- | :--- | :--- | :--- |
| A | 0.1 | 0.2 | 0.2 | 0.8 |
| B | 0.1 | 0.1 | 0.2 |  |
| C | 0.0 | 0.7 |  |  |
| D | 0.6 |  |  |  |



## Clustering Function

$$
\begin{array}{lllll} 
& \text { E } & \text { D } & \text { C } & \text { B } \\
\text { A } & 0.1 & 0.2 & 0.2 & 0.8 \\
& & & & \\
\text { B } & 0.1 & 0.1 & 0.2 & \\
& & & & \\
\text { C } & 0.0 & 0.7 & & \\
\text { D } & 0.6 & & &
\end{array}
$$



## Clustering Function

$$
\begin{array}{lllll} 
& \text { E } & \text { D } & \text { C } & \text { B } \\
\text { A } & 0.1 & 0.2 & 0.2 & 0.8 \\
& & & & \\
\text { B } & 0.1 & 0.1 & 0.2 & \\
& & & & \\
\text { C } & 0.0 & 0.7 & & \\
\text { D } & 0.6 & & &
\end{array}
$$



## Clustering Function

$$
\begin{array}{lllll} 
& \text { E } & \text { D } & \text { C } & \text { B } \\
\text { A } & 0.1 & 0.2 & 0.2 & 0.8 \\
& & & & \\
\text { B } & 0.1 & 0.1 & 0.2 & \\
& & & & \\
\text { C } & 0.0 & 0.7 & & \\
\text { D } & 0.6 & & &
\end{array}
$$



## Clustering Function

- Single-link: Similarity of two most similar members
- Complete-link: Similarity of two least similar members
- Group-average: Average similarity between members


## Single-Link Clustering



- Achieves Local Coherence
- Complexity $O\left(n^{2}\right)$
- Fails when clusters are not well separated


## Complete-Link Clustering



- Achieves Global Coherence
- Complexity $O\left(n^{2} \log n\right)$
- Fails when clusters aren't spherical, or of uniform size


## K-Means Algorithm: Example

Iterative, hard, flat clustering algorithm based on
Euclidean distance


## K-Means Algorithm

1. Choose $k$ points at random as cluster centers
2. Assign each instance to its closest cluster center
3. Calculate the centroid (mean) for each cluster, use it as a new cluster center
4. Iterate steps 2 and 3 until the cluster centers don't change anymore

## K-Means Algorithm: Hard EM

1. Guess initial parameters
2. Use model to make the best guess of $c_{i}$ (E-step)
3. Use the new complete data to learn better model (M-step)
4. Iterate (2-3) until convergence

## Evaluating Clustering Methods

- Perform task-based evaluation
- Test the resulting clusters intuitively, i.e., inspect them and see if they make sense. Not advisable.
- Have an expert generate clusters manually, and test the automatically generated ones against them.
- Test the clusters against a predefined classification if there is one


## Comparing Clustering Methods

(Meila, 2002)
$n \quad$ total \# of points
$n_{k} \quad$ \# of points in cluster $C_{k}$
K \# of nonempty clusters
$N_{11}$ \# of pairs that are in the same cluster under $C$ and $C^{\prime}$
$N_{00} \quad \#$ of pairs that are in different clusters under $C$ and $C^{\prime}$
$N_{10} \quad \#$ of pairs that are in the same cluster under $C$ but not $C^{\prime}$
$N_{01}$ \# of pairs that are in the same cluster under $C^{\prime}$ but not $C$

## Comparing by Counting Pairs

- Wallace criteria

$$
\begin{aligned}
W_{1}\left(C, C^{\prime}\right) & =\frac{N_{11}}{\sum_{k} n_{k}\left(n_{k}-1\right) / 2} \\
W_{2}\left(C, C^{\prime}\right) & =\frac{N_{11}}{\sum_{k^{\prime}} n_{k^{\prime}}\left(n^{\prime}{ }_{k^{\prime}}-1\right) / 2}
\end{aligned}
$$

- Fowles-Mallows criterion

$$
F\left(C, C^{\prime}\right)=\sqrt{W_{1}\left(C, C^{\prime}\right) W_{2}\left(C, C^{\prime}\right)}
$$

Problems: ?

## Comparing Clustering by Set Matching

Contingency table $M$ is a $K \times K$ matrix, whose $k k^{\prime}$ element is the number of points in the intersection of clusters $C_{k}$ and $C_{k^{\prime}}^{\prime}$

$$
L\left(C, C^{\prime}\right)=\frac{1}{K} \sum_{k} \max _{k^{\prime}} \frac{2 m_{k k^{\prime}}}{n_{k}+n_{k}^{\prime}}
$$

Problems: ?

## Comparing Clustering by Set Matching

## Distributional Syntax

Sequences of word clusters and their contexts (Klein, 2005)

| Tag | Top Context by Frequency |
| :--- | :--- |
| DT | (IN-NN), (IN-JJ), (IN-NNP), (VB-NN) |
| JJ | (DT-NN), (IN-NNS), (IN-NN), (JJ-NN),(DT-NNS) |
| MD | (NN-VB), (PRP-VB), (NNS-VB), (NNP-VB), (WDT-VB) |
| NN | (DT-IN), (JJ-IN), (DT-NN), (NN-IN), (NN-.) |
| VB | (TO-DT), (TO-IN), (MD-DT), (MD-VBN),(TO-JJ) |

## Distributional Syntax

The most similar POS pairs and POS sequence pairs based on $D_{J S}$ of their context

| Rank | Tag pairs | Sequence Pairs |
| :--- | :--- | :--- |
| 1 | (VBZ,VBD) | (NNP NNP, NNP NNP NNP) |
| 2 | (DT,PRP\$) | (DT JJ NN IN, DT NN IN) |
| 3 | (NN,NNS) | (NNP NNP NNP NNP, NNP NNP NNP) |
| 4 | (WDT,WP) | (DT NNP NNP, DT NNP) |
| 5 | (VBG,VBN) | (IN DT JJ NN, IN DT NN) |
| 14 | (JJS, JJR) | (NN IN DT, NN DT) |

## Linear vs. Hierarchical Context

The left (right) context of $x$ is the left(right) sibling of the lowest ancestor of $x$

| Rank | Linear | Hierarchical |
| :--- | :--- | :--- |
| 1 | (NN NNS, JJ NNS) | (NN NNS, JJ NNS) |
| 2 | (IN NN, IN DT NN) | (IN NN, IN DT NN) |
| 3 | (DT JJ NN, DT NN) | (IN DT JJ NN, IN JJ NNS) |
| 4 | (DT JJ NN, DT NN NN) | (VBZ VBN, VBD VBN) |
| 5 | (IN DT JJ NN, IN DT NN) | (NN NNS, JJ NN NNS) |

## Grammar Induction

- Task: Unsupervised learning of a language's syntax from a corpus of observed sentences

The cat stalked the mouse.
The mouse quivered.
The cat smiled.

- A tree induction system is not forced to learn all aspects of language (semantics, discourse)


## Motivation

- Linguistic motivation:
- Empirical argument against the poverty of the stimulus (Chomsky, 1965)
- Empirical investigation of syntax modularity (Fodor, 1983; Jackendoff, 1996)
- Engineering motivation:
- No need in training data


## Evaluation and Baselines

- Evaluation:
- Compare grammars
- Compare trees
- Baselines:
- Random Trees
- Left- and Right-Branching Trees


## Structure Search Experiment

- Structure search
- Add production to context free grammar
- Select HMM topology
- Parameter search
- Determine parameters for a fixed PCFG


## Finding Topology

Stolcke\&Omohundro, 1994: Bayesian model merging

- Data incorporation: Given a body of data $X$, build an initial model $M_{0}$ by explicitly accommodating each data point individually such that $M_{0}$ maximizes the likelihood $P(X \mid M)$.
- Generalization: Build a sequence of new models, obtaining $M_{i+1}$ from $M_{i}$ by applying a merging operator $m$ that coalesces substructures in $M_{i}$, $M_{i+1}=m\left(M_{i}\right), i=0,1$
- Optimization: Maximize posterior probability
- Search strategy: Greedy or beam search through the space of possible merges


## HMM Topology Induction

- Data incorporation: For each observed sample create a unique path between the initial and final states by assigning a new state to each symbol token in the sample
- Generalization: Two HMM states are replaced by a single new state, which inherits the union of the transitions and emissions from the old states.


## HMM Topology Induction

- Prior distribution: Choose uninformative priors for a model M with topology $M_{s}$ and parameters $\theta_{M}$.

$$
\begin{gathered}
P(M)=P\left(M_{s}\right) P\left(\theta_{M} \mid M_{s}\right) \\
P\left(M_{s}\right) \propto \exp \left(-l\left(M_{s}\right)\right)
\end{gathered}
$$

where $l\left(M_{s}\right)$ is the number of bits required to encode $M_{s}$.

- Search: Greedy merging strategy.


## Example



## PCFG Induction

- Data Incorporation: Add a top-level production that covers the sample precisely. Create one nonterminal for each observed terminal.
- Merging and Chunking: During merging, two nonterminals are replaced by a single new state. Chunking takes a given sequence of nonterminals and abbreviates it using a newly created nonterminal.
- Prior distribution: Similar to HMM.
- Search: Beam search.


## Example

Input: \{ab,aabb,aaabbb\}

|  |  |
| :---: | :---: |
| Chunk(AB)-> ${ }^{\text {X }}$ |  |
| Chunk(AXB)->Y | $\begin{aligned} S & \rightarrow X \\ & \rightarrow Y \\ & \rightarrow \text { A Y B } \\ X & \rightarrow \text { A B } \\ Y & \rightarrow \text { A X B } \end{aligned}$ |
| Merge S, Y | $\begin{aligned} & S \xrightarrow{S \rightarrow X} \\ & \quad \text {-> A S B } \\ & \text { X A B } \end{aligned}$ |
| Merge S,X |  |

## Results for PCFGS

- Formal language experiments
- Successfully learned simple grammars

| Language | Sample no. | Grammar | Search |
| :--- | :--- | :--- | :--- |
| Parentheses | 8 | $S \rightarrow()\|(S)\| S S$ | BF |
| $a^{2 n}$ | 5 | $S \rightarrow a a \mid S S$ | BF |
| $(a b)^{n}$ | 5 | $S \rightarrow a b \mid a S b$ | BF |
| $w c w^{R}, w \in\{a, b\}^{\star}$ | 7 | $S \rightarrow c\|a S a\| b S b$ | BS (3) |
| Addition strings | 23 | $S \rightarrow a\|b\|(S) \mid S+S$ | BS(4) |

- Natural Language syntax
- Mixed results (issues related to data sparseness)


## Example of Learned Grammar

| Target Grammar | Learned Grammar |
| :---: | :---: |
| $S \rightarrow N P V P$ | $S \rightarrow N P V P$ |
| $V P \rightarrow V e r b N P$ | $V P \rightarrow V N P$ |
| $N P \rightarrow D e t N o u n$ | $N P \rightarrow D e t N$ |
| $N P \rightarrow D e t N o u n R C$ | $N P \rightarrow N P R C$ |
| $R C \rightarrow$ RelVP | $R C \rightarrow R E L V P$ |
| Verb $\rightarrow$ saw\|heard | $V \rightarrow$ saw\|heard |
| Noun $\rightarrow$ cat $\mid$ dog\|mouse | $N \rightarrow$ cat\|dog|mouse |
| Det $\rightarrow a \mid t h e$ | $D e t \rightarrow a \mid t h e$ |
| $R e l \rightarrow t h a t$ | $R e l \rightarrow t h a t$ |

## Example

Input: \{ab,aabb,aaabbb\}

|  |  |
| :---: | :---: |
| Chunk(AB)-> ${ }^{\text {X }}$ |  |
| Chunk(AXB)->Y | $\begin{aligned} S & \rightarrow X \\ & \rightarrow Y \\ & \rightarrow \text { A Y B } \\ X & \rightarrow \text { A B } \\ Y & \rightarrow \text { A X B } \end{aligned}$ |
| Merge S, Y | $\begin{aligned} & S \xrightarrow{S \rightarrow X} \\ & \quad \text {-> A S B } \\ & \text { X A B } \end{aligned}$ |
| Merge S,X |  |

## Issue with Chunk/Merge Systems

- Hard to recover from initial choices
- Hard to make local decision which will interact with each other (e.g., group verb preposition and preposition-determiner, both wrong and non consistent)
- Good local heuristics often don't have well formed objectives that can be evaluated for the target grammar


## Learn PCFGs with EM

- (Lari\&Young 1990): Learning PCFGs with EM
- Full binary grammar over $n$ symbols
- Parse randomly at first
- Re-estimate rule probabilities of parses
- Repeat


## Grammar Format

- Lari\&Young, 1990: Satisfactory grammar learning requires more nonterminals than are theoretically needed to describe a language at hand
- There is no guarantee that the nonterminals that the algorithm learns will have any resemblance to nonterminals motivated in linguistic analysis
- Constraints on the grammar format may simplify the reestimation procedure
- Carroll\&Charniak, 1992: Specify constraints on non-terminals that may appear together on the right-hand side of the rule


## Partially Unsupervised Learning

Pereira\&Schabes 1992

- Idea: Encourage the probabilities into a good region of the parameter space
- Implementation: modify Inside-Outside algorithm to consider only parses that do not cross provided bracketing
- Experiments: 15 non terminals over 45 POS tags The algorithm uses Treebank bracketing, but ignores the labels
- Evaluation Measure: fraction of nodes in gold trees correctly posited in proposed trees (unlabeled recall)
- Results:
- Constrained and unconstrained grammars have similar cross-entropy
- But very different bracketing accuracy: 37\% vs. $90 \%$


## Current Performance

- Constituency recall:

| Random Baseline | 39.4 |
| :--- | :--- |
| Klein'2005 | 88.0 |
| Supervised PCFG | 92.8 |

- Why it works?
- Combination of simple models
- Representations designed for unsupervised learning

