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HST.583 Functional Magnetic Resonance Imaging: Data Acquisition and Analysis
Fall 2008

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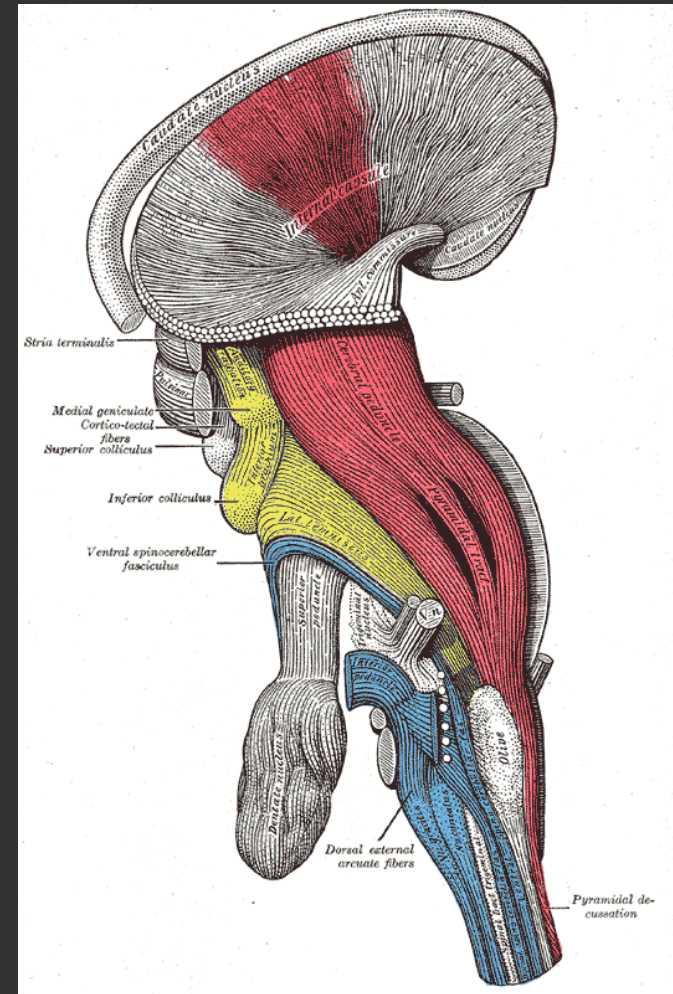
Diffusion weighted imaging

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Why diffusion imaging?

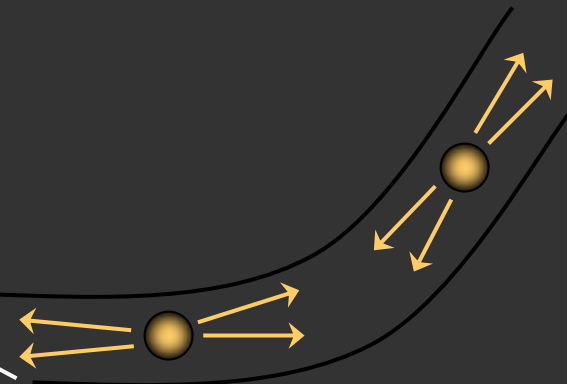
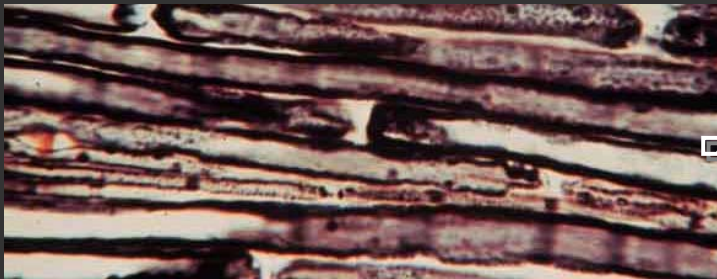
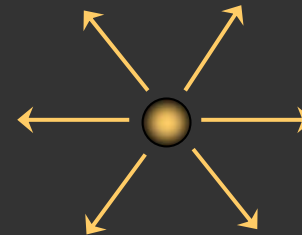
- White matter (WM) is organized in fiber bundles
- Identifying these WM pathways is important for:
 - Inferring connections b/w brain regions
 - Understanding effects of neurodegenerative diseases, stroke, aging, development ...



From Gray's Anatomy: IX. Neurology

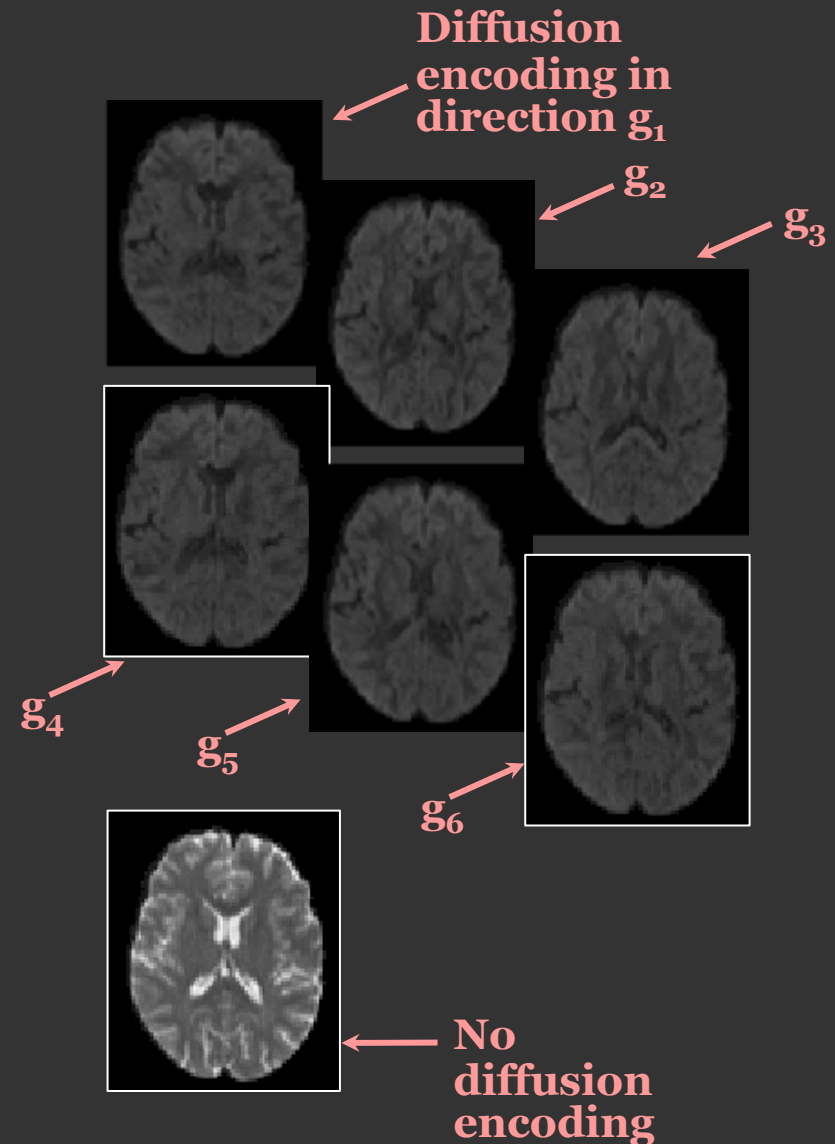
Diffusion in brain tissue

- Differentiate tissues based on the diffusion (random motion) of water molecules within them
- Gray matter: Diffusion is unrestricted \Rightarrow isotropic
- White matter: Diffusion is restricted \Rightarrow anisotropic



Diffusion MRI

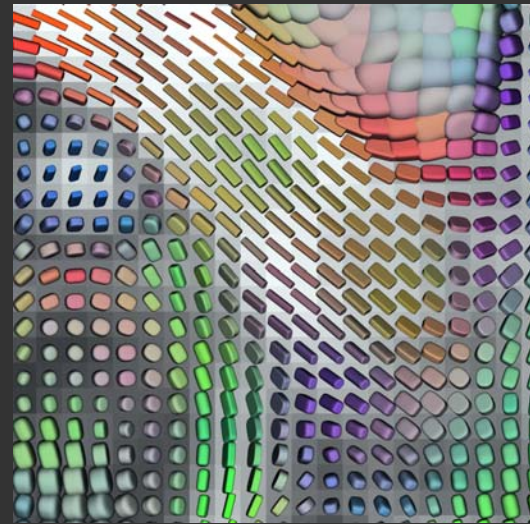
- Magnetic resonance imaging can provide “diffusion encoding”
- Magnetic field strength is varied by gradients in different directions
- Image intensity is attenuated depending on water diffusion in each direction
- Compare with baseline images to infer on diffusion process



Imaging diffusion

- Image the **direction** in which water molecules diffuse at each voxel in the brain
 - ⇒ Infer WM fiber orientation at each voxel
- Clearly, **direction** can't be described by a usual grayscale image

~~Grayscale brain image removed due to copyright restrictions.~~



Courtesy of Gordon Kindlmann. Used with permission.

Tensors

- We express the notion of “direction” mathematically by a **tensor** D
- A tensor is a 3x3 symmetric, positive-definite matrix:

$$D = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{12} & d_{22} & d_{23} \\ d_{13} & d_{23} & d_{33} \end{bmatrix}$$

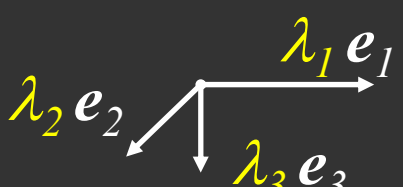
- D is symmetric 3x3 \Rightarrow It has 6 unique elements
- Suffices to estimate the upper (lower) triangular part

Eigenvalues & eigenvectors

- The matrix D is positive-definite \Rightarrow
 - It has 3 real, positive eigenvalues $\lambda_1, \lambda_2, \lambda_3 > 0$.
 - It has 3 orthogonal eigenvectors e_1, e_2, e_3 .

$$D = \lambda_1 e_1 \cdot e_1 + \lambda_2 e_2 \cdot e_2 + \lambda_3 e_3 \cdot e_3$$

eigenvalue eigenvector

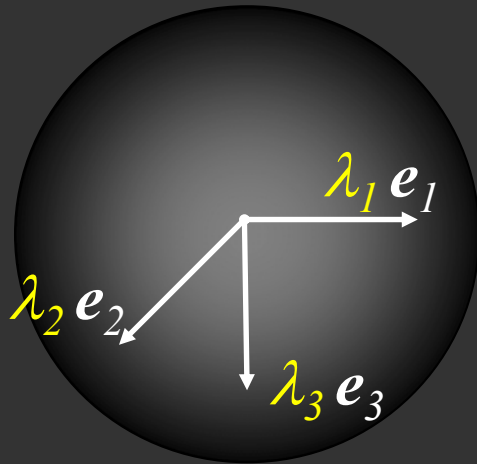
$$e_1 = \begin{bmatrix} e_{1x} \\ e_{1y} \\ e_{1z} \end{bmatrix}$$


Physical interpretation

- Eigenvectors express diffusion direction
- Eigenvalues express diffusion magnitude

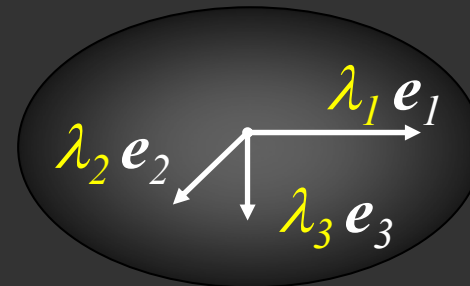
Isotropic diffusion:

$$\lambda_1 \approx \lambda_2 \approx \lambda_3$$



Anisotropic diffusion:

$$\lambda_1 \gg \lambda_2 \approx \lambda_3$$



- One such ellipsoid at each voxel: Likelihood of water molecule displacements at that voxel

Diffusion tensor imaging (DTI)

Image:

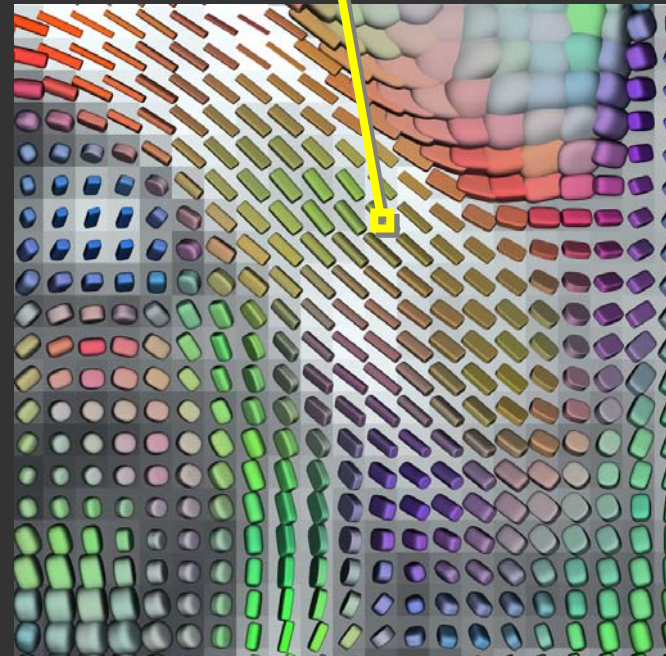
A scalar intensity value f_j at each voxel j



Grayscale brain image removed due to copyright restrictions.

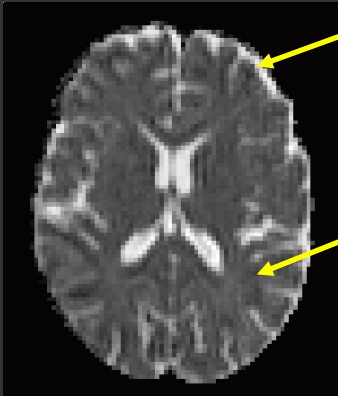
Tensor map:

A tensor D_j at each voxel j



Courtesy of Gordon Kindlmann. Used with permission.

Summary measures

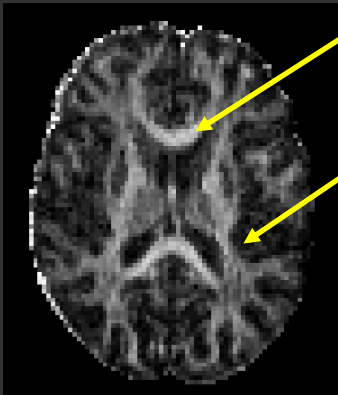


Faster diffusion

Slower diffusion

- Mean diffusivity (MD):
Mean of the 3 eigenvalues

$$MD(j) = [\lambda_1(j) + \lambda_2(j) + \lambda_3(j)]/3$$



Anisotropic diffusion

Isotropic diffusion

- Fractional anisotropy (FA):
Variance of the 3 eigenvalues,
normalized so that $0 \leq (FA) \leq 1$

$$FA(j)^2 = \frac{3}{2} \frac{[\lambda_1(j) - MD(j)]^2 + [\lambda_2(j) - MD(j)]^2 + [\lambda_3(j) - MD(j)]^2}{\lambda_1(j)^2 + \lambda_2(j)^2 + \lambda_3(j)^2}$$

More summary measures

- **Axial diffusivity: Greatest eigenvalue**

$$AD(j) = \lambda_1(j)$$

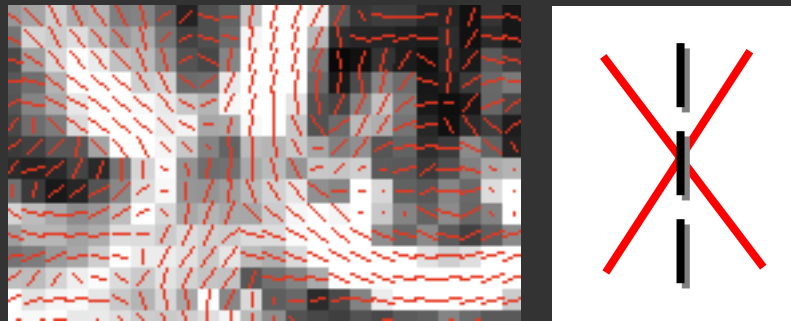
- **Radial diffusivity: Average of 2 lesser eigenvalues**

$$RD(j) = [\lambda_2(j) + \lambda_3(j)]/2$$

- **Inter-voxel coherence: Average angle b/w the major eigenvector at some voxel and the major eigenvector at the voxels around it**

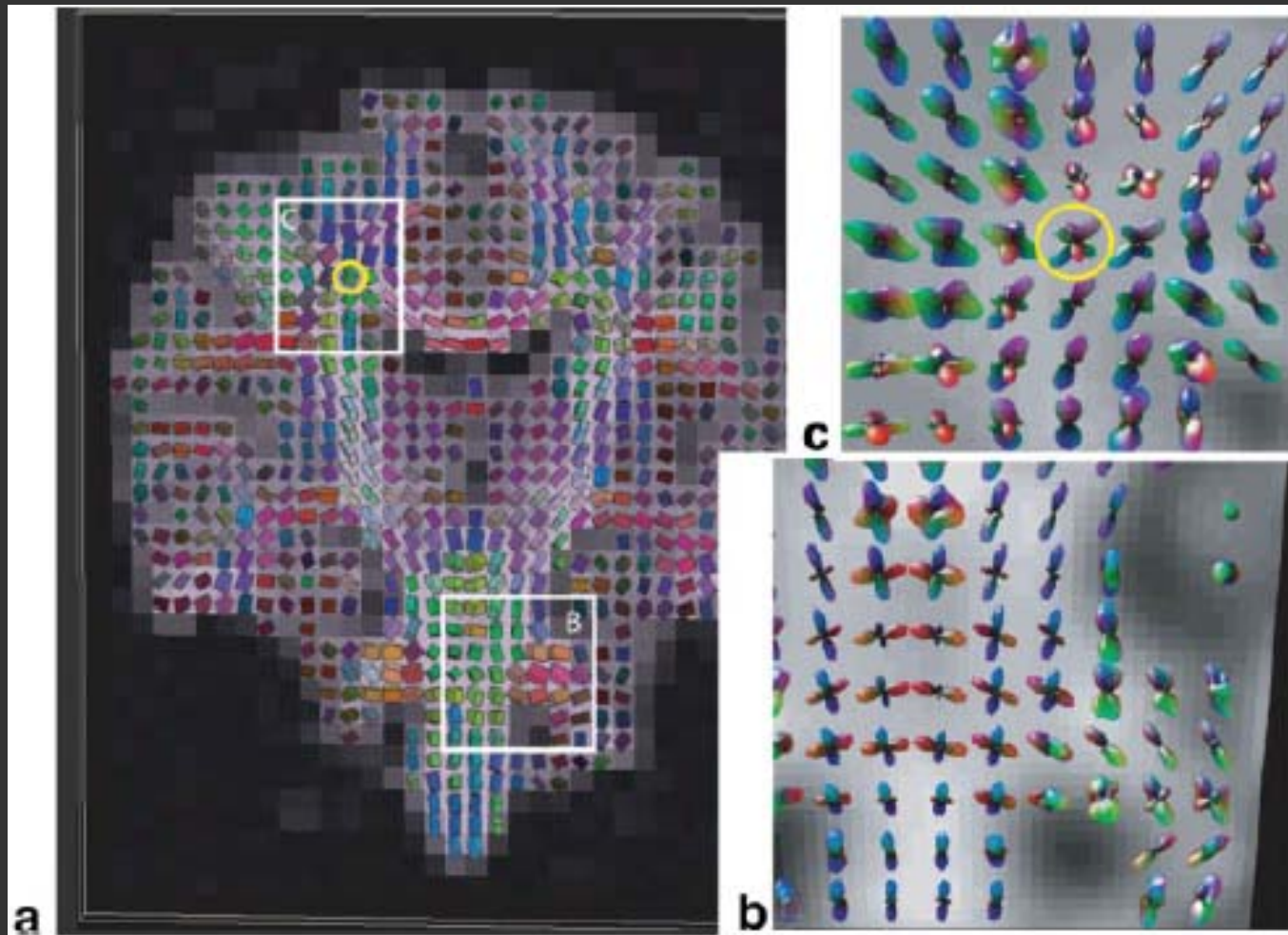
Other models of diffusion

- The tensor is an imperfect model: What if more than one major diffusion direction in the same voxel?



- High angular resolution diffusion imaging (HARDI)
 - A mixture of the usual (“rank-2”) tensors [Tuch’02]
 - A tensor of rank > 2 [Frank’02, Özarslan’03]
 - An orientation distribution function [Tuch’04]
 - A diffusion spectrum (DSI) [Wedeen’05]
- More parameters at each voxel \Rightarrow More data needed

Example: DTI vs. DSI

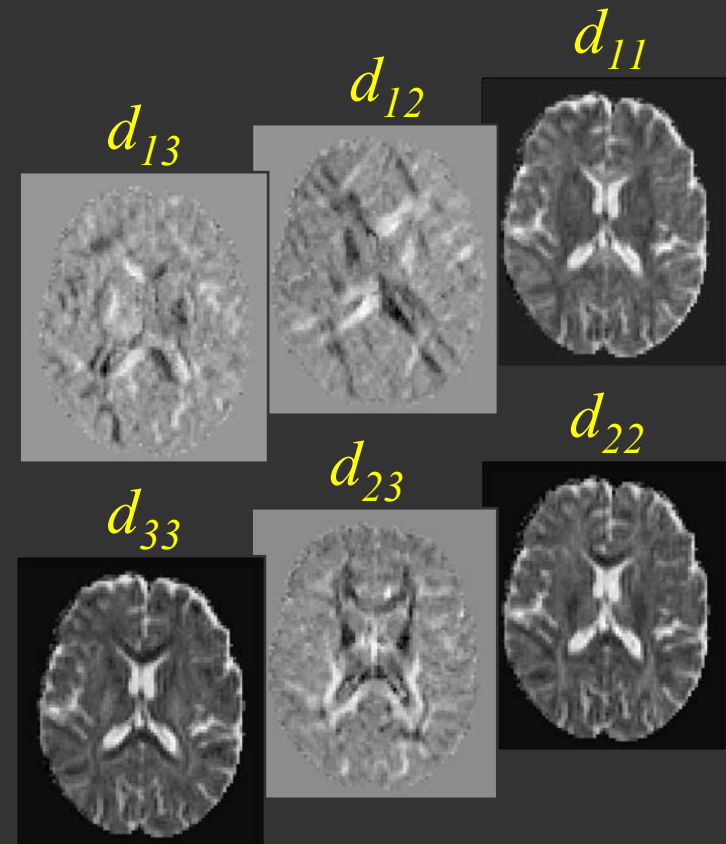


Source: Wedeen, V. J. *et al.*, "Mapping complex tissue architecture with diffusion spectrum magnetic resonance imaging." *MRM* 54, no. 6 (2005): 1377-1386. Copyright (c) 2005 Wiley-Liss, Inc., a subsidiary of John Wiley & Sons, Inc. Reprinted with permission of John Wiley & Sons., Inc.

Back to the tensor

- Remember: A tensor has six unique values

$$D = \begin{bmatrix} d_{11} & d_{12} & d_{13} \\ d_{12} & d_{22} & d_{23} \\ d_{13} & d_{23} & d_{33} \end{bmatrix}$$



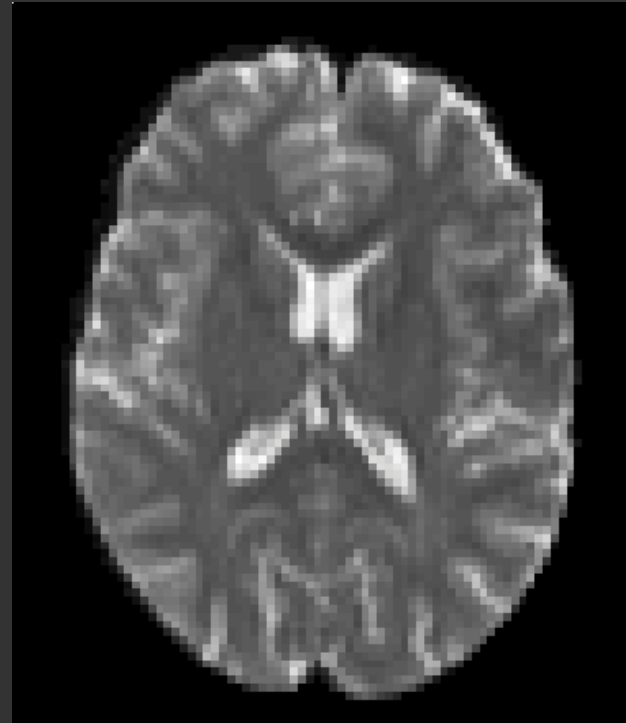
- Must estimate six times as many values at each voxel
⇒ Must collect (at least) six times as much data!

MR data acquisition

Measure **raw MR signal**
(frequency-domain samples
of transverse magnetization)



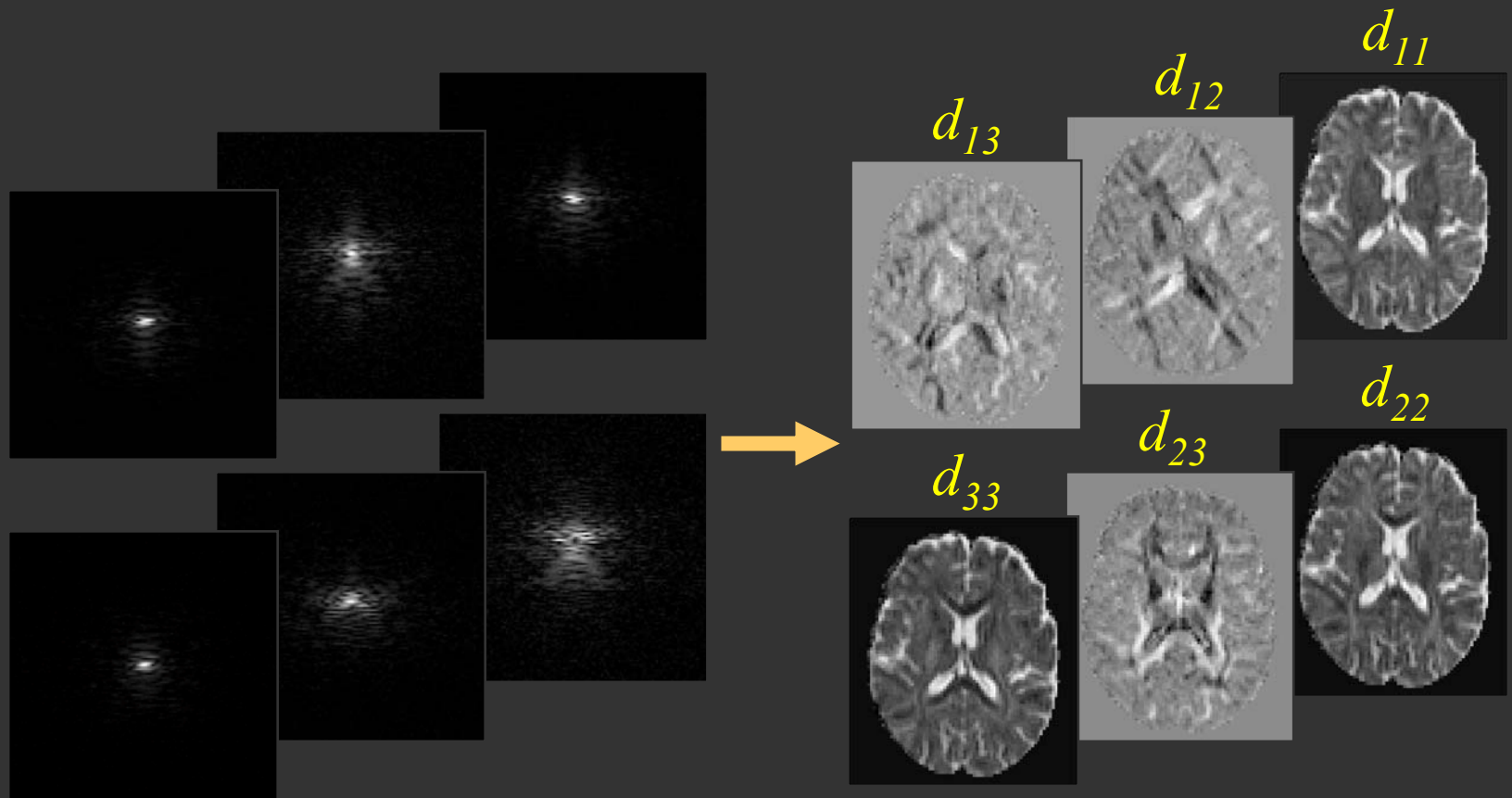
Reconstruct an **image** of
transverse magnetization



Diffusion MR data acquisition

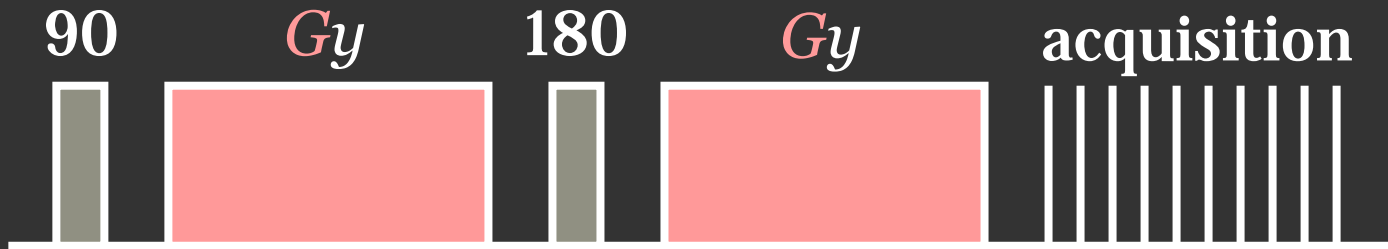
Must acquire at least 6 times as many MR signal measurements

Need to reconstruct 6 times as many values



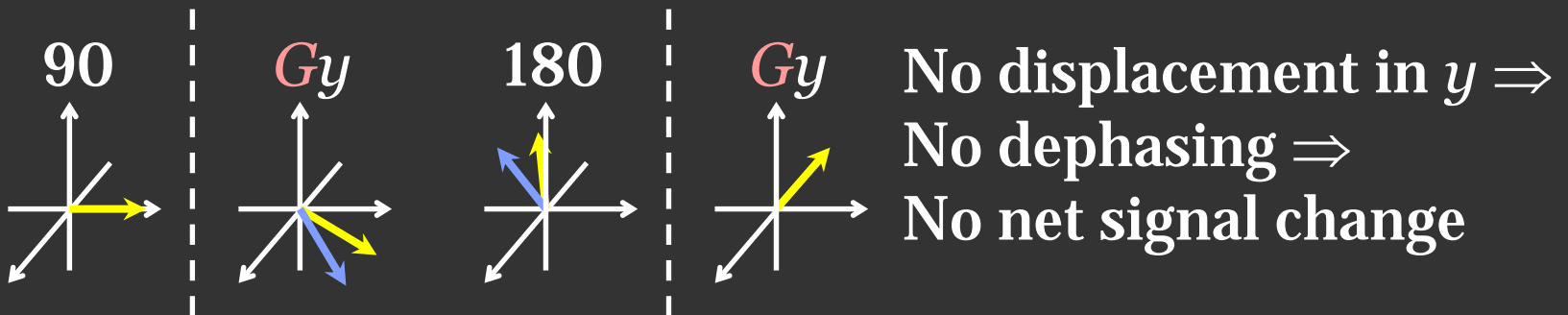
Diffusion encoding in MRI

- Apply two gradient pulses in some direction y :



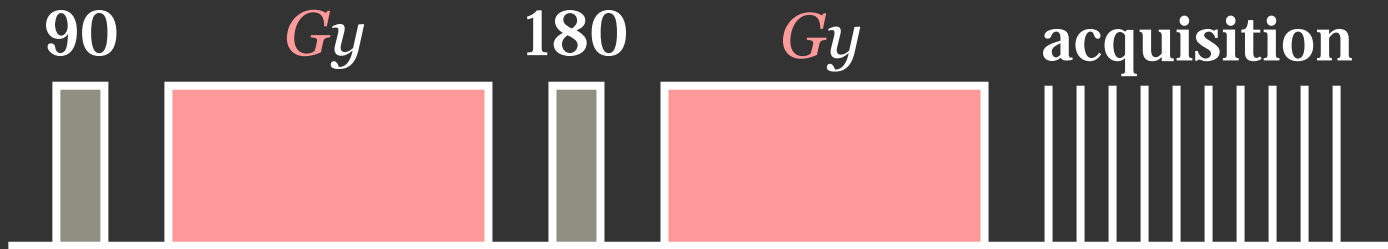
- Case 1: If spins aren't diffusing

$$y = y_1, y_2 \longrightarrow y = y_1, y_2$$



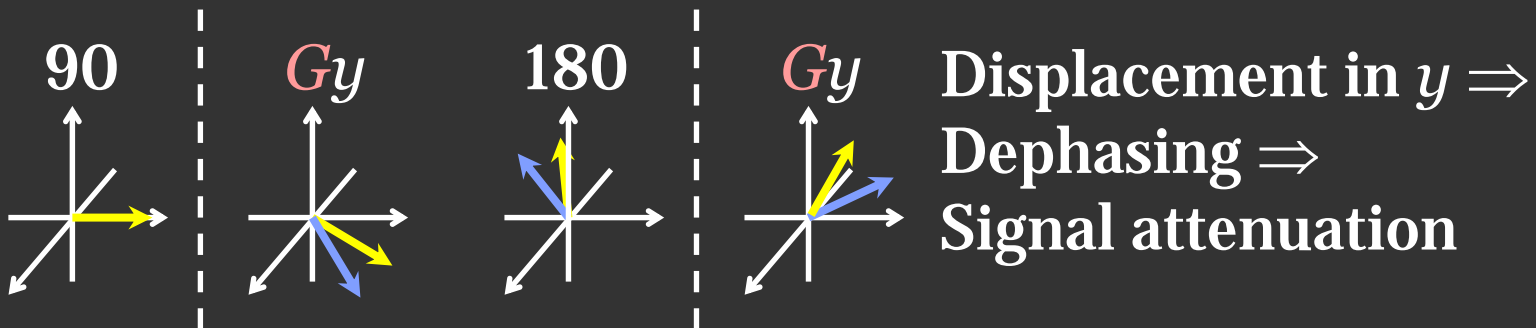
Diffusion encoding in MRI

- Apply two gradient pulses:



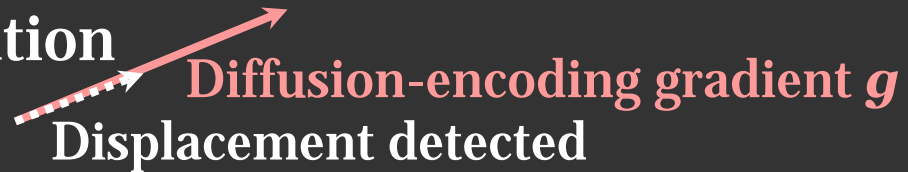
- Case 2: If spins are diffusing

$$y = y_1, y_2 \longrightarrow y = y_1 + \Delta y_1, y_2 + \Delta y_2$$



Choice 1: Gradient directions

- Spin diffusion direction \parallel Applied gradient direction
 \Rightarrow Maximum attenuation



- Spin diffusion direction \perp Applied gradient direction
 \Rightarrow No attenuation



- To capture all diffusion directions well, gradient directions should cover 3D space uniformly



How many directions?

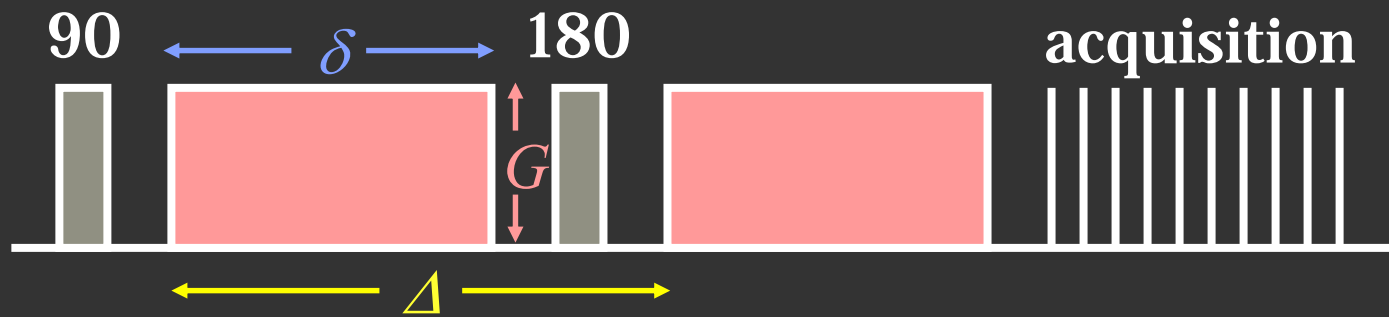
- Acquiring with more gradient directions leads to:
 - + More reliable estimation of diffusion measures
 - Increased imaging time \Rightarrow Subject discomfort, more susceptible to artifacts due to motion, respiration, etc.
- DTI:
 - Six directions is the minimum
 - Usually a few 10's of directions
 - Diminishing returns after a certain number [Jones, 2004]
- HARDI/DSI:
 - Usually a few 100's of directions

Choice 2: The b-value

- The b-value depends on acquisition parameters:

$$b = \gamma^2 G^2 \delta^2 (\Delta - \delta/3)$$

- γ the gyromagnetic ratio
- G the strength of the diffusion-encoding gradient
- δ the duration of each diffusion-encoding pulse
- Δ the interval b/w diffusion-encoding pulses



How high b-value?

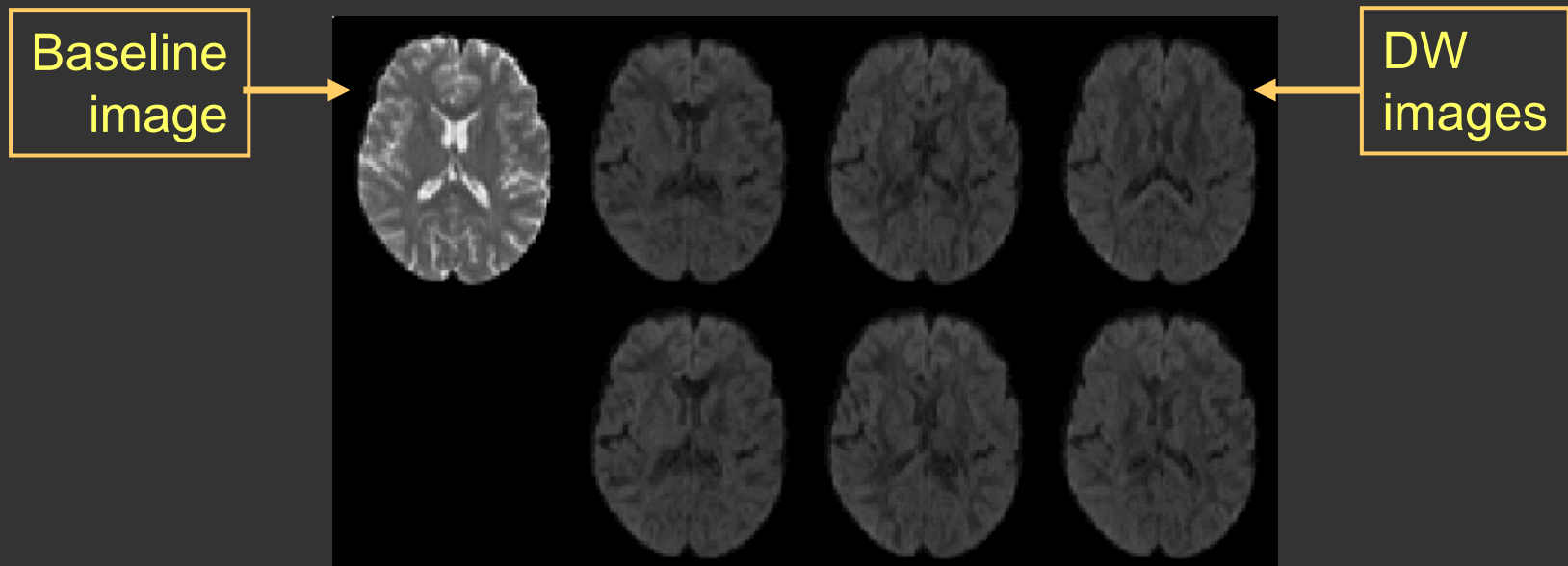
- Increasing the b-value leads to:
 - + Increased contrast b/w areas of higher and lower diffusivity in principle
 - Decreased signal-to-noise ratio \Rightarrow Less reliable estimation of diffusion measures in practice
- DTI: $b \sim 1000 \text{ sec/mm}^2$
- HARDI/DSI: $b \sim 10,000 \text{ sec/mm}^2$
- Data can be acquired at multiple b-values for trade-off
- Repeat acquisition and average to increase signal-to-noise ratio

Estimating the tensor

- $f_j^{b,g} = f_j^0 e^{-b \mathbf{g}' \cdot \mathbf{D}_j \cdot \mathbf{g}}$
where the \mathbf{D}_j the diffusion tensor at voxel j
- Design acquisition:
 - b the diffusion-weighting factor
 - \mathbf{g} the diffusion-encoding gradient direction
- Acquire images:
 - $f_j^{b,g}$ image acquired with diffusion-weighting factor b and diffusion-encoding gradient direction \mathbf{g}
 - f_j^0 “baseline” image acquired without diffusion-weighting ($b=0$)
- Estimate unknown diffusion tensor \mathbf{D}_j

Noise in diffusion-weighted images

- Due to signal attenuation by diffusion encoding, signal-to-noise ratio in DW images can be an order of magnitude lower than “baseline” image
- Eigenvalue decomposition is sensitive to noise, may result in negative eigenvalues



Distortions: Field inhomogeneities

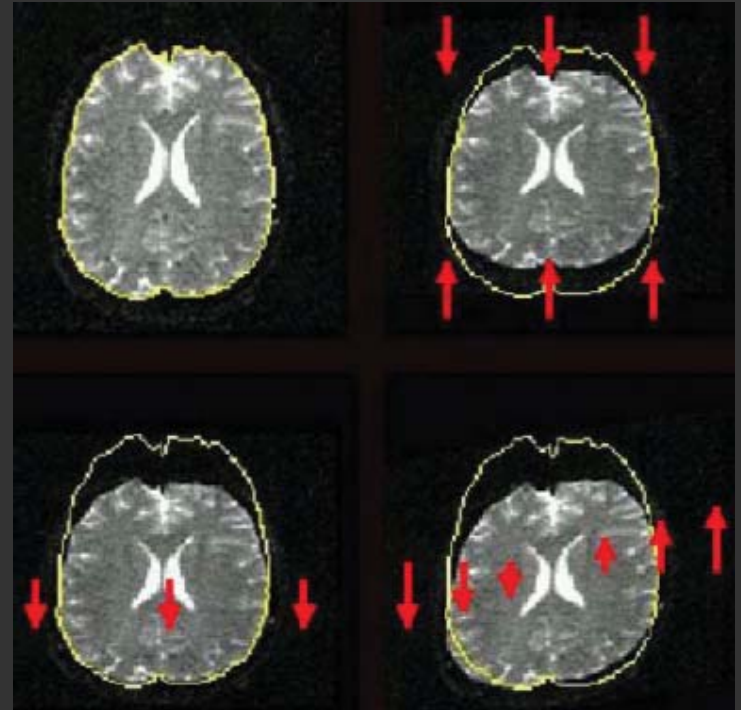
- Causes:
 - **Scanner-dependent** (imperfections of main magnetic field)
 - **Subject-dependent** (changes in magnetic susceptibility in tissue/air interfaces)
- Results: Signal loss in interface areas, geometric distortions

Signal loss



Distortions: Eddy currents

- Fast switching of diffusion-encoding gradients induces eddy currents in conducting components
- Eddy currents lead to residual gradients that shift the diffusion gradients
- The shifts are **direction-dependent**, *i.e.*, different for each DW image
- Results: Geometric distortions



Source: Le Bihan D., et al. "Artifacts and pitfalls in diffusion MRI." *JMRI* 24, no. 3 (2006): 478-488. Copyright © 2006 Wiley-Liss, Inc., A Wiley Company. Reprinted with permission of John Wiley & Sons., Inc.

Distortion correction

Post-process images to reduce distortions due to field inhomogeneities and eddy-currents:

- Either register distorted DW images to an undistorted (non-DW) image

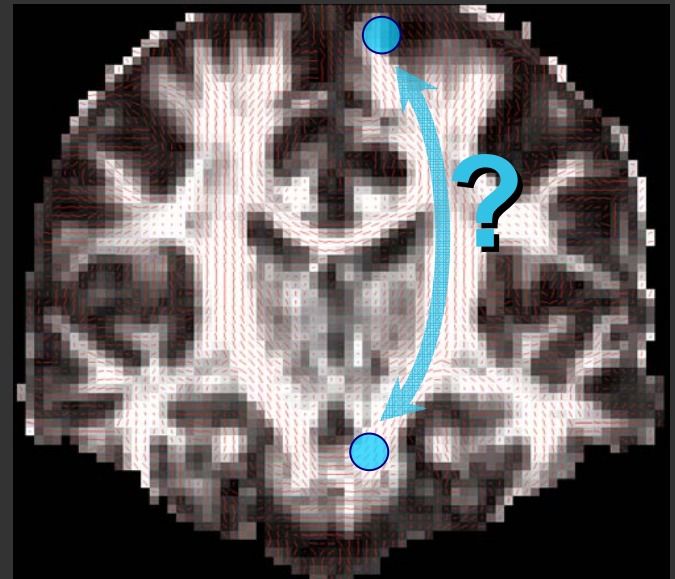
[Haselgrove'96, Bastin'99, Horsfield'99, Andersson'02, Rohde'04, Ardekani'05, Mistry'06]

- Or use information on distortions from separate scans (field map, residual gradients)

[Jezzard'98, Bastin'00, Chen'06; Bodammer'04, Shen'04]

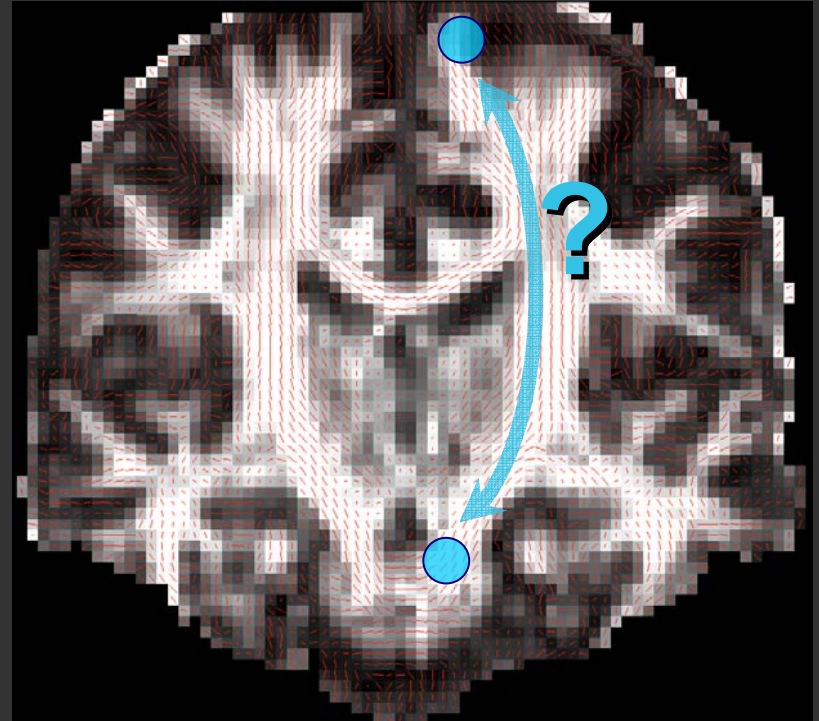
Tractography

- What does one do with diffusion data?
 - Statistical analysis on MD, FA, tensors...
 - **Tractography**: Given the diffusion data, determine “best” pathway between two brain regions
- Challenges in tractography:
 - Noisy, distorted images
 - Pathway crossings
 - High-dimensional space
- Many methods to overcome them...

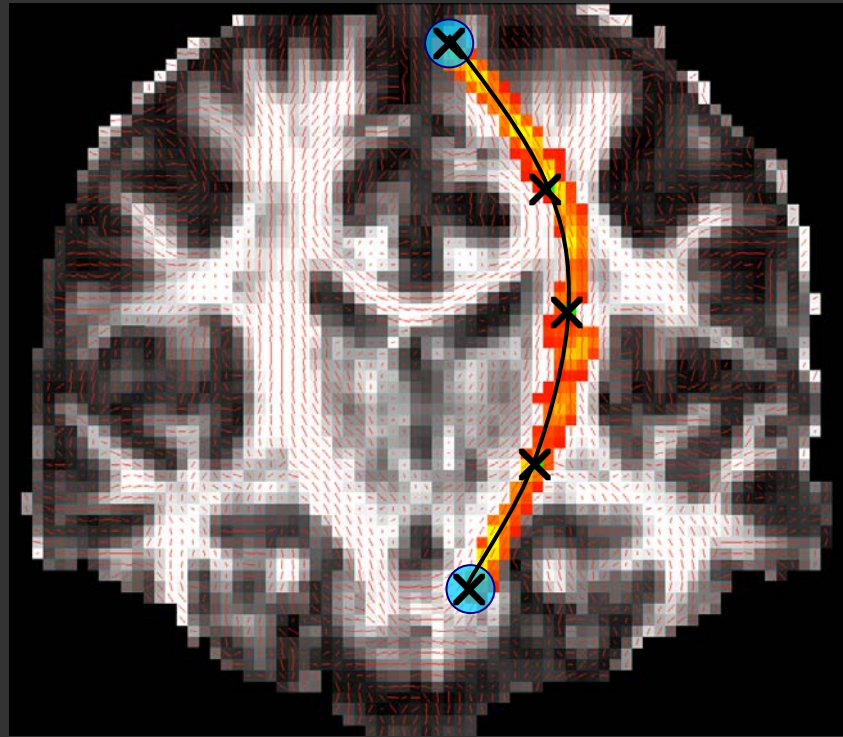
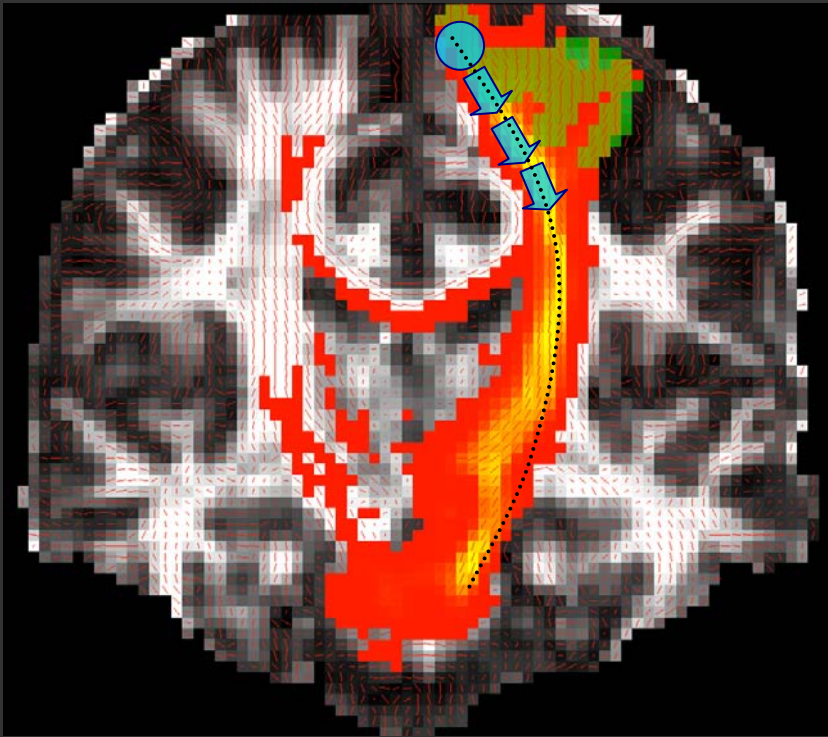


Deterministic vs. probabilistic

- **Deterministic methods:**
Model geometry of diffusion data, *e.g.*, tensor/eigenvectors [Conturo '99, Jones '99, Mori '99, Basser '00, Catani '02, Parker '02, O'Donnell '02, Lazar '03, Jackowski '04, Pichon '05, Fletcher '07, Melonakos '07, ...]
- **Probabilistic methods:**
Also model statistics of diffusion data [Behrens '03, Hagmann '03, Pajevic '03, Jones '05, Lazar '05, Parker '05, Friman '06, Jbabdi '07, ...]

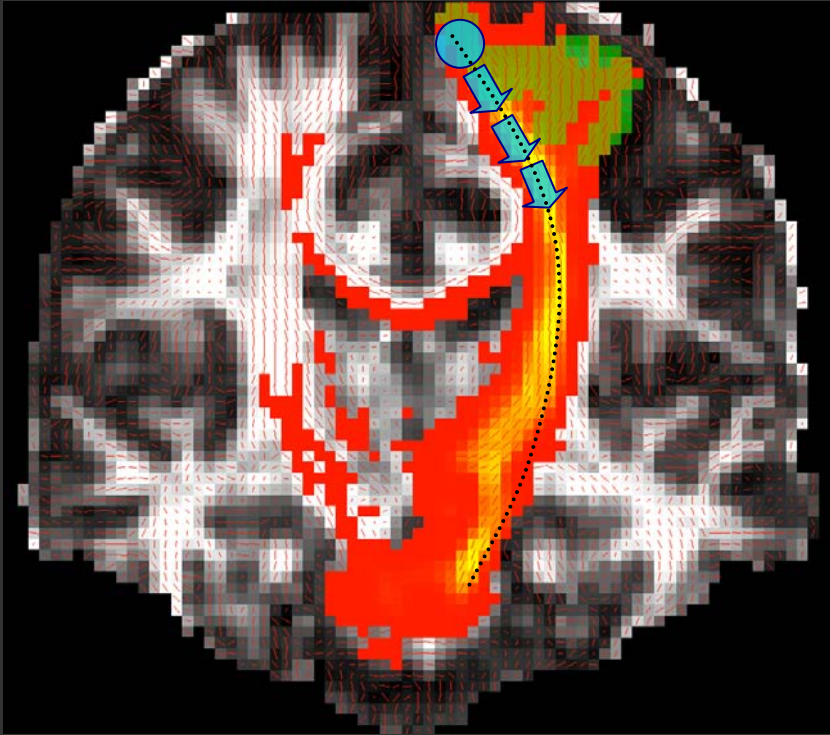


Local vs. global



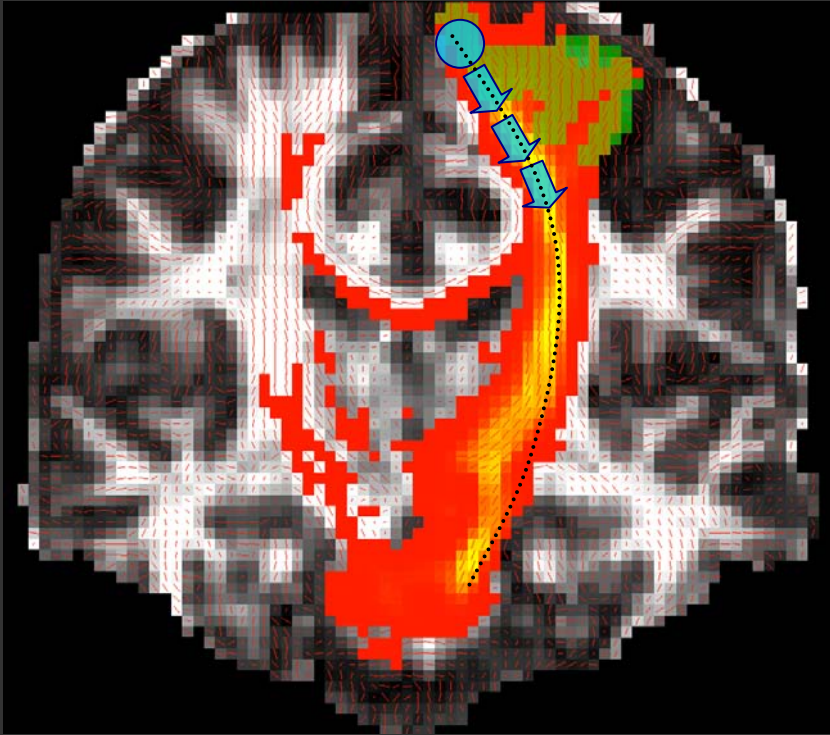
- **Local:** Uses local information to determine next step, errors propagate from areas of high uncertainty
- **Global:** Integrates information along the entire path

Local tractography



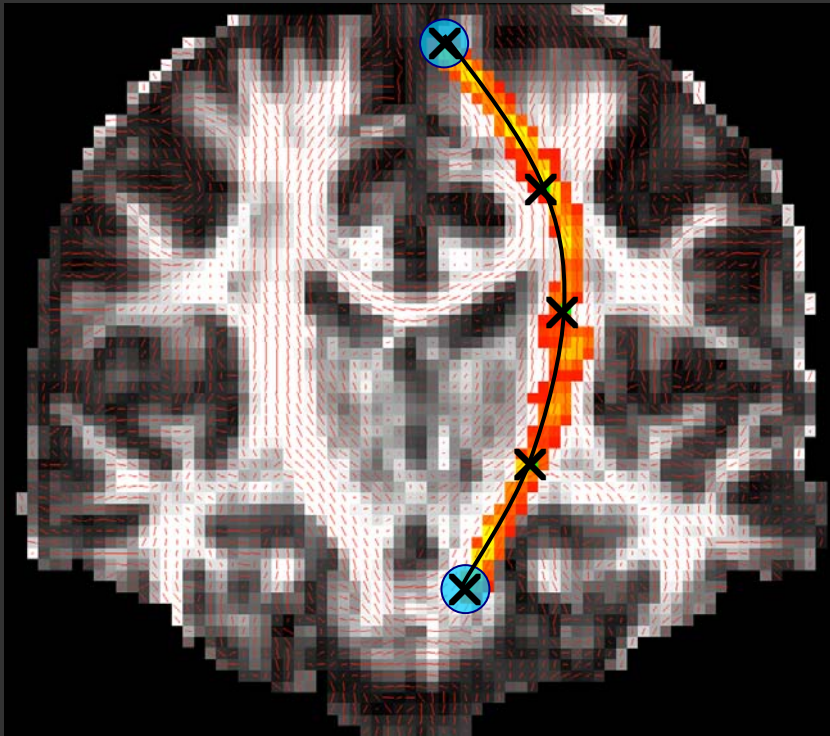
- Define a “**seed**” voxel or ROI to start the tract from
- Trace the tract by small steps, determine “best” direction at each step
- **Deterministic:** Only one possible direction at each step
- **Probabilistic:** Many possible directions at each step (because of noise), some more likely than others

Some issues



- Not constrained to a connection of the seed to a target region
- How do we isolate a specific connection? We can set a threshold, but how?
- What if we want a non-dominant connection? We can define waypoints, but there's no guarantee that we'll reach them.
- Not symmetric between tract “start” and “end” point

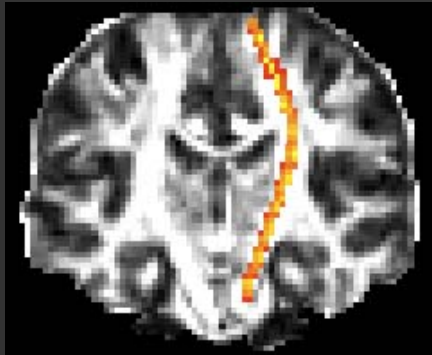
Global tractography



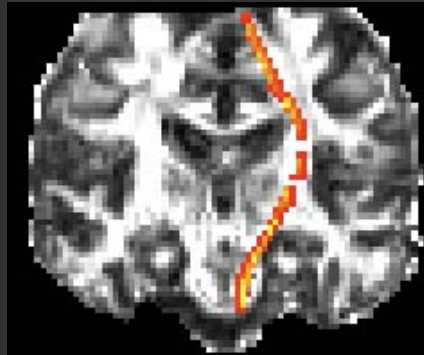
- Define a “seed” voxel or ROI
 - Define a “target” voxel or ROI
 - **Deterministic:** Only one possible path
 - **Probabilistic:** Many possible paths, find their probability distribution
-
- Constrained to a specific connection
 - Symmetric between seed and target regions

Application: Huntington's disease

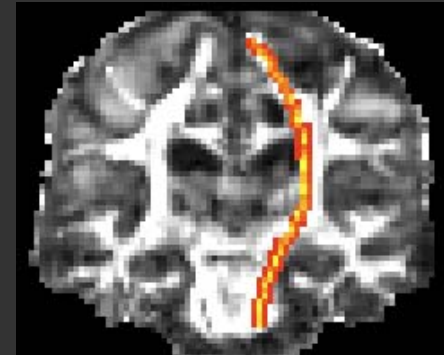
Data courtesy of Dr. D. Rosas, MGH



Healthy



Huntington's (premanifest)



Huntington's (advanced)

