### 18.335 Problem Set 5

## Problem 1:

(a) Trefethen, 36.3. Plot the error in this eigenvalue as a function of how many $A x$ matrix-vector multiplies you perform (use a semilog or log$\log$ scale as appropriate). (The files lanczos.m and A363.m posted on the web page are helpful.)
(b) Same problem, but use restarted Lanczos: after every 10 iterations of Lanzcos, restart with the best Ritz vector from those 10 iterations. Again, plot the error vs. matrix-vector multiply count.
(c) The above questions asked for the minimum- $\lambda$ eigenvalue (which may be negative). Plot what happens if, instead, you try to get the minimum$|\lambda|$ eigenvalue by these techniques. (Aside: a better way is to use Lanczos on $A^{-1}$, but that requires a fast way to solve $A x=b$ in order to multiply by $A^{-1}$.)

## Problem 2:

Trefethen, problem 38.6. (The files SD.m and A386.m on the web page are helpful.)

## Problem 3:

In problem 3 of the Fall 2008 midterm for 18.335, it was claimed that you could use the conjugategradient algorithm for a Hermitian positive semidefinite matrix $A$, with a random starting guess, to find a vector in the null space (see the midterm solutions). Demonstrate this by means of an example, in Matlab, and plot the norm of the residual vs. iteration. (You can construct a random positive-semidefinite matrix $A$ via, for example, $B=r a n d(198,200)$; $A=B \prime *$ B).

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