# Basic Practical diesel cycle

The textbook Diesel cycle is represented by all heat addition at constant pressure. The Otto cycle which is implemented by the spark ignition internal combustion engine adds all heat at constant volume. We will model a combined or dual (Seiliger) cycle with a portion of the heat added at constant volume, the remainder at constant pressure. Setting some parameters to be defined = 1 will reduce to either the Otto or Diesel cycle.

define some units

 $kN := 10^3 \cdot N$   $kPa := 10^3 \cdot Pa$  $MPa := 10^{6} Pa \quad kJ := 10^{3} \cdot J$  $kmol := 10^3 mol_{mol}$ 

This model will use an ideal air standard cycle with air as an ideal gas with constant specific heats and reversible processes to represent the behavior. The **gas relationships** are useful.

air-standard cycles ...

- 1. air as ideal gas is working fluid throughout cycle no inlet or exhaust process
- 2. combustion process replaced by heat transfer process
- 3. cycle is completed by heat transfer to surroundings
- 4. all processes internally reversible
- 5. usually constant specific heat (page 311)

## basic practical diesel cycle

Assumptions for analysis ...

- 1. reversible cycle with all reversible processes
- 2. working fluid is air assumed to be a perfect gas with constant specific heats,  $\gamma = c_p/c_v = 1.4$
- 3. mass of air in cylinder remains constant

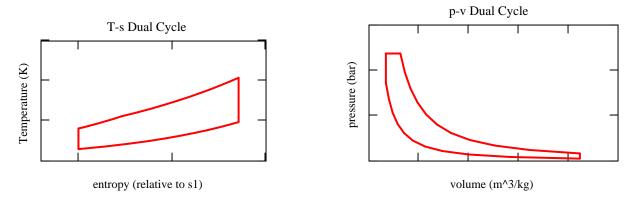
4. combustion processes are represented by heat transfer from an external source. Constant volume or constant pressure pocesses are done.

5. cycle is completed by cooling heat transfer to the surroundings until the air temperature and pressure return to the initial conditions of the cycle (constant volume process).

- 1-2 isentropic compression
- 2-3 constant volume heat addition
- 3-4 constant pressure heat addition
- 4-5 isentropic expansion
- 5-1 constant volume cooling

data for plot

this is the shape ...



next we will put numbers on the plots => themodynamic analysis of dual (Seiliger) cycle

The original notes are sourced from VanWylen and Sonntag. They could be revised to use the form of some of the relationships from Woud, but at considerable effort. Rather what follows is the application of the equations developed in the gas relationships lecture applied to the combined air-standard cycle deriving the relationships summarized in Table 7.3 Analytical prediction of the Selinger process on page 245 of the text.

$$r_{c}, a, b$$
  $r_{c} = \frac{v_{1}}{v_{2}}$   $a = \frac{p_{3}}{p_{2}}$   $b = \frac{v_{4}}{v_{3}}$ 

stage 1-2 isentropic adiabatic compression (expansion) \_\_\_\_\_\_ volume ratio known

$$r_{c} = \frac{v_{initial}}{v_{final}} = \frac{v_{1}}{v_{2}} \quad p_{final} = p_{initial} \left(\frac{v_{initial}}{v_{final}}\right)^{\gamma} = \left(\frac{v_{1}}{v_{2}}\right)^{\gamma} = r_{c}^{\gamma} \qquad T_{final} = T_{initial} \left(\frac{v_{initial}}{v_{final}}\right)^{\gamma-1} = \left(\frac{v_{1}}{v_{2}}\right)^{\gamma-1} = r_{c}^{\gamma-1}$$

$$\frac{v_{1}}{v_{2}} = r_{c} \qquad \qquad \frac{p_{final}}{p_{initial}} = r_{c}^{\gamma} \qquad \qquad \frac{T_{final}}{T_{initial}} = r_{c}^{\gamma-1}$$

stage 2-3
heat transfer at constant volume .... \_\_\_\_\_

$$\frac{p_3}{p_2} = a \qquad p_{initial} = \frac{R \cdot T_{initial}}{v_{constant} \cdot 100} \qquad p_{final} = \frac{R \cdot T_{final}}{v_{constant} \cdot 100} \qquad \frac{T_{final}}{T_{initial}} = \frac{p_{final}}{p_{initial}} = \frac{p_3}{p_2} = a \\ \frac{v_1}{v_2} = 1 \qquad \qquad \frac{p_3}{p_2} = a \qquad \qquad \frac{T_{final}}{T_{initial}} = a$$

stage 3-4

heat transfer at constant pressure ....

$$b = \frac{v_{\text{final}}}{v_{\text{initial}}} = \frac{v_4}{v_3} \qquad v_{\text{initial}} = \frac{R \cdot T_{\text{initial}}}{p_{\text{constant}} \cdot 100} \qquad v_{\text{final}} = \frac{R \cdot T_{\text{final}}}{p_{\text{constant}} \cdot 100} \qquad \frac{T_4}{T_3} = \frac{T_{\text{final}}}{T_{\text{initial}}} = \frac{v_{\text{final}}}{v_{\text{initial}}} = b$$

$$\frac{v_4}{v_3} = b \qquad \qquad \frac{P_4}{p_3} = 1 \qquad \qquad \frac{T_4}{T_3} = b$$

### stage 4-5 isentropic adiabatic compression (<u>expansion</u>)\_\_\_\_\_ volume ratio known

$$\frac{v_5}{v_4} = \frac{v_5}{v_3} \cdot \frac{v_3}{v_4} = \frac{v_5}{v_3} \cdot \frac{v_3}{v_4} = \frac{v_1}{v_2} \cdot \frac{v_3}{v_4} = \frac{r_c}{b} \qquad \text{as } v_5 = v_1 \text{ and } v_2 = v_3 \qquad [W \ 7.68 \ \& \ 7.69]$$

$$p_{\text{final}} = p_{\text{initial}} \cdot \left(\frac{v_{\text{initial}}}{v_{\text{final}}}\right)^{\gamma} = \left[p_4 \cdot \left(\frac{v_4}{v_5}\right)\right]^{\gamma} = p_4 \cdot \left(\frac{1}{\frac{r_c}{b}}\right)^{\gamma} = p_5$$

$$T_{\text{final}} = T_{\text{initial}} \left( \frac{v_{\text{initial}}}{v_{\text{final}}} \right)^{\gamma - 1} = T_4 \left( \frac{v_4}{v_5} \right)^{\gamma - 1} = T_4 \left( \frac{1}{\frac{r_c}{b}} \right)^{\gamma - 1} = T_5$$
  
$$\frac{v_5}{v_4} = \frac{r_c}{b} \qquad \qquad \frac{p_4}{p_5} = \left( \frac{r_c}{b} \right)^{\gamma} \qquad \qquad \frac{T_4}{T_5} = \left( \frac{r_c}{b} \right)^{\gamma - 1} \qquad \text{N.B. ratios are inconsistent 5/4 ... 4/5}$$

stage 5-1

heat transfer at constant volume .... \_

$$\frac{v_5}{v_1} = 1 \qquad p_{\text{initial}} = \frac{R \cdot T_{\text{initial}}}{v_{\text{constant}} \cdot 100} \qquad p_{\text{final}} = \frac{R \cdot T_{\text{final}}}{v_{\text{constant}} \cdot 100} \qquad \text{so} \dots \qquad \frac{p_{\text{initial}}}{p_{\text{final}}} = \frac{T_{\text{initial}}}{T_{\text{final}}} = \frac{p_5}{p_1} = \frac{T_5}{T_1}$$
$$\frac{p_5}{p_1} = \frac{p_5}{p_4} \cdot \left(\frac{p_4 = p_3}{p_1}\right) = \frac{p_5}{p_4} \cdot \frac{p_3}{p_2} \cdot \frac{p_2}{p_1} = \frac{1}{\left(\frac{r_c}{b}\right)^{\gamma}} \cdot a \cdot r_c^{\gamma} = a \cdot b^{\gamma}$$
$$\frac{v_5}{v_1} = 1 \qquad \qquad \frac{p_5}{p_1} = a \cdot b^{\gamma} \qquad \qquad \frac{T_5}{T_1} = a \cdot b^{\gamma}$$
this one is initial/final

# Now, applying the gas relationships to the calculation of states around the air-standard combined cycle

constants ...  $\gamma := 1.4$   $c_v := 0.7165 \frac{kJ}{kg \cdot K}$   $c_p := 1.0035 \frac{kJ}{kg \cdot K}$   $R := 0.287 \frac{kJ}{kg \cdot K}$ 

given ...  $T_1, v_1(calc), s_1, p_1, r_v, r_p, r_c$ 

$$T_1 := 295K \qquad s_1 := 1 \frac{kJ}{kg} \qquad p_1 := 1 \text{ bar } r_v := 12.5 \quad r_p := 1.38 \quad r_c := 1.86 \text{ } v_1 := \frac{R \cdot T_1}{p_1} \qquad v_1 = 0.847 \frac{m^3}{kg}$$

 $r_v = compression ratio r_c in text$ 

 $r_p$  = pressure ratio during constant volume heat addition = a in text

 $r_c$  = cut-off ratio. portion of stroke during which constant pressure heat addition occurs = b in text

$$r_v = \frac{v_1}{v_2} = r_c$$
  $r_p = \frac{p_3}{p_2} = a$   $r_c = \frac{v_4}{v_3} = b$ 

1-2 isentropic compression of air

$$\frac{\frac{\gamma-1}{T_2}}{T_1} = \left(\frac{p_2}{p_1}\right)^{\frac{\gamma}{r}} = \left(\frac{v_1}{v_2}\right)^{\gamma-1} \qquad (7.35) \quad \text{this .. for reversible} \\ \text{adiabatic process} \qquad \frac{T_2}{T_1} = \left(\frac{v_1}{v_2}\right)^{\gamma-1} \qquad p_2 = p_1 \cdot \left(\frac{v_1}{v_2}\right)^{\gamma} \\ s_2 \coloneqq s_1 \qquad v_2 \coloneqq \frac{v_1}{r_v} \qquad T_2 \coloneqq T_1 \cdot \left(\frac{v_1}{v_2}\right)^{\gamma-1} \qquad p_2 \coloneqq \frac{R \cdot T_2}{v_2} \\ v_2 = 0.068 \frac{m^3}{kg} \qquad T_2 = 810.188 \text{ K} \qquad p_2 = 34.33 \text{ bar}$$

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later we will plot on T-s and p-v so the relationships for intermediate states is shown. Any state value can serve as the plot parameter, but we will use temperature.

$$T_{1} \leq T\_plot \leq T_{2} \qquad s = s_{1} = s_{2} = constant$$

$$\frac{T_{2}}{T_{1}} = \left(\frac{v_{1}}{v_{2}}\right)^{\gamma-1} \text{ and } \dots \qquad \frac{T_{2}}{T_{1}} = \left(\frac{p_{2}}{p_{1}}\right)^{\frac{\gamma}{\gamma}} \text{ so } \dots \quad v\_plot = v_{1} \cdot \left(\frac{T_{1}}{T\_plot}\right)^{\frac{\gamma-1}{\gamma-1}} \text{ and } \dots \quad p\_plot = p_{1} \cdot \left(\frac{T\_plot}{T_{1}}\right)^{\frac{\gamma}{\gamma-1}}$$

2-3 constant volume heat addition using rp during constant volume portion of heat addition ...

 $v_3 \coloneqq v_2$   $p_3 \coloneqq p_2 \cdot r_p$   $p_3 = 47.375 \text{ bar}$  need to calculate  $T_3$   $v_2 = v_3$ 

$$\frac{\mathbf{p} \cdot \mathbf{v} = \mathbf{R} \cdot \mathbf{T}}{\mathbf{r}_{1}} \quad \frac{\mathbf{p}_{1} \cdot \mathbf{v}_{1}}{\mathbf{r}_{1}} = \frac{\mathbf{p}_{2} \cdot \mathbf{v}_{2}}{\mathbf{r}_{2}} \quad (\mathbf{3.5}) \quad \frac{\mathbf{p}_{3}}{\mathbf{r}_{3}} = \frac{\mathbf{p}_{2}}{\mathbf{r}_{2}} \quad \mathbf{r}_{3} \coloneqq \mathbf{T}_{2} \cdot \frac{\mathbf{p}_{3}}{\mathbf{p}_{2}} \quad \mathbf{r}_{3} = 1.118 \times 10^{3} \, \mathrm{K}$$

$$\frac{\mathbf{s}_{2} - \mathbf{s}_{1} = \mathbf{c}_{\mathrm{vo}} \cdot \ln\left(\frac{\mathbf{T}_{2}}{\mathbf{r}_{1}}\right) + \mathbf{R} \cdot \ln\left(\frac{\mathbf{v}_{2}}{\mathbf{v}_{1}}\right) \quad (\mathbf{7.21}) \quad \mathbf{c}_{\mathrm{vo}} = \mathrm{constant} \quad \mathbf{s}_{3} \coloneqq \left(\mathbf{s}_{2} + \mathbf{c}_{\mathrm{v}} \cdot \ln\left(\frac{\mathbf{T}_{3}}{\mathbf{r}_{2}}\right) \cdot \mathrm{K}\right) \quad \mathbf{s}_{3} = 1.231 \, \frac{\mathrm{kJ}}{\mathrm{kg}}$$

for later plotting

$$T_2 \le T_plot \le T_3$$
 s\_plot =  $s_2 + c_v \cdot ln\left(\frac{T_plot}{T_2}\right) \cdot K$ 

p-v are end points v = constant (straight lines) although intermediate states would be determined from the state equation ...

$$p_plot = \frac{R \cdot T_plot}{v_2}$$

# 3-4 heat added at constant pressure with rc.

$$\begin{aligned} \mathbf{v}_{4} \coloneqq \mathbf{v}_{3} \cdot \mathbf{r}_{c} & \mathbf{p}_{4} \coloneqq \mathbf{p}_{3} & \mathbf{T}_{4} \coloneqq \frac{\mathbf{p}_{4} \cdot \mathbf{v}_{4}}{\mathbf{R}} \\ \mathbf{v}_{4} &= 0.126 \frac{\mathbf{m}^{3}}{\mathbf{kg}} & \mathbf{p}_{4} = 47.375 \text{ bar} & \mathbf{T}_{4} &= 2.08 \times 10^{3} \text{ K} \end{aligned}$$

$$\begin{aligned} \mathbf{v}_{4} &= c_{126} \frac{\mathbf{m}^{3}}{\mathbf{kg}} & \mathbf{p}_{4} = 47.375 \text{ bar} & \mathbf{T}_{4} &= 2.08 \times 10^{3} \text{ K} \end{aligned}$$

$$\begin{aligned} \mathbf{v}_{2} - \mathbf{s}_{1} = \mathbf{c}_{po} \cdot \ln\left(\frac{\mathbf{T}_{2}}{\mathbf{T}_{1}}\right) - \mathbf{R} \cdot \ln\left(\frac{\mathbf{p}_{2}}{\mathbf{p}_{1}}\right) & (\mathbf{T}_{23}) & c_{po} = \text{constant} & \mathbf{s}_{4} \coloneqq \left(\mathbf{s}_{3} + \mathbf{c}_{p} \cdot \ln\left(\frac{\mathbf{T}_{4}}{\mathbf{T}_{3}}\right) \cdot \mathbf{K}\right) & \mathbf{s}_{4} = 1.854 \frac{\mathbf{k}J}{\mathbf{kg}} \end{aligned}$$

$$\begin{aligned} \mathbf{for \ later \ plotting} & \mathbf{s}_{-plot} \leq \mathbf{T}_{4} & \mathbf{s}_{-plot} = \mathbf{s}_{3} + \mathbf{c}_{p} \cdot \ln\left(\frac{\mathbf{T}_{-plot}}{\mathbf{T}_{2}}\right) \cdot \mathbf{K} & \mathbf{p} \cdot \mathbf{v} \ are \ end \ points \ \mathbf{v} = \text{constant} & \mathbf{v}_{-plot} = \frac{\mathbf{R} \cdot \mathbf{T}_{-plot}}{\mathbf{p}_{2}} \end{aligned}$$

$$\begin{aligned} \mathbf{f}_{3} \leq \mathbf{T}_{-plot} \leq \mathbf{T}_{4} & \mathbf{s}_{5} := \mathbf{v}_{1} & \mathbf{s}_{5} \coloneqq \mathbf{s}_{4} & \mathbf{s}_{5} = 1.854 \frac{\mathbf{k}J}{\mathbf{kg}} \end{aligned}$$

$$\begin{aligned} \mathbf{f}_{4} = \left(\frac{\mathbf{v}_{5}}{\mathbf{v}_{4}}\right)^{\gamma-1} & \mathbf{T}_{5} \coloneqq \mathbf{T}_{4} \cdot \left(\frac{\mathbf{v}_{4}}{\mathbf{v}_{5}}\right)^{\gamma-1} & \mathbf{T}_{5} = 970.553 \text{ K} \end{aligned}$$

$$\begin{aligned} \mathbf{f}_{5} \coloneqq \mathbf{R} \cdot \mathbf{T}_{5} & \mathbf{p}_{5} = 3.29 \text{ bar} \end{aligned}$$

as with isentropic compression above using T as the plot parameter ...

$$T_4 \ge T_plot \ge T_5$$
 decreasing ...  $s = s_4 = s_5 = constant$ 

$$\frac{T_5}{T_4} = \left(\frac{v_4}{v_5}\right)^{\gamma-1} \text{ and } \dots \quad \frac{T_5}{T_4} = \left(\frac{p_5}{p_4}\right)^{\frac{\gamma}{\gamma}} \text{ so } \dots \quad v_\text{plot} = v_4 \cdot \left(\frac{T_4}{T_\text{plot}}\right)^{\frac{\gamma}{\gamma-1}} \text{ and } \dots \quad p_\text{plot} = p_4 \cdot \left(\frac{T_\text{plot}}{T_4}\right)^{\frac{\gamma}{\gamma-1}}$$

 $s_{\rm ML} := \left( s_5 + c_{\rm V} \cdot \ln \left( \frac{T_1}{T_5} \right) \cdot K \right)$ 

# 5-1 constant volume cooling

and for later plotting ...

$$T_5 \ge T_{plot} \ge T_1$$
  $s_{plot} = s_5 + c_v \cdot \ln\left(\frac{T_{plot}}{T_5}\right) \cdot K$ 

decreasing ...

p-v are end points v = constant (straight lines) although intermediate states would be determined from the state equation ...

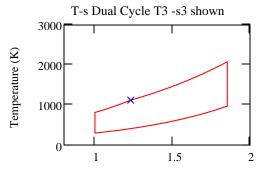
check closure of s<sub>1</sub>

 $s_1 = 1 \frac{kJ}{kg}$ 

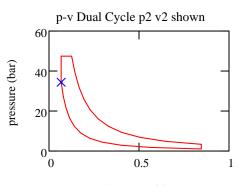
$$p\_plot = \frac{R \cdot T\_plot}{v_2}$$

$$\begin{pmatrix} T_1 \\ T_2 \\ T_3 \\ T_4 \\ T_5 \\ T_1 \end{pmatrix} = \begin{pmatrix} 295 \\ 810 \\ 1118 \\ 2080 \\ 971 \\ 295 \end{pmatrix} K \qquad \begin{pmatrix} s_1 \\ s_2 \\ s_3 \\ s_4 \\ s_5 \\ s_1 \end{pmatrix} = \begin{pmatrix} 1 \\ 1 \\ 1.231 \\ 1.854 \\ 1.854 \\ 1 \end{pmatrix} K \qquad \begin{pmatrix} p_1 \\ p_2 \\ p_3 \\ p_4 \\ p_5 \\ p_1 \end{pmatrix} = \begin{pmatrix} 1 \\ 34.33 \\ 47.375 \\ 3.29 \\ 1 \end{pmatrix} bar \qquad \begin{pmatrix} v_1 \\ v_2 \\ v_3 \\ v_4 \\ v_5 \\ v_1 \end{pmatrix} = \begin{pmatrix} 0.847 \\ 0.068 \\ 0.068 \\ 0.126 \\ 0.847 \\ 0.847 \end{pmatrix} K$$

now for plotting, including the intermediate values ... details in area below, relationships developed above



entropy (relative to s1)



volume (m^3/kg)

### now for calculations of efficiency

 $r_v = \text{compression ratio } r_v = \frac{v_1}{v_2}$ 

 $r_p = pressure ratio during constant volume heat addition <math>r_p = \frac{p_3}{p_2} = \frac{T_3}{T_2}$  at constant volume (ideal gas law pv=RT)

 $r_{c}$  = cut-off ratio. portion of stroke during which constant pressure heat addition occurs  $r_{c} = \frac{v_{4}}{v_{3}} = \frac{T_{4}}{T_{3}}$  at constant

pressure (ideal gas law pv=RT)

1-2 isentropic compression of air

$$\frac{\frac{\gamma-1}{T_2}}{T_1} = \left(\frac{p_2}{p_1}\right)^{\gamma-1} = \left(\frac{v_1}{v_2}\right)^{\gamma-1} \text{ this .. for reversible adiabatic process} \qquad \frac{T_2}{T_1} = \left(\frac{v_1}{v_2}\right)^{\gamma-1} = r_v^{\gamma-1} \qquad p_2 = p_1 \cdot \left(\frac{v_1}{v_2}\right)^{\gamma} = p_1 \cdot r_v^{\gamma}$$

2-3 constant volume heat addition using rp during constant volume portion of heat addition ...

$$Q_{H1} = m \cdot c_v \cdot (T_3 - T_2) = m \cdot c_v \cdot T_2 \cdot \left(\frac{T_3}{T_2} - 1\right) = m \cdot c_v \cdot T_2 \cdot (r_p - 1)$$

3-4 heat added at constant pressure with rc.

$$Q_{H2} = m \cdot c_p \cdot \left(T_4 - T_3\right) = m \cdot c_p \cdot T_3 \cdot \left(\frac{T_4}{T_3} - 1\right) = m \cdot c_p \cdot T_3 \cdot \left(r_c - 1\right) = m \cdot c_p \cdot T_2 \cdot \frac{T_3}{T_2} \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right) = m \cdot \gamma \cdot c_v \cdot T_2 \cdot r_p \cdot \left(r_c - 1\right)$$

5-1 constant volume cooling

substituting  $\gamma = c_p/c_v$  and  $r_p = T_3/T_2$ 

$$Q_{L} = -m \cdot c_{v} \cdot \left(T_{5} - T_{1}\right) = -m \cdot c_{v} \cdot T_{1} \cdot \left(\frac{T_{5}}{T_{1}} - 1\right)$$

$$\frac{T_{5}}{T_{1}} = \frac{p_{5}}{p_{1}} = \frac{p_{5}}{p_{4}} \cdot \frac{p_{4}}{p_{3}} \cdot \frac{p_{3}}{p_{2}} \cdot \frac{p_{2}}{p_{1}} = \left(\frac{v_{4}}{v_{5}}\right)^{\gamma} \cdot 1 \cdot r_{p} \cdot \left(\frac{v_{1}}{v_{2}}\right)^{\gamma} = \left(\frac{v_{4}}{v_{3}}\right)^{\gamma} \cdot r_{p} = r_{p} \cdot r_{c}^{\gamma} \qquad \Longrightarrow \qquad Q_{L} = -m \cdot c_{v} \cdot T_{1} \cdot \left(r_{p} \cdot r_{c}^{\gamma} - 1\right)$$

$$as v_{5} = v_{1} \text{ and } v_{2} = v_{3}$$

combining these for thermal efficiency of the cycle  $\ldots$ 

$$\begin{split} \eta_{th} &= 1 + \frac{Q_L}{Q_H} = 1 - \frac{T_1 \cdot \left(r_p \cdot r_c^{\gamma} - 1\right)}{T_2 \cdot \left[\left(r_p - 1\right) + \gamma \cdot r_p \cdot \left(r_c - 1\right)\right]} = 1 - \frac{r_p \cdot r_c^{\gamma} - 1}{r_v^{\gamma - 1} \cdot \left[\left(r_p - 1\right) + \gamma \cdot r_p \cdot \left(r_c - 1\right)\right]} & r_v = 12.5 \\ \eta_{th} &\coloneqq 1 - \frac{r_p \cdot r_c^{\gamma} - 1}{r_v^{\gamma - 1} \cdot \left[\left(r_p - 1\right) + \gamma \cdot r_p \cdot \left(r_c - 1\right)\right]} & \eta_{th} = 0.592 & r_c = 1.86 \end{split}$$

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and we could calculate the work per cycle

$$\mathbf{W} = \mathbf{Q}_{H1} + \mathbf{Q}_{H2} + \mathbf{Q}_{L} = \mathbf{m} \cdot \mathbf{c}_{v} \cdot \left(\mathbf{T}_{3} - \mathbf{T}_{2}\right) + \mathbf{m} \cdot \mathbf{c}_{p} \cdot \left(\mathbf{T}_{4} - \mathbf{T}_{3}\right) - \mathbf{m} \cdot \mathbf{c}_{v} \cdot \left(\mathbf{T}_{5} - \mathbf{T}_{1}\right)$$

m := 1 for per unit mass calculation in mcd

$$Q_{H1} := m \cdot c_v \cdot (T_3 - T_2) \qquad Q_{H1} = 220.59 \frac{kJ}{kg}$$

$$Q_{H2} := m \cdot c_p \cdot (T_4 - T_3) \qquad Q_{H2} = 964.897 \frac{kJ}{kg}$$

$$Q_L := -m \cdot c_v \cdot (T_5 - T_1) \qquad Q_L = -484.034 \frac{kJ}{kg}$$

$$W_{L} = Q_{H1} + Q_{H2} + Q_{L}$$
  $W = 701.453 \frac{kJ}{kg}$ 

N.B. this specific power is more than double LM 2500 another parameter describing diesel engines

# Indicated Mean Effective Pressure; Imep

$$Imep = \frac{work\_per\_stroke}{swept\_volume} = \frac{work}{V_1 - V_2} \qquad m = \frac{p_1 \cdot V_1}{R \cdot T_1} \qquad \underline{M}$$
$$Imep = \frac{W \cdot m}{V_1 - V_2} = \frac{W \cdot \frac{p_1 \cdot V_1}{R \cdot T_1}}{V_1 - V_2} = \frac{W \cdot \frac{p_1}{R \cdot T_1}}{1 - \frac{V_2}{V_1}} = \frac{W \cdot \frac{p_1}{R \cdot T_1}}{1 - \frac{1}{r_v}}$$
$$Imep := \frac{W \cdot \frac{p_1}{R \cdot T_1}}{1 - \frac{1}{r_v}} \qquad Imep = 9.005 \text{ bar}$$

consider indicated power, ref: Woud 7.4.2-3  $n_e = engine_rpm$ 

power\_per\_cyl = 
$$\frac{\text{work}_per_cycle}{\text{unit_time}}$$
time is period of power strokes = 1/freq = 1/(n\_e=engine\_rpm)2-stroke n\_e = # power  
strokes/time $P_i = \frac{W_i}{\text{period}_power_stroke} = \frac{W_i}{\frac{1}{\text{freq}} = \frac{1}{n_e = \text{engine}_rpm}} = W_i \cdot n_e$ 4-stroke n\_e = 2\*# power  
strokes/time $P_i = W_i \cdot \frac{n_e}{2}$  $k = \text{if (stroke = 2, 1, 2)}$ with ... $i = \text{number_of}_cylinders$ engine power is ... $P_i = W_i \cdot \frac{n_e \cdot i}{k} = \text{Imep} \cdot V_S \cdot \frac{n_e \cdot i}{k}$ 

brake power P<sub>B</sub>, power at engine drive flange, after mechanical losses in engine see Woud (7.12) and 7.4.1

can also express as ...

$$W1 := \eta_{th} \cdot \left(Q_{H1} + Q_{H2}\right)$$
$$W = 701.453 \frac{kW}{\frac{kg}{s}} \qquad W1 = 701.296 \frac{kW}{\frac{kg}{s}}$$

some diesel examples ...

# wartsila 32 (four stroke)

#### wartsila 64 (four stroke)

### Sulzer RT-flex96C, Sulzer RTA96C (two stroke)

 $W_{e} = \frac{effective\_work}{unit\_mass} = \frac{W_{i}}{mass} \cdot \eta_{mechanical}$ 

$$P_e = W_e \cdot \frac{n_e \cdot i}{k} = mep_e \cdot V_S \cdot \frac{n_e \cdot i}{k}$$

$$P_e = constant \cdot mep_e \cdot n_e \quad \text{for later discussion}$$

mep<sub>e</sub> = mean\_effective\_pressure = brake\_mean\_effective\_pressure = BMEP

$$\operatorname{mep}_{e} = \frac{\operatorname{P}_{e} \cdot k}{\operatorname{V}_{S} \cdot \operatorname{n}_{e} \cdot i} = \frac{\operatorname{P}_{e}}{\operatorname{V}_{S} \cdot \frac{\operatorname{n}_{e}}{k} \cdot i} = \frac{\operatorname{power\_per\_cyl}}{\operatorname{V}_{S} \cdot \frac{\operatorname{n}_{e}}{k}}$$

#### **COLT-PIELSTICK PC4.2B DATA**

Configuration Vee Only Bore 570 mm Stroke 660 mm **Engine Version 60 Hz Propulsion** Cylinder (nos) 10-12-16-18 Output Range (kW) 12,500-22,500 13,250-23,850 Speed (rpm) 400 400/430 Mean Eff. Pressure (bar) 22.3 22.3/22.0 Mean Piston Speed (m/s) 8.8 8.8/9.5 Output/cyl kW (hp) 1250 (1676) 1250 (1676)/1325 (1777) from: page 16 of **Fairbanks Morse medium speed diesel handbook** 

power\_per\_cyl := 1250kW 
$$n_e := \frac{400}{\min}$$
 n\_stroke := 4 k := if (n\_stroke = 2, 1, 2) bore := 570mm stroke := 660mm

$$V_{S} := \frac{\pi}{4} \cdot bore^{2} \cdot stroke$$
  $V_{S} = 5.948 \text{ ft}^{3}$   $mep_{e} := \frac{power\_per\_cyl}{V_{S} \cdot \frac{n_{e}}{k}}$   $mep_{e} = 22.266 \text{ bar}$  as stated in data above

two special cases (can be calculated above setting  $\rm r_{p}$  and  $\rm r_{c}$  appropriately ...

### Otto cycle - spark ignition engine heat added at TDC (constant volume) only extra subscript added for special designation

air-standard Otto cycle: *spark* ignition internal-combustion engine

1-2 isentropic compression of air

2-3(=4) heat added at constant volume (piston momentarily at rest at tdc

4-5 isentropic expansion

5-1 heat rejection at constant volume (piston at crank-end dead center)

from air standard dual cycle above

$$\eta_{\text{th}} = 1 + \frac{Q_{\text{L}}}{Q_{\text{H}}} = 1 - \frac{T_{1} \cdot \left(r_{\text{p}} \cdot r_{\text{c}}^{\gamma} - 1\right)}{T_{2} \cdot \left[\left(r_{\text{p}} - 1\right) + \gamma \cdot r_{\text{p}} \cdot \left(r_{\text{c}} - 1\right)\right]} = 1 - \frac{r_{\text{p}} \cdot r_{\text{c}}^{\gamma} - 1}{r_{\text{v}}^{\gamma - 1} \cdot \left[\left(r_{\text{p}} - 1\right) + \gamma \cdot r_{\text{p}} \cdot \left(r_{\text{c}} - 1\right)\right]}$$

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$$\mathbf{r_{co}} \coloneqq \mathbf{1} \qquad \qquad \eta_{\text{th\_otto}} \coloneqq \mathbf{1} - \frac{\mathbf{r_{po}} \cdot \mathbf{r_{co}}^{\gamma o} - 1}{\mathbf{r_{vo}}^{\gamma o - 1} \cdot \left[ \left( \mathbf{r_{po}} - 1 \right) + \gamma o \cdot \mathbf{r_{po}} \cdot \left( \mathbf{r_{co}} - 1 \right) \right]} \qquad \qquad \eta_{\text{th\_otto}} \rightarrow 1 - \frac{1}{\mathbf{r_{vo}}^{\gamma o - 1}}$$

$$\mathbf{r}_{\text{MAX}} = 1.0 \qquad \mathbf{r}_{\text{MAX}} = 5 \quad \mathbf{r}_{\text{MAX}} = \begin{bmatrix} 10 \\ 15 \end{bmatrix} \qquad \eta_{\text{th}\_\text{otto}} = 1 - \frac{1}{\mathbf{r}_{\text{V}}^{\gamma - 1}} \qquad \text{removing o} \\ \mathbf{designation} \qquad \eta_{\text{th}\_\text{otto}} = \begin{bmatrix} 0.602 \\ 0.661 \end{bmatrix}$$

# and ... Diesel cycle ... all heat added at constant pressure

air-standard Diesel cycle: compression ignition internal-combustion engine

1-2(=3) isentropic compression of air

3-4 heat added at constant *pressure* (gas expanding during heat addition)

4-5 isentropic expansion

5-1 heat rejection at constant volume (piston at crank-end dead center)

$$\mathbf{r}_{pd} \coloneqq 1 \quad \eta_{th\_diesel} \coloneqq 1 - \frac{\mathbf{r}_{pd} \cdot \mathbf{r}_{cd}^{\gamma d} - 1}{\mathbf{r}_{vd}^{\gamma d-1} \cdot \left[ \left( \mathbf{r}_{pd} - 1 \right) + \gamma d \cdot \mathbf{r}_{pd} \cdot \left( \mathbf{r}_{cd} - 1 \right) \right]} \qquad \eta_{th\_diesel} \rightarrow 1 - \frac{\mathbf{r}_{cd}^{\gamma d} - 1}{\mathbf{r}_{vd}^{\gamma d-1} \cdot \gamma d \cdot \left( \mathbf{r}_{cd} - 1 \right)}$$

$$\mathbf{r}_{vd} \coloneqq 2.5 \qquad \mathbf{r}_{pq} \coloneqq 1 \quad \mathbf{r}_{v} \coloneqq \begin{pmatrix} 10 \\ 15 \\ 20 \end{pmatrix} \qquad \eta_{th\_diesel} \coloneqq 1 - \frac{\mathbf{r}_{c}^{\gamma} - 1}{\mathbf{r}_{v}^{\gamma - 1} \cdot \gamma \cdot \left( \mathbf{r}_{c} - 1 \right)} \qquad \eta_{th\_diesel} \equiv \begin{pmatrix} 0.506 \\ 0.58 \\ 0.625 \end{pmatrix}$$

# Relate r<sub>c</sub>, a, b to efficiency

$$r_v = \frac{v_1}{v_2} = r_c$$
  $r_p = \frac{p_3}{p_2} = a$   $r_c = \frac{v_4}{v_3} = b$ 

▶ reset variables

$$\begin{split} \eta_{th} &\coloneqq 1 - \frac{r_{p} \cdot r_{c}^{\gamma} - 1}{r_{v}^{\gamma-1} \cdot \left[ \left(r_{p} - 1\right) + \gamma \cdot r_{p} \cdot \left(r_{c} - 1\right) \right]} \end{split}$$

substitute, var1 = var2, where var1 is to be replaced

$$\eta_{\text{th}} \text{ substitute}, r_{\text{v}} = r_{\text{cc}}, r_{\text{p}} = a, r_{\text{c}} = b, \gamma = \kappa \rightarrow 1 - \frac{a \cdot b^{\kappa} - 1}{r_{\text{cc}} \cdot 4 \cdot [a - 1 + a \cdot (b - 1) \cdot \kappa]}$$
[W 7.87]