

Bayes' Theorem

$$P(A/E)P(E) = P(A, E)$$

$$P(E/A)P(A) = P(A, E)$$

$$P(A/E) = P(E/A)P(A)/P(E)$$

Bayesian Updating

$$F' = CFP(E)$$

F': Updated Probability Distribution

F: Prior Probability Distribution

C: Proportional Constant

E: Evidence

USE OF EXPERTS & BAYES' THEOREM

Experts can be used either to provide

1. Model of belief (e.g., our subjectively obtained distribution of alternative causes of Egypt Air plane crash).
2. Model of the world \Rightarrow assignment of most likely alternatives or outcome (i.e., provides evidence as his/her expert opinion as if the evidence were resulting from a random trial).

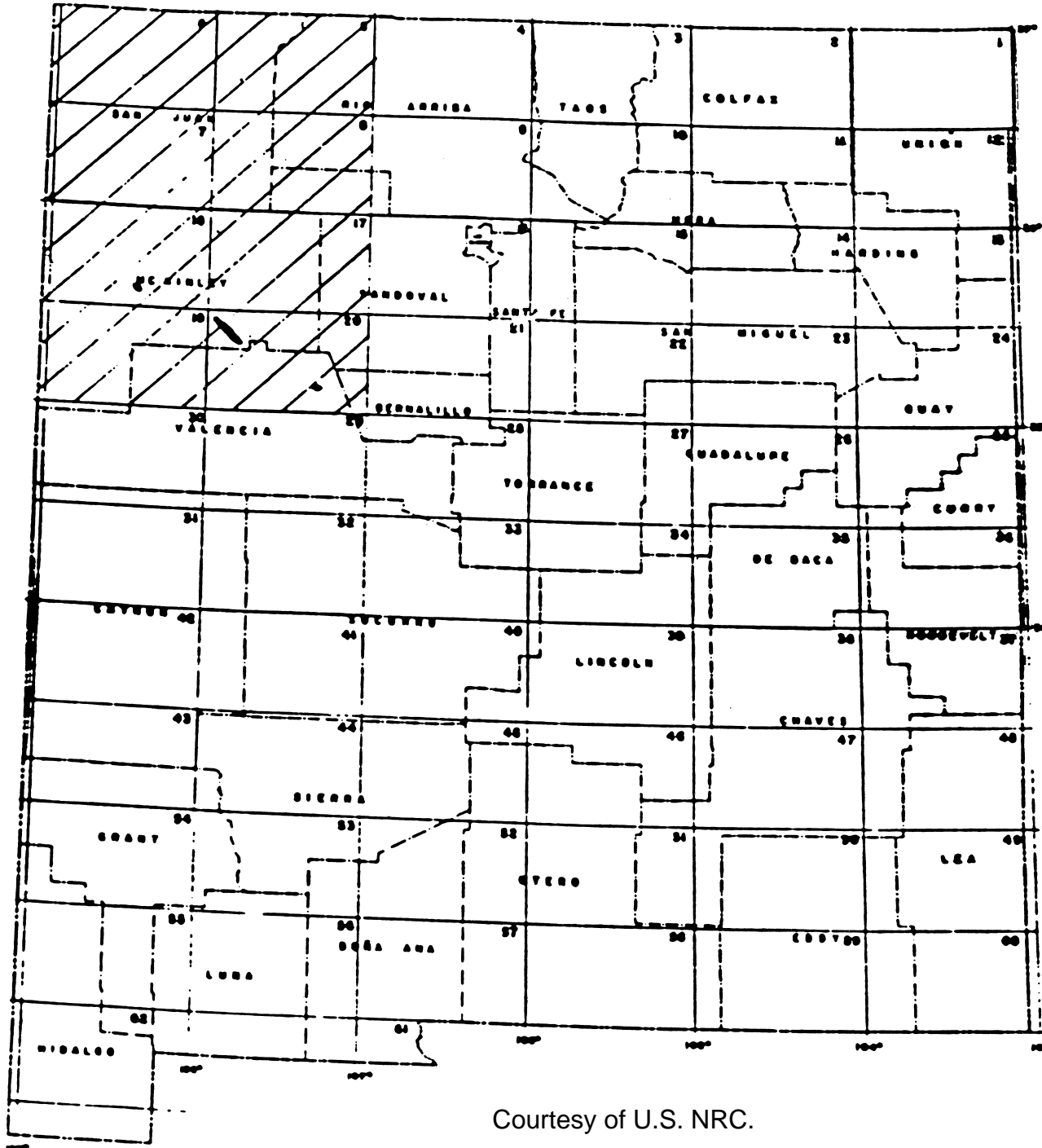
Former Case: New evidence can be used to update a subjective model of belief just as with any other model of belief.

Latter Case: $P(\Theta = \theta_i | E = e_j)$ is posterior probability distribution based upon evidence obtained from an expert.

$$= \frac{P(E = e_j | \Theta = \theta_i) P(\Theta = \theta_i)}{P(E = e_j)}, \text{ where}$$

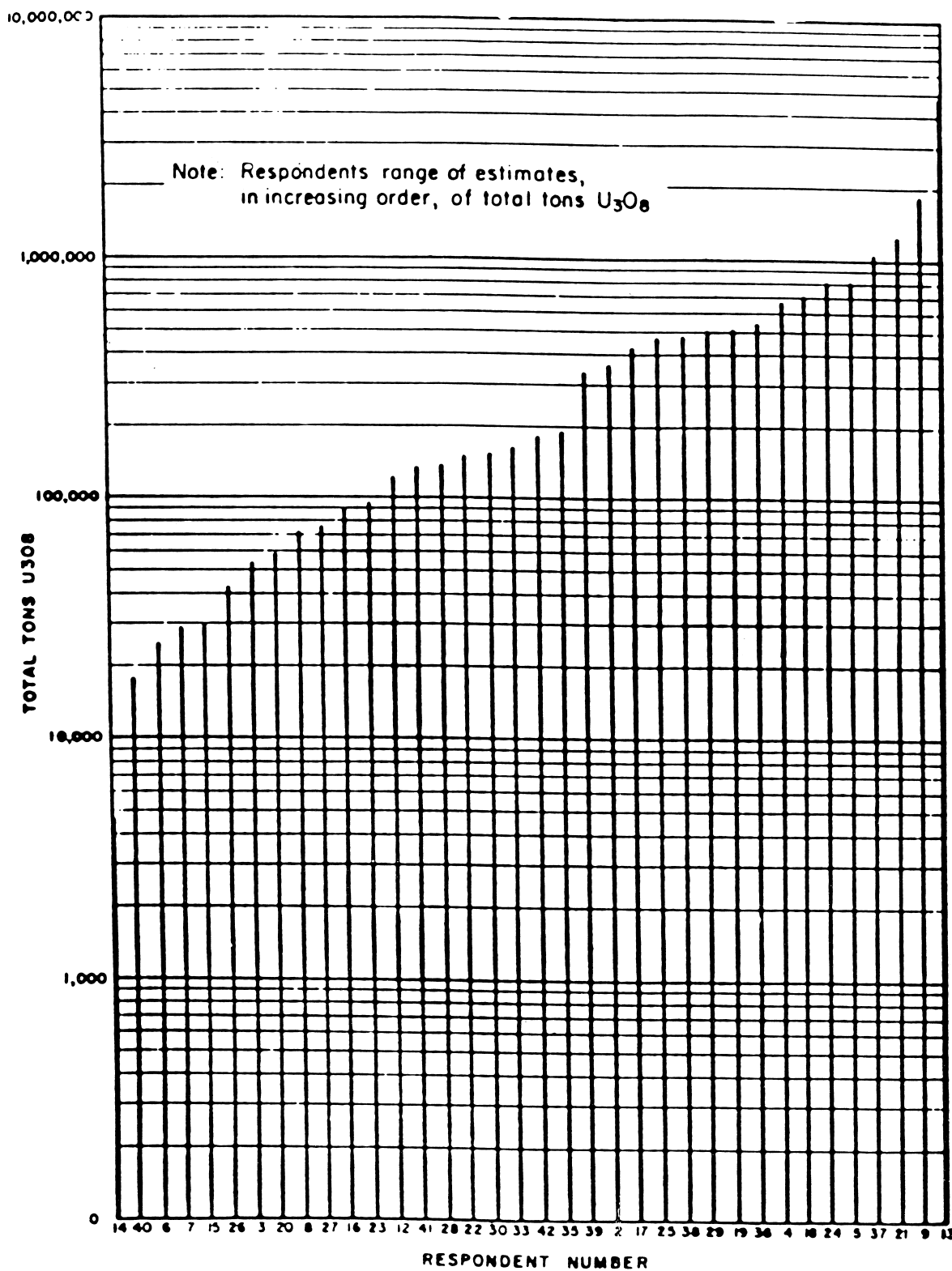
$P(E = e_i | \Theta = \theta_j)$ is observer's judgment of the probability that expert will give evidence, e_j , when observer believes that $\Theta = \theta_j$.

SUBJECTIVE PROBABILITY STUDY – STATE OF NEW MEXICO



Courtesy of U.S. NRC.

NEW MEXICO SUBJECTIVE PROBABILITY STUDY (AFTER DELPHI)



Courtesy of U.S. NRC.