- Understand how deferral, deductibility & rate differences affect after-tax returns
- Discuss key features of competing investment structures



Assumptions

- Same underlying security
 - Pre-tax return (R) = 7%
- Tax rates constant across time & individuals
 - Tax rate on ordinary income (t) = 30%
 - Tax rate on capital gains (tg) = 15%
- No frictions (transaction costs)
- Certainty
- \$100 initial investment



Savings Vehicles

- Savings vehicles differ on three dimensions
 - Is the investment deductible? (yes / no)
 - Are earnings tax deferred? (yes / no)
 - What tax rates apply? (ordinary "t" / capital "tg" / exempt)



- Other examples (savings accounts, corporate bonds, etc.)
- Characteristics
 - No deduction
 - No deferral
 - Ordinary rates
- ► Not "tax" advantaged



► After-tax accumulation (ATA):

 $ATA = [(1+R) - tR]^n = [1+R(1-t)]^n$

- ► After-tax rate of return:
 - $\mathbf{r} = \{ [1 + R(1 t)]^n \}^{1/n} 1 = R(1 t)$
- Observations:

"r" does not depend on horizon



Type II: Single Premium Deferred Annuity (SPDA)

- Other example (non-deductible IRA)
- Characteristics
 - No deduction
 - Deferral
 - Ordinary rates



Type II: Single Premium Deferred Annuity (SPDA)

► After-tax rate of return:

 $r = \{(1+R)^n (1-t) + t\}^{1/n} - 1$

• Observations:

"r" grows with horizon because of deferral SPDA dominates MM if n>1



Type III: Mutual Fund With All Capital Gains

- ► Assumes 100% turnover each year
- Characteristics
 - No deduction
 - No deferral
 - Capital gains rates



Type III: Mutual Fund With All Capital Gains

► After-tax accumulation (ATA):

 $ATA = [(1+R) - tgR]^n = [1+R(1-tg)]^n$

After-tax rate of return:

$$\mathbf{r} = \{ [1+\mathbf{R} (1-\mathbf{t}g)]^n \}^{1/n} - 1 = \mathbf{R}(1-\mathbf{t}g) \}$$

• Observations:

Same as MM but replace "t" with "tg" "g" is inclusion factor, so tcg = tg (e.g. if tcg = 28% and t = 40% then g=0.28/0.40 = 0.70)

If g < 1 dominates MM



- Other example (growth stock without dividends)
- Characteristics
 - No deduction
 - Deferral
 - Capital gains rates



► After-tax accumulation (ATA):

ATA= $(1+R)^n - [(1+R)^n - 1]tg = (1+R)^n(1-tg) + tg$

After-tax rate of return:

 $r = \{(1{+}R)^n (1{-}tg) + tg\}^{1/n} - 1$

• Observations:

Same as SPDA but taxed at capital gains rate Dominates SPDA if g<1 Dominates III (mutual fund w/ all cg) if n>1 "r" grows with horizon because of deferral



Type V: Insurance Policy or Tax Exempt Munis

- Characteristics
 - No deduction
 - Permanent Deferral (Never taxed assuming away the AMT)



Type V: Insurance Policy or Tax Exempt Munis

► After-tax accumulation (ATA):

 $ATA = (1+R)^n$

• After-tax rate of return:

 $r = \{(1+R)^n\}^{1/n} - 1 = R$

• Observations:

Dominates I through IV (Assuming pretax rate of return is the same across all assets. Ignores implicit taxes.)



Type VI: Pension Fund or Deductible IRA

- Characteristics
 - Deduction
 - Deferral
 - Ordinary rates



Type VI: Pension Fund or Deductible IRA

► **IF** $t_o = t_n$

► After-tax accumulation (ATA):

ATA=
$$\underline{1}_{1-t_o}(1+R)^n(1-t_n) = (1+R)^n$$

► After-tax rate of return:

$$\mathbf{r} = \{ \frac{1}{1-t_o} (1+R)^n (1-t_n) \}^{1/n} - 1$$

= (1+R) {(1-t_n)/(1-t_o)}^{1/n} - 1 = R



Type VI: Pension Fund or Deductible IRA

• Observations:

- Equivalent to tax-exempt muni when $t_o = t_n$
- Government as partner allows you to invest 1/(1-t_o) but takes its cut at the end
- Is comparison to munis fair in this case?



- Tax exempt saving no longer equivalent to saving through a pension
 - If tax rates are rising over time, pensions and SPDAs become less attractive
 - If tax rates are falling, pensions and SPDAs become more attractive
- How does time horizon affect your decisions regarding a pension investment?



Ordinary tax rates

Individuals Maximum rate 2000 39.6% 2001 39.1% 2002 38.6% 2003 38.6%

► Corporations

0 - 50,000	15%
50,000 - 75,000	25%
75,000 - 100,000	34%
100,000 - 335,000	39%
335,000 - 10,000,000	34%
10,000,000 - 15,000,000	35%
15,000,000 - 18,333,333	38%
>18,333,333	35%



Capital gains and losses

- ► Short term < 1 year
- ► Long term >1 year
- Netting rules
 - Net short-term gains and losses and long-term gains and losses
 - If both are net gains or net losses, do no more netting
 - Otherwise net the two



Individuals

- ► Gains
 - Ordinary rates for short term capital gains (STCG)
 - Special rates for long term capital gains (LTCG), held > 12 months
 - After December 31, 2000 (generally)
 - Maximum rate of 20% (10% if in 10 or 15% bracket)
 - Special rate of 18% / 8% if held for more than 5 years
 - Prior law:
 - maximum of 28% for LTCG



Individuals

- ► Losses
 - Can deduct up to \$3,000 of net capital losses (investment property) per year
 - Net capital losses can be carried over indefinitely



Corporations

- No special tax rate for LTCG
 - (actually, there is, but it's equal to 35%)
- A corporation's capital loss may only be used to offset capital gains
- Get 3 year carryback and 5 year carryforward for NCL

