## MITOCW | MITRES6_012S18_L11-04_300k

Let us now consider an application of what we have done so far.
Let X be a normal random variable with given mean and variance.

This means that the PDF of $X$ takes the familiar form.

We consider random variable $Y$, which is a linear function of $X$. And to avoid trivialities, we assume that a is different than zero.

We will just use the formula that we have already developed.

So we have that the density of Y is equal to 1 over the absolute value of a .

And then we have the density of $X$, but evaluated at $x$ equal to this expression.

So this expression will go in the place of x in this formula.

And we have y minus b over a minus mu squared divided by 2 sigma squared.

And now we collect these constant terms here.

And then in the exponent, we multiply by a squared the numerator and the denominator, which gives us this form here.

We recognize that this is again, a normal PDF.

It's a function of $y$.

We have a random variable Y . This is the mean of the normal.

And this is the variance of that normal.

So the conclusion is that the random variable $Y$ is normal with mean equal to $b$ plus a mu.

And with variance a squared, sigma squared.

The fact that this is the mean and this is the variance of Y is not surprising.

This is how means and variances behave when you form linear functions.

The interesting part is that the random variable Y is actually normal.

Intuitively, what happened here is that we started with a normal bell shaped curve.

A bell shaped PDF for $X$. We scale it vertically and horizontally, and then shift it horizontally by $b$.

As we do these operations, the PDF still remains bell shaped.

And so the final PDF is again a bell shaped normal PDF.

